



3109 Cornelius Drive  
Bloomington, IL 61704  
309.807.2300  
pinnacleactuaries.com  
Roosevelt C. Mosley, Jr., FCAS, MAAA, CSPA  
[rmosley@pinnacleactuaries.com](mailto:rmosley@pinnacleactuaries.com)  
Direct: 309.807.2330

November 12, 2020

The Honorable Dana T. Wade  
Assistant Secretary for Housing and Federal Housing Commissioner  
U.S. Department of Housing and Urban Development  
451 Seventh Street, S.W., Room 9100  
Washington, D.C. 20410

Dear Commissioner Wade:

Pinnacle Actuarial Resources, Inc. (Pinnacle) has completed the final report for the Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund Forward Loans. The attached report details our estimate of the Cash Flow Net Present Value for Fiscal Year 2020 as of September 30, 2020.

Roosevelt C. Mosley, Jr., FCAS, MAAA is responsible for the content and conclusions set forth in the report. I am a Fellow of the Casualty Actuarial Society and a member of the American Academy of Actuaries, and am qualified to render the actuarial opinion contained herein.

It has been a pleasure working with you and your team to complete this study. I remain available for any questions or comments you have regarding the report and its conclusions.

Respectfully Submitted,

A handwritten signature in black ink that reads "Roosevelt Mosley".

Roosevelt C. Mosley, Jr., FCAS, MAAA, CSPA  
Principal and Consulting Actuary

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Net Worth of Forward Mortgage Insurance-In-Force

---

*Final Report Based on Data as of September 30, 2020*

November 12, 2020



3109 Cornelius Drive  
Bloomington, IL 61704  
309.807.2300  
pinnacleactuaries.com

*Commitment Beyond Numbers*



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

## Table of Contents

Summary of Findings .....	1
Executive Summary .....	6
Impact of Economic Forecasts.....	6
Distribution and Use.....	8
Reliances and Limitations.....	8
Section 1: Introduction.....	10
Scope .....	10
Background.....	11
Mortgage Insurance Premiums .....	12
Down Payment and Closing Costs .....	14
Homebuyer Counseling .....	15
Automated Underwriting Systems .....	16
Adjustable Rate Mortgages .....	17
Foreclosure Avoidance and Loss Mitigation Programs .....	17
COVID-19 Pandemic .....	20
Current and Future Market Environment .....	21
Interest Rates .....	22
Home Price Index Growth .....	25
Unemployment Rate .....	27
Mortgage Volume.....	29
Report Structure.....	30
Section 2 - Summary of Findings and Comparison with Fiscal Year 2019 Actuarial Review .....	32
Economic Net Worth Estimate .....	32
Change in the Economic Net Worth.....	35
Sources of Change in the Cash Flow NPV from the Fiscal Year 2019 Review .....	35
Updated Economic Scenario Forecast.....	35
Updated Predictive Models.....	36

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page ii

- Actual Performance of Cohorts 2019 and Prior in Fiscal Year 2020..... 36
- Fiscal Year 2020 Origination Volume..... 36
- Section 3 - Cash Flow NPV Based on Alternative Scenarios ..... 37
  - Baseline Scenario..... 37
  - Alternative Scenario 0 – Upside (4<sup>th</sup> Percentile)..... 38
  - Alternative Scenario 1 – Upside (10<sup>th</sup> Percentile)..... 38
  - Alternative Scenario 2 – Downside (75<sup>th</sup> Percentile)..... 38
  - Alternative Scenario 3 – Downside (90<sup>th</sup> Percentile)..... 38
  - Alternative Scenario 4 – Downside (96<sup>th</sup> Percentile)..... 38
  - Slower Trend Growth ..... 39
  - Stagflation..... 39
  - Next-Cycle Recession..... 39
  - Low Oil Price ..... 39
  - Summary of Alternative Scenarios ..... 39
  - Stochastic Simulation ..... 40
  - Sensitivity Tests of Economic Variables..... 41
- Section 4 - Characteristics of the Fiscal Year 2020 Insurance Portfolio ..... 45
  - Volume and Share of Mortgage Originations..... 45
  - Originations by Location..... 47
  - Originations by Product..... 48
  - Initial Loan to Value Distributions ..... 49
  - Borrower Credit History Distribution ..... 51
  - Initial Relative Loan Size Distribution ..... 52
  - Initial Contract Interest Rate ..... 54
  - Source of Down Payment Assistance ..... 54
- Section 5 – Summary of Methodology ..... 56
  - Data Sources..... 56
  - Data Processing – Mortgage Level Modeling (Appendix A) ..... 56
  - Data Reconciliation..... 57

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page iii

Specification of Mortgage Transition Models (Appendix B) .....	61
Loss Severity Model (Appendix C) .....	63
Cash Flow Projections (Appendix E) .....	64
Appendices .....	66
Appendix A: Data – Sources, Processing and Reconciliation.....	67
Data Sources.....	67
Data Processing – Mortgage Level Modeling .....	67
Data Reconciliation.....	68
Appendix B – Transition Models.....	73
Section 1: Model Specification .....	73
Multinomial Logistic Regression Theory and Model Specification.....	77
Computation of Multinomial Logistic Probabilities from Binomial Models.....	78
Section 2: Transition Model Explanatory Variables.....	80
Section 3: Binomial Model Results .....	83
Current Transition Model Parameters – FRM30NSR C_SR.....	83
Current Transition Model Parameters – FRM30NSR C_PRE .....	88
Current Transition Model Parameters – FRM30NSR C_CXS.....	95
Current Transition Model Parameters – FRM30NSR C_D .....	99
Current Transition Model Parameters – FRM30SR C_CXS .....	105
Current Transition Model Parameters – FRM30SR C_D.....	110
Current Transition Model Parameters – FRM30SR C_END .....	116
Current Transition Model Parameters – FRM15 C_SR .....	120
Current Transition Model Parameters – FRM15 C_D.....	124
Current Transition Model Parameters – FRM15 C_CXS .....	126
Current Transition Model Parameters – FRM15 C_PRE .....	129
Current Transition Model Parameters – ARM C_SR.....	132
Current Transition Model Parameters – ARM C_CXS.....	138
Current Transition Model Parameters – ARM C_D .....	144
Current Transition Model Parameters – ARM C_PRE.....	153

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page iv

Default Transition Model Parameters – FRM30NSR D_CLM.....	160
Default Transition Model Parameters – FRM30NSR D_CXM .....	166
Default Transition Model Parameters – FRM30NSR D_CXS.....	170
Default Transition Model Parameters – FRM30NSR D_END.....	175
Default Transition Model Parameters – FRM30SR D_CLM .....	181
Default Transition Model Parameters – FRM30SR D_CXM.....	185
Default Transition Model Parameters – FRM30SR D_CXS .....	189
Default Transition Model Parameters – FRM30SR D_END .....	193
Default Transition Model Parameters – FRM15 D_CLM .....	196
Default Transition Model Parameters – FRM15 D_CXM.....	199
Default Transition Model Parameters – FRM15 D_CXS .....	202
Default Transition Model Parameters – FRM15 D_END .....	206
Default Transition Model Parameters – ARM D_CLM.....	209
Default Transition Model Parameters – ARM D_CXM .....	213
Default Transition Model Parameters – ARM D_CXS.....	217
Default Transition Model Parameters – ARM D_END .....	222
Section 3: Model Validation .....	226
Current FRM30NSR Transition Models.....	226
Current FRM30SR Transition Models .....	228
Current FRM15 Transition Models .....	230
Current ARM Transition Models.....	232
Default FRM30NSR Transition Models .....	234
Default FRM30SR Transition Models.....	236
Default FRM15 Transition Models.....	238
Default ARM Transition Models .....	240
Appendix C: Loss Severity Models.....	243
Model Specifications .....	243
Net Loss Severity Model Specification .....	245
Estimation Sample.....	247

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page v

Explanatory Variables .....	247
Model Parameters .....	248
Loss Mitigation Binomial Model .....	248
Loss Mitigation HAMP Severity Model .....	251
Third Party Sale Claims Logistic Model .....	253
Pre-Forclosure Sale Claims Logistic Model .....	255
Conveyance Severity Model .....	257
Conveyance Recovery Severity Model .....	261
Third Party Sales Severity Model .....	265
Pre-Forclosure Sale Severity Model .....	268
Model Validation .....	271
Loss Mitigation Model .....	272
Claim Type Model .....	272
Claim Type Severity Models .....	274
Appendix D: Economic Scenarios .....	277
Alternative Scenarios .....	277
Graphical Depiction of the Scenarios .....	277
Stochastic Simulation .....	280
Historical Data .....	280
Modeling Method .....	285
Data Transformation .....	287
Model Specifications .....	287
COVID-19 Pandemic Considerations .....	291
Simulation Generation .....	291
Interest Rate Simulations .....	291
House Price Appreciation Rate .....	293
Unemployment Rate .....	294
Gross Domestic Product .....	296
Small Business Normalized Optimism Index/ Consumer Confidence Index .....	296

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page vi

Appendix E: Cash Flow Analysis.....	298
Introduction.....	298
Cash Flow Components .....	298
MIP .....	299
Upfront MIP.....	301
Annual Premium.....	301
Refunded MIP.....	301
Losses Associated with Claims.....	302
Loss Mitigation Expenses.....	302
Net Present Value.....	303
Appendix F: Review of HUD Analysis of Economic Net Worth, Comparison of HUD and Pinnacle Models, and Assessment of Vulnerabilities .....	305
Forward Budget Model Commentary.....	305
Model Schema .....	305
Pinnacle Forward Budget Model Commentary.....	311
Model Schema .....	311
Simulation.....	312
Appendix G: Summary of Historical and Projected Claim Rates, Non-Claim Termination Rates and Loss Severities .....	313



## Summary of Findings

---

This report presents the results of Pinnacle Actuarial Resources, Inc.'s (Pinnacle's) independent actuarial review of the Economic Value associated with forward mortgages insured by the Mutual Mortgage Insurance Fund (MMI or Fund) for Fiscal Year 2020. The Economic Value associated with Home Equity Conversion Mortgages (HECMs) are analyzed separately and are excluded from this report. In the remainder of this report, the term MMI refers to forward mortgages and excludes HECMs.

Below we summarize the findings associated with each of the required deliverables.

**Deliverable 1: Produce a written Actuarial Study for Forward that provides actuarial central estimates of MMI Economic Net Worth as of the end of Fiscal Year 2020 and assesses HUD's estimates of Economic Net Worth.**

The Economic Net Worth is defined as cash available to the Fund plus the Net Present Value (NPV) of all future cash outflows and inflows that are expected to result from the mortgages currently insured by the MMI.

As of the end of Fiscal Year 2020, Pinnacle's Actuarial Central Estimate (ACE) of the MMI Forward Cash Flow NPV is \$23.397 billion.

The total capital resource as reported in the [Annual Report to Congress Regarding the Status of the FHA Mutual Mortgage Insurance Fund](#) is \$67.368 billion at the end of Fiscal Year 2020. Thus, the ACE of the Economic Net Worth of the MMI is \$90.765 billion.

**Deliverable 2: Include a review of the risk characteristics of existing MMI loans including commentary on how such characteristics have changed in recent years.**

A review of the risk characteristics of existing MMI loans, and a commentary on how these risk characteristics have changed is included in Section 4.

**Deliverable 3: Apply the final Forward actuarial model to the existing portfolio to produce conditional (and cumulative) claim, prepayment, and loss-given-default rates at various levels of aggregation across loans, and for individual policy years and policy year-quarter. Cash-flow summaries should also be provided for major categories (e.g., premium revenues, claim expenses and recoveries or net loss due to claim, with affected loan counts and balances).**

Appendix G shows the interim and final claim rates, non-claim termination rates and loss severities by cohort. Each of these elements is calculated for each year of developed experience, and final projections are also included. Cash flow summaries by major category and credit subsidy cohort are shown below and discussed in more detail in Sections 2 and 3.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 2

Table 1: Projected Cash Flow Summaries

Cash Flow Category	Net Present Value of Cash Flow
Mortgage Insurance Premium	55,147,709,341
Loss Incurred	23,961,917,445
Loss Mitigation Expense	869,291,003
HAMP Expense	20,106,614,457
HAMP Recovery	13,186,796,336

**Deliverable 4: To promote transparency of the Studies’ assessments, the Studies should identify methodological vulnerabilities that may occur in its actuarial models or in HUD’s analyses of Economic Net Worth. This discussion should evaluate the scope and scale of such vulnerabilities in creating possible forecast risk and suggest possible lines of research in these areas. The Studies should assess and comment upon HUD’s own models that estimate Economic Net Worth for methodological vulnerabilities and compare HUD’s methodologies with those in the Studies.**

The assumptions and judgments on which the Cash Flow NPV estimates are based are summarized in Section 5 of this report. Appendix B shows the specifications and assumptions related to the transition models. Appendix C details the loss severity models. Section 3 describes the economic assumptions incorporated into the Cash Flow NPV estimates and the sensitivity of the estimates to alternative economic scenarios. Lastly, Section 5 and Appendix E summarize the assumptions associated with the cash flow analysis.

Section 3 provides a discussion of the economic conditions that could result in material adverse change to the Cash Flow NPV.

Appendix F provides a discussion of the HUD methodologies for estimating Economic Net Worth, a comparison of HUD modeling methodology to those used in this study, and methodological vulnerabilities of the HUD models.

**Deliverable 5: The Studies should include historical data on changes in program terms as well as relevant loan and borrower characteristics (e.g., credit scores, loan-to-value ratios) by cohort and other sub-populations. Loan performance data (claim rates, prepayment rates, severity and recovery rates) both historical and projected should be presented in the “finger-table” formats (arrayed by cohort and policy years for different loan products).**

A review of the risk characteristics of existing MMI loans, and a commentary of how these risk characteristics have changed is included in Section 4. Appendix G shows the interim and final claim rates, non-claim termination rates and loss severities by cohort. Each of these elements is calculated for each year of developed experience, and final projections are also included.

**Deliverable 6: The Contractor should use the President’s Economic Assumptions (provided by ORMRA) for the actuarial central estimates of the Studies. However, in addition to the central single path economic forecast,**

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 3

**the Studies should test alternative economic forecasts for stress-testing and sensitivity analysis to estimate ranges of reasonableness.**

Pinnacle’s ACE of Cash Flow NPV is based on the Economic Assumption for the 2021 Budget from the Office of Management and Budget (OMB Economic Assumptions). Pinnacle also estimated Cash Flow NPV outcomes based on economic scenarios from Moody’s Analytics (Moody’s). The Cash Flow NPV results based on these scenarios are shown in Table 2.

*Table 2: Range of Cash Flow NPV Outcomes Based on OMB & Moody’s Scenarios*

<b>Economic Scenario</b>	<b>Fiscal Year 2020 Cash Flow NPV</b>
Pinnacle ACE	23,396,682,771
Baseline	5,109,328,875
Alternative 0 – Upside (4th Percentile)	19,905,923,534
Alternative 1 – Upside (10th Percentile)	12,935,115,293
Alternative 2 – Downside (75th Percentil	(369,228,238)
Alternative 3 – Downside (90th Percentil	(8,607,939,515)
Alternative 4 – Downside (96th Percentil	(18,993,162,441)
Slower-Trend Growth	(1,564,277,946)
Stagflation	(1,263,561,223)
Next-Cycle Recession	965,577,777
Low Oil Price	2,470,564,208

The range of results based on the Moody’s estimates is negative \$18.993 billion to positive \$19.906 billion.

In addition, Pinnacle has estimated a range of outcomes based on 100 randomly generated stochastic simulations of key economic variables. Based on these simulations, the range of Cash Flow NPV estimates is negative \$21.162 billion to positive \$26.989 billion.

The Cash Flow NPV estimate provided by the Federal Housing Administration (FHA) to be used in the FHA’s Annual Report to Congress is positive \$10.4 billion. Based on Pinnacle’s Actuarial Central Estimate and range of reasonable estimates, we conclude that the FHA estimate of Cash Flow NPV to be used in the FHA’s Annual Report to Congress is reasonable.

Pinnacle’s Cash Flow NPV by cohort is shown below for the largest negative outcome and the largest positive outcome based on the stochastic simulation results.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 4

Table 3: Range of Cash Flow NPV Estimates - Forward Portfolio

Cohort	Largest Negative	Largest Positive	Pinnacle ACE
1992	-582,799	-499,011	-348,460
1993	-1,732,222	-2,025,224	-1,160,429
1994	-2,803,568	-2,868,117	-1,915,290
1995	-3,336,264	-1,550,995	-1,435,867
1996	-7,546,770	-3,901,140	-3,362,930
1997	-11,621,631	-5,949,803	-6,759,911
1998	-24,000,445	-13,200,889	-10,775,983
1999	-36,526,680	-13,851,925	-14,869,717
2000	-28,565,433	-10,771,444	-13,245,634
2001	-78,849,753	-50,858,671	-46,115,845
2002	-119,825,815	-67,799,028	-69,343,144
2003	-184,894,858	-110,274,953	-106,768,867
2004	-282,073,988	-149,998,354	-163,750,202
2005	-278,974,908	-178,908,301	-156,305,021
2006	-320,695,118	-189,452,807	-173,081,954
2007	-441,340,874	-279,523,086	-255,907,972
2008	-1,182,233,082	-670,053,225	-669,157,326
2009	-1,559,866,282	-872,430,805	-918,788,943
2010	-1,384,465,022	-737,323,753	-776,487,875
2011	-930,707,047	-451,196,593	-503,559,927
2012	-1,204,986,075	-428,503,213	-447,634,443
2013	-1,857,645,251	-322,744,020	-387,410,293
2014	393,118,924	1,870,461,330	1,831,341,873
2015	-89,708,553	3,276,025,896	3,463,919,332
2016	-1,087,884,321	4,350,067,169	4,365,037,310
2017	-2,492,623,609	4,681,571,413	4,000,572,745
2018	-3,842,675,881	2,561,169,930	1,533,469,469
2019	-4,064,463,252	2,624,591,563	2,041,597,422
2020	-34,268,421	12,189,020,226	10,888,930,652
Total	-21,161,778,996	26,989,222,172	23,396,682,771

**Deliverable 7: To provide comparability to HUD estimates of Economic Net Worth, the Contractor shall use Federal Credit Reform Act discounting assumptions and procedures.**

Pinnacle has developed estimates of Economic Net Worth using the Federal Credit Reform Act discounting assumptions.

**Deliverable 8: These Studies should use stochastic or Monte Carlo simulations of future economic conditions including for interest rates and house price appreciation. The objective of these requirements is to illustrate the sensitivity of forecasts to economic uncertainty and other forms of forecast error.**

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 5

As described in the results for Deliverable 6, additional economic assumptions were generated using Monte Carlo simulations and Moody's economic scenarios. These results are discussed in further detail in Section 3.

**Deliverable 9: Provide econometric appendices to the Studies that include variable specifications and statistical output from all regressions in the Studies. Individual estimation equations may not be combined for reporting.**

Appendix B shows the predictive model parameters and goodness of fit measures for the Transition models. Appendix C shows the parameters and goodness of fit measures for the Loss Severity models. See the [Binomial Model Results](#) and [Model Validation](#) sections in Appendix B and the [Model Parameters](#) and [Model Validation](#) sections in Appendix C.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 6

## Executive Summary

---

The 1990 Cranston-Gonzalez National Affordable Housing Act (NAHA) requires an independent actuarial analysis of the economic value of the FHA and Department of Housing and Urban Development's (HUD's) MMI. Enacted on July 30, 2008, the Housing and Economic Recovery Act of 2008 (HERA) moved the requirement for an independent actuarial review into 12 USC 1708(a)-(4).

HERA also moved several additional programs into the MMI. One of them, HECMs, which are reverse mortgages, is analyzed separately and is excluded from this report. In the remainder of this report, the term MMI refers to forward mortgages and excludes HECMs.

The primary purpose of this actuarial analysis is to estimate the Economic Net Worth of the current book of business. The Economic Net Worth is defined as cash available to the Fund plus the NPV of all future cash outflows and inflows that are expected to result from the mortgages currently insured by the MMI.

We have calculated a range of estimates using economic projections from the OMB Economic Assumptions for Fiscal Year 2020, ten economic projection scenarios from Moody's and a stochastic simulation approach to test variation from the base economic scenario.

Based on our analysis, we estimate that the Cash Flow NPV as of the end of Fiscal Year 2020 is \$23.397 billion. We also estimate that the range of Cash Flow NPV based on randomly generated economic scenarios is between negative \$21.162 billion and positive \$26.989 billion.

The total capital resource as reported in the [Annual Report to Congress Regarding the Status of the FHA Mutual Mortgage Insurance Fund](#) is \$67.368 billion at the end of Fiscal Year 2020. Thus, the estimated Economic Net Worth of the MMI is \$90.765 billion.

### Impact of Economic Forecasts

The Cash Flow NPV of the MMI depends on many factors. One of the most important set of factors is the prevailing economic conditions over the next 30 years, and most critically during the next 10 years. We incorporate the most significant factors in the U.S. economy affecting the performance of the mortgages insured by the MMI through the use of the following variables in our models:

- 30-year fixed-rate home mortgage effective rates
- 10-year Constant Maturity Treasury (CMT) rates
- Three-year CMT rates
- One-year CMT rates
- Housing price index (HPI)
- Unemployment rates

The projected Cash Flow NPV of FHA's books of business is affected by changes in these economic variables. The ACE in this report is derived from using the required OMB Economic Assumptions.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 7

We have also estimated the Cash Flow NPV of the MMI under ten economic scenarios from Moody's. These scenarios are:

1. Baseline
2. Alternative 0 – Upside (4th Percentile)
3. Alternative 1 – Upside (10th Percentile)
4. Alternative 2 – Downside (75th Percentile)
5. Alternative 3 – Downside (90th Percentile)
6. Alternative 4 – Downside (96th Percentile)
7. Slower Trend Growth
8. Stagflation
9. Next-Cycle Recession
10. Low Oil Price

These scenarios do not represent the full range of possible future economic paths, but represent a considerable variation of economic conditions. Therefore, they provide insights into the projected Cash Flow NPV of the MMI under a range of economic environments.

The summary of the estimated Cash Flow NPV resulting from each scenario is shown in Table 4.

*Table 4: Projected Forward Cash Flow NPV Using Alternative Economic Scenarios*

<b>Economic Scenario</b>	<b>Fiscal Year 2020 Cash Flow NPV</b>
Pinnacle ACE	23,396,682,771
Baseline	5,109,328,875
Alternative 0 – Upside (4th Percentile)	19,905,923,534
Alternative 1 – Upside (10th Percentile)	12,935,115,293
Alternative 2 – Downside (75th Percentile)	(369,228,238)
Alternative 3 – Downside (90th Percentile)	(8,607,939,515)
Alternative 4 – Downside (96th Percentile)	(18,993,162,441)
Slower-Trend Growth	(1,564,277,946)
Stagflation	(1,263,561,223)
Next-Cycle Recession	965,577,777
Low Oil Price	2,470,564,208

We also randomly generated 100 stochastic simulations of key economic variables. Based on these simulations, the range of Cash Flow NPV estimates is negative \$21.162 billion to positive \$26.989 billion.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 8

## Distribution and Use

---

This report is being provided to FHA for its use and the use of makers of public policy in evaluating the Economic Net Worth of the MMI. Permission is hereby granted for its distribution on the condition that the entire report, including the exhibits and appendices, is distributed rather than any excerpt. Pinnacle also acknowledges that this report will be included in the FHA's Annual Report to Congress, and permission is granted for this purpose as well. We are available to answer any questions that may arise regarding this report.

Any third parties receiving the report should recognize that the furnishing of this report is not a substitute for their own due diligence and should place no reliance on this report or the data contained herein that would result in the creation of any duty or liability by Pinnacle to the third party.

Our conclusions are predicated on a number of assumptions as to future conditions and events. These assumptions, which are documented in subsequent sections of the report, must be understood in order to place our conclusions in their appropriate context. In addition, our work is subject to inherent limitations, which are also discussed in this report.

## Reliances and Limitations

---

Listed in Section 5 are the data sources Pinnacle has relied upon in our analysis. We have relied on the accuracy of these data sources in our calculations. If it is subsequently discovered that the underlying data or information is erroneous, then our calculations would need to be revised accordingly.

We have relied on a significant amount of data and information from external sources without audit or verification. This includes economic data projected over the next 30 years from Moody's and OMB. However, we did review as many elements of the data and information as practical for reasonableness and consistency with our knowledge of the mortgage insurance industry. It is possible that the historical data used to develop our estimates may not be predictive of future default and claim experience. We have not anticipated any extraordinary changes to the legal, social or economic environment which might affect the number or cost of mortgage defaults beyond those contemplated in the economic scenarios described in this report. To the extent that the realized economic conditions deviate significantly from these assumptions, the Economic Net Worth projections may differ, perhaps significantly, from actual results.

A substantial source of uncertainty relates to the emergence of the COVID-19 pandemic in 2020. This uncertainty could impact the projection of Cash Flow NPV in several different ways including distortion of historical patterns as the MMI handles claims differently and sudden changes in loan origination exposure as the peril continues to emerge. Some of these uncertainties may affect the settlement of claims that began prior to COVID-19 being declared a pandemic. At this point, it is not possible to reliably forecast these impacts. The COVID-19 pandemic may have a material impact on our Cash Flow NPV estimates as its effects emerge.

The predictive models used in this analysis are based on a theoretical framework and certain assumptions. This model structure predicts the rates of default, claim, loss and prepayment based on a number of individual



## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 9

mortgage characteristics and economic variables. The models are built using predictive modeling techniques, analyzing data from actual historical experience of FHA-insured mortgages. The parameters of the predictive models are estimated over a wide variety of mortgages originated since 1975 and their performance under the range of economic conditions and mortgage market environments experienced during the past 44 years. The predictive models are combined with assumptions about future behavior of current mortgage endorsements and certain key economic assumptions to produce future projections of the performance of the existing mortgages insured by the MMI.

Pinnacle is not qualified to provide formal legal interpretation of federal legislation or FHA policies and procedures. The elements of this report that require legal interpretation should be recognized as reasonable interpretations of the available statutes, regulations and administrative rules.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 10

## Section 1: Introduction

---

### Scope

HUD and FHA have engaged Pinnacle to perform the annual independent Actuarial Review of the MMI. This study is required by 12 USC 1708(a)-(4) and must be completed in compliance with the Federal Credit Reform Act as implemented and all applicable Actuarial Standards of Practice (ASOPs). This study provides an analysis of the financial position of MMI as of September 30, 2020 using data through September 30, 2020.

The MMI is a group of accounts of the federal government which records transactions associated with the FHA's guarantee programs for single family mortgages. Currently, the FHA insures approximately 7.91 million forward mortgages under the MMI and 434,938 reverse mortgages under the HECM program.

Per 12 USC 1711-(f), FHA must endeavor to ensure that the MMI maintains a capital ratio of not less than 2.0%. The capital ratio is defined as the ratio of capital to the MMI obligations on outstanding mortgages (IIF). Capital is defined as cash available to the Fund plus the Net Present Value (NPV) of all future cash outflows and inflows that are expected to result from the mortgages currently insured by the MMI.

The deliverables included in this study, as defined by the Statement of Work, are as follows:

1. Produce a written Actuarial Study for Forward that provides the actuarial central estimate of MMI Economic Net Worth as of the end of the subject Fiscal Year and assesses HUD's estimates of Economic Net Worth.
2. Include a review of the risk characteristics of existing MMI loans including commentary on how such characteristics have changed in recent years.
3. Apply the final Forward actuarial models to the existing portfolio to produce conditional (and cumulative) claim, prepayment, and loss-given-default rates at various levels of aggregation across loans, and for individual policy years and policy year-quarter. Cash-flow summaries shall also be provided for major categories (e.g., premium revenues, claim expenses and recoveries or net loss due to claim, with affected loan counts and balances).
4. To promote transparency of the Study's assessments, the Study shall identify methodological vulnerabilities that may occur in its actuarial models or in HUD's analyses of Economic Net Worth. This discussion shall evaluate the scope and scale of such vulnerabilities in creating possible forecast risk and suggest possible lines of research in these areas. The Study shall assess and comment upon HUD's own models that estimate Economic Net Worth for methodological vulnerabilities and compare HUD's methodologies with those in the Study.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 11

5. The Study shall include historical data on changes in program terms as well as relevant loan and borrower characteristics (e.g., credit scores, loan-to-value ratios) by cohort and other sub-populations. Loan performance data (claim rates, prepayment rates, severity and recovery rates), both historical and projected, shall be presented in the “finger-table” formats (arrayed by cohort and policy years for different loan products).
6. The Contractor shall use the President’s Economic Assumptions (PEA), provided by Office of Risk Management and Regulatory Affairs (ORMRA) for the Actuarial Central Estimates (ACE) of the Study. However, in addition to the central single path economic forecast, the Study shall test alternative economic forecasts for stress-testing and sensitivity analysis to estimate ranges of reasonableness.
7. To provide comparability to HUD estimates of Economic Net Worth, the Contractor shall use Federal Credit Reform Act discounting assumptions and procedures.
8. This Study shall use stochastic or Monte Carlo simulations of future economic conditions, including for interest rates and house price appreciation. The objective of these requirements is to illustrate the sensitivity of forecasts to economic uncertainty and other forms of forecast error.
9. Provide econometric appendices to the Study that include variable specifications and statistical output from all regressions in the Study. Individual estimation equations shall not be combined for reporting.

### Background

HUD was established in 1937 by the U.S. Housing Act of 1937. The current mission of HUD is:

*...to create strong, sustainable, inclusive communities and quality affordable homes for all. HUD is working to strengthen the housing market to bolster the economy and protect consumers; meet the need for quality affordable rental homes; utilize housing as a platform for improving quality of life; build inclusive and sustainable communities free from discrimination, and transform the way HUD does business.<sup>1</sup>*

Congress created FHA in 1934. The FHA “provides mortgage insurance on loans made by FHA-approved lenders throughout the United States and its territories. FHA insures mortgages on single family and multifamily homes, including manufactured homes and hospitals. It is the largest insurer of mortgages in the world, insuring over 34 million properties since its inception in 1934.”<sup>2</sup> The mortgage insurance provided was done so through the establishment of the MMI.

The National Affordable Housing Act (NAHA), enacted in 1990, introduced a minimum capital requirement for the MMI<sup>3</sup>. By 1992, the capital ratio was to be at least 1.25%, and by 2000 the capital ratio was to be no less

---

<sup>1</sup> <https://portal.hud.gov/hudportal/HUD?src=/about/mission>

<sup>2</sup> [https://portal.hud.gov/hudportal/HUD?src=/program\\_offices/housing/fhahistory](https://portal.hud.gov/hudportal/HUD?src=/program_offices/housing/fhahistory)

<sup>3</sup> Public Law 101-625, 101<sup>st</sup> Congress, November 28, 1990, Section 332.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 12

than 2.0%. The capital ratio is defined by NAHA as the ratio of capital to unamortized IIF. NAHA also implemented the requirement that an independent actuarial study of the MMI be completed annually. The Housing and Economic Recovery Act (HERA) amended 12 USC 1708(a)-(4) to include the requirement for the annual Actuarial Study.

Given the purpose of HUD and FHA, availability of mortgages to a broad segment of the home-buying market is important to promote and strengthen the U.S. housing market. However, the capital requirements established by NAHA can potentially be in conflict with the desire for widespread availability of mortgage insurance. Since the implementation of NAHA, many of the steps taken by HUD have attempted to balance broader availability of mortgage insurance and the financial stability of the MMI.

### Mortgage Insurance Premiums

Adequate mortgage insurance premium (MIP) is key in maintaining the economic strength of the MMI, but the level of MIP can also impact the ability of potential home buyers to afford a home. A summary of the adjustments in MIP since 1991 is shown below:

- In 1991, it was established that MIP would be determined as the combination of an upfront MIP and a yearly premium which was a percentage of the remaining outstanding mortgage balance each year.<sup>4</sup> Overall, this represented an increase in MIP, which was needed to help meet the new capital requirement established by NAHA.
- In 1994, the upfront MIP was decreased by 75 basis points to 2.25%.<sup>5</sup> This was in response to improved financial experience of the MMI.
- In 1996, the upfront MIP was decreased by 25 basis points to 2.00% for first-time homebuyers that received mortgage counseling prior to purchasing their home.<sup>6</sup> This was implemented based on the success of a pilot program which showed that first-time homebuyers who received this counseling had better default experience.
- In 1997, the upfront MIP was decreased by an additional 25 basis points to 1.75% for first-time homebuyers that received mortgage counseling prior to purchasing their home. In total, the upfront MIP was 50 basis points lower than it would be for a homebuyer who did not receive counseling.<sup>7</sup>

---

<sup>4</sup> Mortgagee Letter 91-26, May 30, 1991: Single Family Insurance Processing for Risk Based Insurance Premiums.

<sup>5</sup> Mortgagee Letter 94-14, March 31, 1994: Single Family Loan Production – Reduced Upfront Mortgage Insurance Premium (UFMIP).

<sup>6</sup> Mortgagee Letter 96-48, August 28, 1996: Single Family Production – Reduction in Up-Front Mortgage Insurance Premiums (UFMIP) for First-Time Homebuyers Who Receive Housing Counseling.

<sup>7</sup> Mortgagee Letter 97-37, August 13, 1997: Single Family Production – Further Reduction in Up-Front Mortgage Insurance Premiums (UFMIP) for First-Time Homebuyers Who Receive Housing Counseling.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 13

- In 2000, in recognition of the improved experience of the MMI, several changes were implemented. First, the upfront MIP was reduced by 75 basis points to 1.50%. Second, the upfront MIP refund schedule was shortened to five years instead of seven years. Third, a provision to cancel the annual MIP once the loan-to-value (LTV) ratio was 78% or less was implemented. Also, the discount in the upfront MIP for first-time homebuyers that received counseling was discontinued.<sup>8</sup>
- In April of 2010, upfront MIP was increased by 75 basis points to 2.25%.<sup>9</sup> This increase in premium was in response to the housing and economic crisis of 2008, and was the first in a series of increases over the next three years.
- In October of 2010, upfront MIP was decreased but annual MIP was increased significantly.<sup>10</sup> Overall, this resulted in an increase in MIP.
- In 2011, the annual MIP was increased by 25 basis points.<sup>11</sup>
- In 2012, the annual MIP was increased by 10 basis points.<sup>12</sup>
- In 2013, several changes were implemented related to annual MIP. First, the term for collection of MIP was extended to 11 years for mortgages with an initial LTV ratio of 90% or less, and for 30 years for mortgages with an initial LTV ratio of greater than 90%. Second, mortgages with terms of 15 years or less and LTV ratio of 78% or less at the time of origination, which were exempt from MIP, would no longer be exempt. Lastly, the annual MIP was increased by 5 to 10 basis points for mortgages with terms of 15 years or less and LTV ratios of 78% or less at origination.<sup>13</sup>
- As a result of improved financial experience, in 2015 annual MIP rates were decreased by 50 basis points for loans with terms greater than 15 years.<sup>14</sup>

---

<sup>8</sup> Mortgagee Letter 2000-38, October 27, 2000: Single Family Loan Production – Further Reduction in Upfront Mortgage Insurance Premiums and Other Mortgage Insurance Premium Changes.

<sup>9</sup> Mortgagee Letter 2010-02, January 21, 2010: Increase in Upfront Premiums for FHA Mortgage Insurance.

<sup>10</sup> Mortgagee Letter 2010-28, September 1, 2010: Changes to FHA Mortgage Insurance Premiums.

<sup>11</sup> Mortgagee Letter 2011-10, February 14, 2011: Annual Mortgage Insurance Premium Changes and Guidance on Case Numbers.

<sup>12</sup> Mortgagee Letter 2012-04, March 6, 2012: Single Family Mortgage Insurance: Annual and Up-Front Mortgage Insurance Premium – Changes.

<sup>13</sup> Mortgagee Letter 2013-04, January 31, 2013: Revision of Federal Housing Administration (FHA) policies concerning cancellation of the annual Mortgage Insurance Premium (MIP) and increase to the annual MIP.

<sup>14</sup> Mortgagee Letter 2015-01, January 9, 2015: Reduction of Federal Housing Administration (FHA) annual Mortgage Insurance Premium (MIP) rates and Temporary Case Cancellation Authority.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 14

- In 2017, a decrease was proposed for annual MIP rates,<sup>15</sup> but this decrease was suspended later in the year.<sup>16</sup>

### Down Payment and Closing Costs

The source of funds for down payment and closing costs has been a significant issue for HUD. There are limitations on closing costs and down payment assistance that can be provided by sources other than the borrower or family, and there have been several mortgagee letters addressing this issue. Allowing assistance with down payments and closing costs increases the opportunity for more people to achieve homeownership. Historically, however, mortgages for which a larger percentage of the down payment and closing costs were provided by sources other than the borrowers own funds have demonstrated poorer performance. A summary of mortgagee letters addressing this is provided below:

- Prior to 1992, closing costs could not be financed in the loan. In 1992, the limitation on financing of closing costs was removed, but mortgages were still subject to LTV ratio limits.<sup>17</sup> This provision was implemented to make it easier for homebuyers to meet the down payment requirements.
- In 1996, HUD allowed family members to lend the borrower 100% of the down payment.<sup>18</sup> This also was intended to make it easier for borrowers to achieve homeownership.
- Two provisions were implemented in 1998. First, it was prohibited for the seller or any other party to pay mortgage interest for the buyer. In addition, any interest rate buydown could not result in a reduction in the interest rate of more than 2% below the note rate. These changes were implemented to avoid a significant increase in the payment amount once the seller-paid mortgage interest funds were depleted or the interest rate buydown term was complete.<sup>19</sup>
- In 2000, guidance was provided by HUD to mortgagees to ensure that the source of the gifts to buyers is documented, and the person giving the gift must certify that the funds did not come from someone with an interest in the transaction. This was implemented to combat a practice of the sellers providing funds to family members of the buyer that would then be used for the down payment.<sup>20</sup>

---

<sup>15</sup> Mortgagee Letter 2017-01, January 9, 2017: Reduction of Federal Housing Administration (FHA) Annual Mortgage Insurance Premium (MIP) Rates.

<sup>16</sup> Mortgagee Letter 2017-07, January 20, 2017: Suspension of Mortgagee Letter 2017-01 – Reduction of Federal Housing Administration (FHA) Annual Mortgage Insurance Premium (MIP) Rates.

<sup>17</sup> Mortgagee Letter 92-39, October 16, 1992: Single Family Loan Production - Elimination of Limit on Financing Closing Costs.

<sup>18</sup> Mortgagee Letter 96-58, October 23, 1996: Single Family Loan Production - Secondary Financing from Family Members.

<sup>19</sup> Mortgagee Letter 98-1, January 2, 1998: Single Family Loan Production - Underwriting Adjustable Rate Mortgages, Interest Buydowns, Homeownership Counseling and Other Credit Policy Issues

<sup>20</sup> Mortgagee Letter 2000-28, August 7, 2000: Gift Documentation, Mortgage Forms and other Credit Policy and Appraisal Issues.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 15

- In 2001, HUD withdrew its proposed rule on Sources of Homeowner Downpayment that would have prohibited gifts from non-profit organizations being used for the mortgagor's investment in a mortgaged property if the organization received the funds for the gift either directly or indirectly from the seller.
- Section 2113 of the Housing And Economic Recovery Act Of 2008 prohibited downpayment contributions from a seller or any other person or entity that would financially benefit from the transaction.
- In 2019, guidance by HUD was provided to clarify the rules associated with funds being provided by a governmental source for down payment assistance. The mortgagee letter requires the mortgagee to verify that the funds provided by the government agency were transferred to the Borrower before or at the time of closing, and that the governmental agency was acting in its legal capacity in providing these funds. Documentation is also required from the government that the agency has the authority to provide the funds, and from an attorney for the government entity verifying that the property is within the government agency's jurisdiction. There can be no direct transfer of assistance from the government agency to the mortgagee, and there can be no requirement that the loan be transferred to a specific mortgagee as a condition of receiving assistance from the government agency.<sup>21</sup>

This guidance was subsequently suspended until further notice<sup>22</sup> and ultimately rescinded.<sup>23</sup>

### Homebuyer Counseling

Counseling for homebuyers was encouraged historically by FHA with the idea that if homebuyers were educated on issues of homeownership and mortgages, they would be less likely to default on the mortgage and would be more responsible homeowners. The history of mortgagee letters related to homebuyer counseling is outlined below:

- In 1993, a pilot of a counseling program for pre-purchase and pre-foreclosure situations was announced.<sup>24</sup>
- In 1996, after the pilot of the counseling program, the upfront MIP was decreased by 25 basis points for first-time homebuyers who complete homeownership counseling.<sup>25</sup> Just one year later in 1997, the

---

<sup>21</sup> Mortgagee Letter 19-06, April 18, 2019: Downpayment Assistance and Operating in a Governmental Capacity.

<sup>22</sup> Mortgagee Letter 19-10, July 23, 2019: Suspension of the Effective Date of Mortgagee Letter 2019-06, *Downpayment Assistance and Operating in a Governmental Capacity*.

<sup>23</sup> Mortgagee Letter 19-12, August 13, 2019: Rescission of Mortgagee Letters 2019-06, *Downpayment Assistance and Operating in a Governmental Capacity*; 2019-07, *Extension of the Effective Date of Mortgagee Letter 2019-06, Downpayment Assistance and Operating in a Governmental Capacity*; and 2019-10, *Suspension of the Effective Date of Mortgagee Letter 2019-06, Downpayment Assistance and Operating in a Governmental Capacity*.

<sup>24</sup> Mortgagee Letter 93-28, September 20, 1993: Prepurchase and Foreclosure Prevention Counseling Demonstration.

<sup>25</sup> Mortgagee Letter 96-48, August 28, 1996: Single Family Production - Reduction in Up-Front Mortgage Insurance

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 16

upfront MIP was decreased by an additional 25 basis points for first-time homebuyers who complete homeownership counseling.<sup>26</sup> This discount was provided to recognize expected improvement in default experience.

- In 1998, a mortgagee letter was released indicating that the homeownership counseling program would be reviewed. This was in response to homeownership counseling programs that were being used that did not meet FHA guidelines. While the requirements of the counseling program were that it should involve 15 to 20 hours of instruction, there were cases where homebuyers were being provided with workbooks without additional interaction or instruction. The guidelines of the homeownership counseling program were reiterated in this letter.<sup>27</sup>
- In 2000, in conjunction with an overall reduction in upfront MIP, the homeownership counseling discount was discontinued.<sup>28</sup>

### Automated Underwriting Systems

Beginning in 1995, the use of automated underwriting systems (AUSs) began to increase. Theoretically, the use of AUSs increases the availability of mortgages, and improves the efficiency and speed of mortgage processing:

- In 1995, HUD approved usage of AUSs. Mortgagees had to request permission to use these systems and receive approval from HUD.<sup>29</sup>
- In 1996, criteria were established for the approval by HUD of AUSs.<sup>30</sup>

In 1998, FHA approved Freddie Mac's Loan Prospector for underwriting FHA-insured mortgages, using a scorecard custom-estimated for FHA endorsed loans. FHA also made a substantial number of revisions to its credit policies and reduced documentation requirements for loans assessed by Loan Prospector. This was the first time that FHA incorporated an AUS in its insurance endorsement process. Fannie Mae's Desktop Underwriter and PMI Mortgage Services' Automated Underwriting Risk Analysis (AURA) were approved to underwrite FHA mortgages in 1999, followed soon thereafter by Countrywide Funding Corporation's Countrywide Loan-Underwriting Expert System (CLUES) and JP Morgan-Chase's Zippy. Beginning in May 2004, all approved AUSs applied FHA's Technology-Open-To-Approved-Lenders (TOTAL) mortgage scorecard to evaluate

---

Premiums (UFMIP) for First-Time Homebuyers Who Receive Housing Counseling.

<sup>26</sup> Mortgagee Letter 97-37, August 13, 1997: Single Family Production - Further Reduction in Up-Front Mortgage Insurance Premiums (UFMIP) for First-Time Homebuyers Who Receive Housing Counseling.

<sup>27</sup> Mortgagee Letter 98-1, January 2, 1998: Single Family Loan Production - Underwriting Adjustable Rate Mortgages, Interest Buydowns, Homeownership Counseling and Other Credit Policy Issues.

<sup>28</sup> Mortgagee Letter 2000-38, October 27, 2000: Single Family Loan Production - Further Reduction in Upfront Mortgage Insurance Premiums and Other Mortgage Insurance Premium Changes

<sup>29</sup> Mortgagee Letter 95-7, January 27, 1995: Single Family Loan Production - Revised Underwriting Guidelines and Other Policy Issues.

<sup>30</sup> Mortgagee Letter 96-34, July 10, 1996: Single Family Loan Production - Automated Underwriting Systems.



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 17

loan applications for possible automated approval for FHA insurance. Initially, more than two-thirds of loans submitted generally received automated approval, eliminating the need for manual underwriting reviews. Since May 2004, HUD required lenders to submit borrower credit scores. Starting in July 2008, all loans were to be submitted through FHA's TOTAL scorecard. Additional guidance issued in February 2011 prohibited the use of the TOTAL scorecard on streamline refinance transactions.

### Adjustable Rate Mortgages

Adjustable rate mortgages (ARMs) are mortgages where the interest rate adjusts over the life of the loan. The interest rate adjustments are tied to interest rate indexes, such as Constant Maturity Treasury (CMT) rates. The interest rate at the beginning of the loan is typically lower than the prevailing fixed rate mortgage, and increases over the early years of the loan. The initial interest rate can be fixed for a varying period of time (one year, three years, five years, etc.) and, after the fixed interest rate period, can change yearly. Most ARMs also have a lifetime cap on how much the interest rate can increase relative to the initial interest rate.

Historically, the default rates related to ARM's have been higher than the default rates for fixed rate mortgages. This is based in part on the fact that as the interest rate increases, the monthly mortgage payment increases, and, as a result, the likelihood of borrower defaults increases. However, there is an offsetting impact, as the likelihood of prepayments decrease as interest rates increase. To address this, HUD has issued a series of mortgagee letters related to ARMs:

- In 1998, HUD issued guidance that for ARMs, borrowers must qualify using mortgage payments based on the contract or initial rate plus one percent, which effectively represents the second year interest rate. This applied to all mortgages with LTV ratios of greater than or equal to 95%. In addition, it prohibited any form of a temporary interest rate buydown. This was due to the fact that the payment shock associated with the termination of the buydown was causing default rates to increase to an unacceptable level.<sup>31</sup>
- In 2004, HUD expanded mortgage insurance availability to cover three-, five-, seven- and 10-year ARMs.<sup>32</sup>
- In 2007, the one-year London Interbank Offered Rate (LIBOR) was added as an acceptable index for ARMs.<sup>33</sup>

### Foreclosure Avoidance and Loss Mitigation Programs

The pre-foreclosure sale (PFS) program allows mortgagors to sell their homes and use the proceeds to satisfy their mortgage debt obligations even if the proceeds were less than owed. Ultimately, these programs help limit

---

<sup>31</sup> Mortgagee Letter 98-1, January 2, 1998: Single Family Loan Production - Underwriting Adjustable Rate Mortgages, Interest Buydowns, Homeownership Counseling and Other Credit Policy Issues.

<sup>32</sup> Mortgagee Letter 2004-10, March 19, 2004: Adjustable Rate Mortgages.

<sup>33</sup> Mortgagee Letter 2007-13, October 12, 2007: Adjustable Rate Mortgages—Addition of LIBOR Index.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 18

the number of defaults that turn into claims, and also limit the losses sustained by MMI when a claim occurs. Over the years, FHA has issued a number of mortgagee letters related to foreclosure and loss mitigation:

- In 1996, a mortgagee letter was released to provide information on the loss mitigation procedures, including special forbearance plans, mortgage modifications, PFSs, deeds in lieu of foreclosure and partial claims. The primary objective was to keep the homeowner in the home, and if that was not possible then the objective was disposition of the property without full foreclosure.<sup>34</sup>
- In 2008, due to the increase in defaults resulting from the housing crisis, FHA released a mortgagee letter reminding mortgagees of PFS as an option and also consolidated the provisions of the PFS program into one place. This letter also updated provisions of the PFS to better address the mortgage crisis.<sup>35</sup>
- In 2010, FHA released a mortgagee letter announcing enhancements to the FHA refinance program to allow responsible borrowers an opportunity to stay in their homes. This could occur if the lender agreed to write off at least 10% of the principal balance and if the remaining loan provisions were met.<sup>36</sup>
- In 2011, FHA issued guidance requiring a trial payment program prior to completing a permanent loan modification or partial claim. During the trial payment period, the borrower must complete three months of payments at the amount that will continue under the modification.<sup>37</sup>
- In 2012, FHA revised the Loss Mitigation Home Retention Options to reduce the claims against the MMI and help more borrowers stay in their homes. These revisions included eliminating the maximum Back End Debt to Income ratio; eliminating the restriction on the principal, interest, taxes and insurance that can be included in the claim; and, eliminating the requirement that the existing mortgage be no more than 12 months past due.<sup>38</sup>
- In 2013, FHA established updated requirements for PFSs and Deed in Lieu (DIL) requirements. These changes included the use of the Deficit Income Test (DIT) and the elimination of the financial hardship/deficit income PFS requirement for servicemen who have received a Permanent Change of Station order.<sup>39</sup>

---

<sup>34</sup> Mortgagee Letter 96-61, November 12, 1996: FHA Loss Mitigation Procedures - Special Instructions.

<sup>35</sup> Mortgagee Letter 2008-43, December 24, 2008: Pre-Foreclosure Sale (PFS) Program - Utilizing the PFS Loss Mitigation Option to Assist Families Facing Foreclosure.

<sup>36</sup> Mortgagee Letter 2010-23, August 6, 2010: FHA Refinance of Borrowers in Negative Equity Positions.

<sup>37</sup> Mortgagee Letter 2011-28, August 15, 2011: Trial Payment Plan for Loan Modifications and Partial Claims under Federal Housing Administration's Loss Mitigation Program.

<sup>38</sup> Mortgagee Letter 2012-22, November 16, 2012: Revisions to FHA's Loss Mitigation Home Retention Options.

<sup>39</sup> Mortgagee Letter 2013-23, July 9, 2013: Updated Pre-Foreclosure Sale (PFS) and Deed in Lieu (DIL) of Foreclosure Requirements.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 19

- In 2013, additional modifications were made to the FHA Loss Mitigation Home Retention Options. These changes included defining continuous income that can be considered in the transaction, allowing for arrearages to be included in partial claims, and allowing for modifications for mortgagors in bankruptcy.<sup>40</sup>
- In 2014, the updated PFS guideline required a minimum marketing period of 15 calendar days for all PFS transactions. It also clarified that non-arms-length transactions are permitted only if they are necessary to comply with state law.<sup>41</sup>
- Also in 2014, FHA issued a mortgagee letter to increase the use of Claims Without Conveyance of Title (CWCOT) procedures. This letter also established that the Commissioner's Adjusted Fair Market Value must be used for all foreclosure sales and PFS efforts.<sup>42</sup>
- In 2018, FHA issued a mortgagee letter implementing special loss mitigation processes for victims of Hurricanes Irma, Harvey and Maria and the California Wildfires. These procedures were implemented to help homeowners stay in their homes and reduce losses to FHA.<sup>43</sup>
- Later in 2018, FHA issued a mortgagee letter in response to continued elevated default rates and lower utilization of loss mitigation options in Puerto Rico and the U.S. Virgin Islands. This mortgagee letter expanded loss mitigation assistance to borrowers in default.<sup>44</sup>
- In 2019, HUD incorporated additional changes to further streamline and revise Loss Mitigation

---

<sup>40</sup> Mortgagee Letter 2013-32, September 20, 2013: Update to FHA's Loss Mitigation Home Retention Options.

<sup>41</sup> Mortgagee Letter 2014-15, July 10, 2014: Updated Requirements for Pre-Foreclosure Sales (PFS) and Deeds in Lieu (DIL) of Foreclosure.

<sup>42</sup> Mortgagee Letter 2014-24, November 26, 2014: Increasing Use of FHA's Claims Without Conveyance of Title (CWCOT) Procedures.

<sup>43</sup> Mortgagee Letter 2018-01, February 22, 2018: Loss Mitigation for borrowers with FHA-insured mortgages whose property and/or place of employment is located in Presidentially-Declared Major Disaster Areas, adversely affected by Hurricanes Harvey, Irma, Maria, certain California wildfires that occurred in October 2017 (FEMA-DR-4344) or certain California Wildfires, Flooding, Mudflows, and Debris Flows that occurred in December 2017 (FEMA-DR-4353).

<sup>44</sup> Mortgagee Letter 2018-05, August 15, 2018: Updated Loss Mitigation for mortgagees servicing mortgage loans for borrowers with FHA-insured mortgages whose property and/or place of employment is located in the Presidentially-Declared Major Disaster Areas (PDMDAs) of Puerto Rico Hurricane Maria DR-4339 or Virgin Islands Hurricane Maria DR-4340 and Disaster Foreclosure Moratorium for certain FHA-insured mortgages secured by properties located in areas of Puerto Rico and the U.S. Virgin Islands that the U.S. Department of Homeland Security's Federal Emergency Management Agency (FEMA) has declared to be eligible for Individual Assistance (Affected Counties) as a result of Hurricane Maria (Puerto Rico Hurricane Maria DR-4339 and Virgin Islands Hurricane Maria DR-4340).

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 20

Procedures for Presidentially Declared Major Disaster Areas (PDMDAs).<sup>45</sup>

### COVID-19 Pandemic

The President of the United States proclaimed that the COVID-19 outbreak in the United States constitutes a national emergency as of March 1, 2020. As a result, for a period of time many jurisdictions reduced services, businesses closed, and other activities were curtailed. In addition, the pandemic has impeded the ability of Americans to work and provide for their families. This directly impacts the financial wellbeing of individuals, families, and businesses. Furthermore, many Americans have been asked to remain in their homes to stem the tide of COVID-19 as many states implemented shelter-in-place orders. To ensure families are not displaced during this critical period, several mortgagee letters were issued.

- March 18, 2020: Properties secured by FHA-insured mortgages were subject to a 60-day moratorium on foreclosures. This moratorium applied to the initiation of foreclosures and foreclosures in process.<sup>46</sup> On May 14, 2020, the foreclosure moratorium was extended through June 30, 2020.<sup>47</sup> On June 17, 2020, the moratorium was extended through August 31, 2020,<sup>48</sup> and on August 27, 2020 the moratorium was extended through December 31, 2020.<sup>49</sup> Deadlines for the first legal action and reasonable diligence times were extended by 90 days from the date of the expiration of the moratorium.
- March 27, 2020: Rules for re-verification of employment were adjusted to account for the fact that many businesses were closed during shelter-in-place orders. Also, changes were made to FHA Appraisal Protocols to allow for exterior only and desktop appraisals in order to maintain appropriate social distancing.<sup>50</sup> On May 14, 2020, the applicability of these changes were extended through June 30, 2020.<sup>51</sup> On June 29, 2020, the applicability of these changes were extended through August 31, 2020.<sup>52</sup> On

---

<sup>45</sup> Mortgagee Letter 2019-14, August 29, 2019: Updates to FHA's Loss Mitigation Options for Borrowers in Presidentially-Declared Major Disaster Areas (PDMDAs)

<sup>46</sup> Mortgagee Letter 2020-04, March 18, 2020: Foreclosure and Eviction Moratorium in connection with the Presidentially Declared COVID-19 National Emergency.

<sup>47</sup> Mortgagee Letter 2020-13, May 14, 2020: Extension of Foreclosure and Eviction Moratorium in connection with the Presidentially-Declared COVID-19 National Emergency and New Reporting Requirements Related to FHA Single Family's CARES Act Loss Mitigation Options.

<sup>48</sup> Mortgagee Letter 2020-19, June 17, 2020: Extension of Foreclosure and Eviction Moratorium in Connection with the Presidentially-Declared COVID-19 National Emergency.

<sup>49</sup> Mortgagee Letter 2020-27, August 27, 2020: Extension of Foreclosure and Eviction Moratorium in Connection with the Presidentially-Declared COVID-19 National Emergency.

<sup>50</sup> Mortgagee Letter 2020-05, March 27, 2020: Re-verification of Employment and Exterior-Only and Desktop-Only Appraisal Scope of Work Options for FHA Single Family Programs Impacted By COVID-19.

<sup>51</sup> Mortgagee Letter 2020-14, May 14, 2020: Extension of the Effective Date of Mortgagee Letter 2020-05, Re-verification of Employment and Exterior-Only and Desktop-Only Appraisal Scope of Work Options for FHA Single Family Programs Impacted By COVID-19.

<sup>52</sup> Mortgagee Letter 2020-20, June 29, 2020: Re-Extension of the Effective Date of Mortgagee Letter 2020-05, Re-verification of Employment and Exterior-Only and Desktop-Only Appraisal Scope of Work Options for FHA Single Family Programs Impacted By COVID-19.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 21

August 28, 2020, the applicability of these changes was extended through October 31, 2020.<sup>53</sup>

- April 1, 2020: Borrowers who experienced an adverse impact on their ability to make on-time mortgage payments were eligible for forbearance for an initial period of six months, and this initial period can be extended by up to six additional months. While in forbearance, the borrower must be evaluated for loss mitigation options.<sup>54</sup> On July 8, 2020, HUD issued a mortgagee letter detailing the full suite of loss mitigation options available for borrowers affected by COVID-19.<sup>55</sup> On October 20, 2020, the date for approving a COVID-19 forbearance was extended to December 31, 2020.<sup>56</sup>
- June 4, 2020: Mortgages under forbearance due to the effects of COVID-19 were allowed to be endorsed by HUD if at the time of the closing the buyer met all necessary requirements and the mortgage was current at the time of forbearance.<sup>57</sup>
- June 12, 2020: Claims for loss mitigation options were allowed to be submitted electronically.<sup>58</sup>

The COVID-19 pandemic, the shelter-in-place orders and the modifications to the loss mitigation and forbearance guidelines will have a significant impact on the Cash Flow NPV of the MMI. We have considered these impacts as part of our analysis, and will highlight throughout the report how COVID-19 has impacted our analysis and the Cash Flow NPV projections.

### Current and Future Market Environment

In addition to the policies related to the MMI, the default and claim rate and ultimately the Cash Flow NPV of the MMI are dependent on the economic environment. As interest rates increase, mortgage rates tend to increase, which in turn causes default rates to increase. The general health of the economy impacts the value of homes. As home values increase, losses to the MMI will tend to decrease as the value received in the disposition of a home increases. Also, as the general health of the economy improves, the demand for mortgages increases. This generally results in an increase in the demand for mortgages endorsed by the MMI for mortgage insurance.

The impacts of COVID-19 on the economy have been significant. For some of the economic variables considered

---

<sup>53</sup> Mortgagee Letter 2020-28, August 28, 2020: Re-Extension of the Effective Date of Mortgagee Letter (ML) 2020-05, Reverification of Employment and Exterior-Only and Desktop-Only Appraisal Scope of Work Options for the Federal Housing Administration (FHA) Single Family programs impacted by the Coronavirus Disease of 2019 (COVID-19).

<sup>54</sup> Mortgagee Letter 2020-06, April 1, 2020: FHA's Loss Mitigation Options for Single Family Borrowers Affected by the Presidentially-Declared COVID-19 National Emergency in Accordance with the CARES Act.

<sup>55</sup> Mortgagee Letter 2020-22, July 8, 2020: FHA's COVID-19 Loss Mitigation Options.

<sup>56</sup> Mortgagee Letter 2020-34, October 20 2020: Update to the Date for Approving a COVID-19 Forbearance or COVID19 Home Equity Conversion Mortgage (HECM) Extension.

<sup>57</sup> Mortgagee Letter 2020-16, June 4 2020: FHA Catalyst: Case Binder Module – Single Family Forward and Home Equity Conversion Mortgage (HECM) Electronic Endorsement Submission.

<sup>58</sup> Mortgagee Letter 2020-18, June 12 2020: FHA Catalyst: Claims Module - Single Family Forward Loss Mitigation Home Retention Claims.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

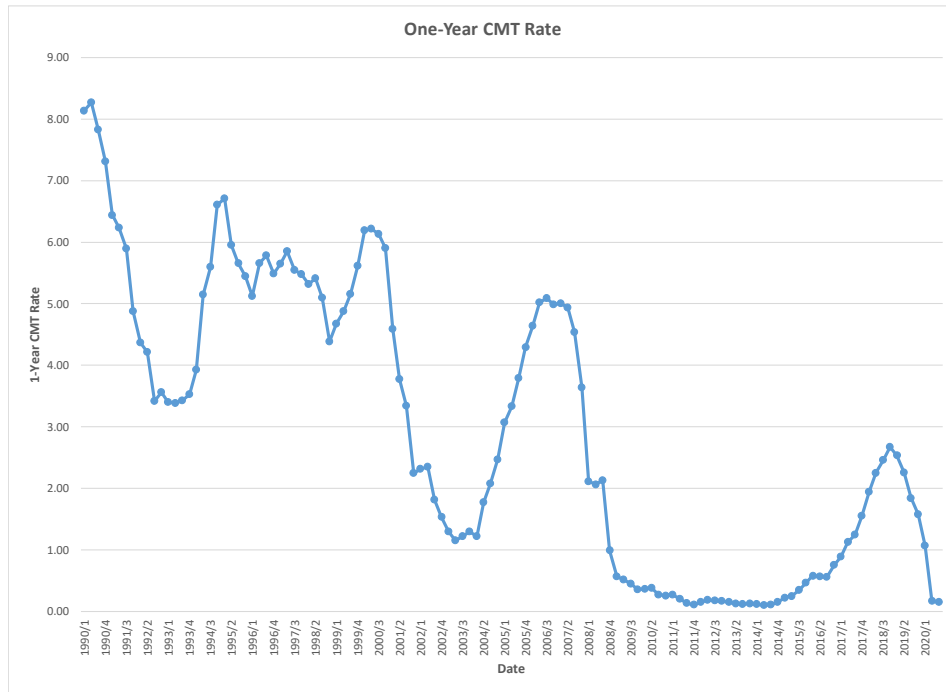
Page 22

in the analysis, the impact of COVID-19 has caused levels that have not been seen historically. Throughout the analysis, we have analyzed the impact of COVID-19 on economic and other variables and the Cash Flow NPV.

## Interest Rates

Figure 1 shows the historical one-year CMT rate since 1990.

Figure 1: One-Year CMT Rate



In 2008, in response to the housing crisis and economic recession, the Federal Reserve began decreasing interest rates as part of an active monetary policy. At the beginning of 2007, the one-year CMT rate was around 5%. Over the next seven years, the rate dropped steadily to a low of 0.1% in the fourth quarter of 2014. Subsequent to 2014, the rate began increasing again to a high of 2.7% by December 2018. Since that time the rate has been decreasing, and as of the third quarter of 2020, was at 0.17%, the lowest level since 2014. Recent decreases in the one-year CMT have been a direct result of monetary policy in response to the economic impact of COVID-19.

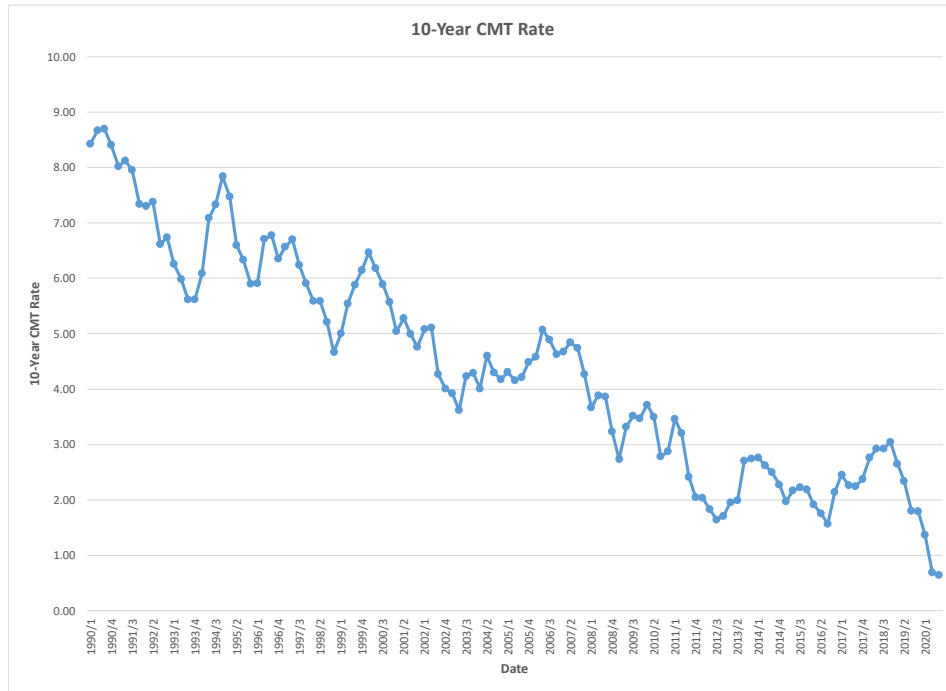
Figure 2 shows the 10-year CMT rate since 1990.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 23

Figure 2: 10-Year CMT Rate



The 10-year CMT rate shows a similar trend, although the changes are not as significant. In mid-2007, the 10-year CMT rate was nearly 5%. Since that time, the rate dropped to under 2% in 2012. Subsequent to 2012, the rate increased to just over 3.0% by December 2018. The rate has since been decreasing, and due to the economic impacts of COVID-19 has dropped to 0.64%, the lowest level in the last 30 years.

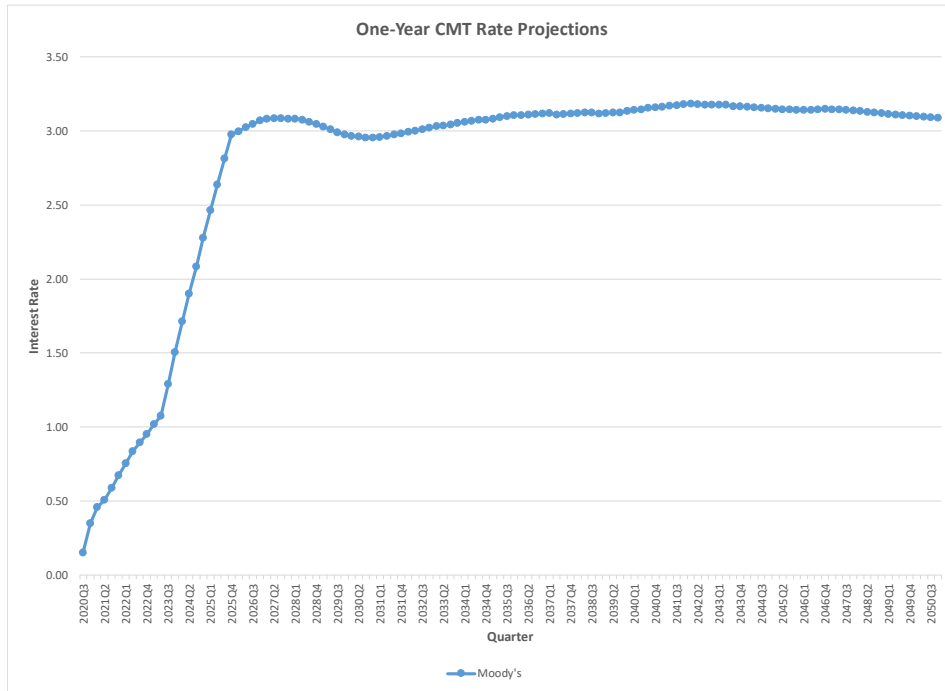
For the purposes of projecting Cash Flow NPV, it is required that Pinnacle produce an estimate using the projection figures from the OMB. In addition to OMB projections, Pinnacle has also used Moody's economic projections to generate a range of indications of the economic value. Figure 3 shows the one-year CMT rate projections from Moody's Baseline Scenario.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 24

Figure 3: One-Year CMT Rate Projections



Moody's projections show increases in the one-year CMT rates. The rate increases to 3.1% by 2027, and then remains in the range of 2.9% to 3.2% for the rest of the projection period.

The 10-year CMT rate projections from Moody's are shown below.

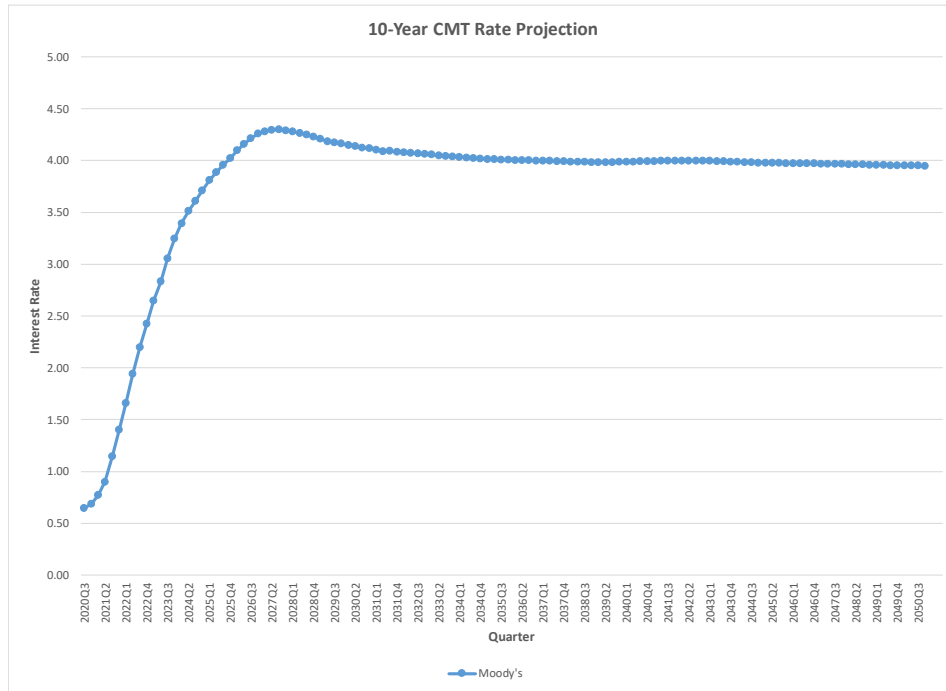


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 25

Figure 4: 10-Year CMT Rate Projection



The 10-year CMT rate increases gradually and then stabilizes at approximately 4.0% by the end of the projection period.

## Home Price Index Growth

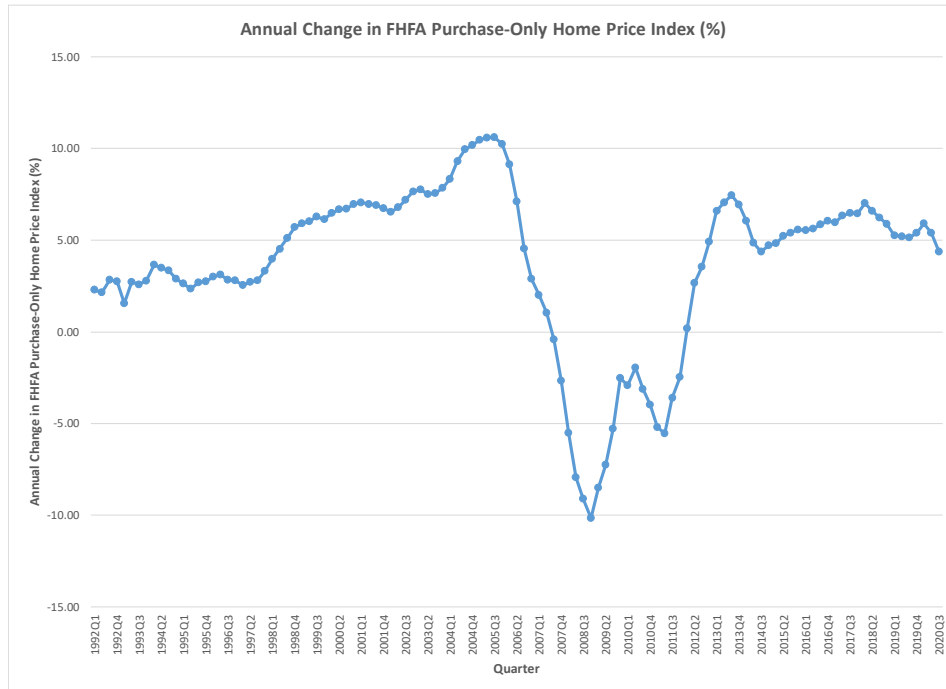
The growth rate in home prices will have an impact on the volume of mortgages endorsed by FHA, the percentage of defaults in mortgages and the ultimate cost of the mortgage insurance claims. The annual percentage change in the historical Federal Housing Finance Agency (FHFA) Purchase Only House Price Index by quarter is shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 26

Figure 5: Historical FHFA Purchase Only House Price Index



From 1992 through 2005, the annual rate of change increased to a high of over 10%. During the housing crisis that began in 2006, the annual rate of change decreased significantly, dropping to a low of -10% in 2008 and remained negative through 2012. The increasing trend continued through 2013, and the rate then remained between 5% - 7% through the second quarter of 2020. The rate dropped to 4.4% in the third quarter of 2020.

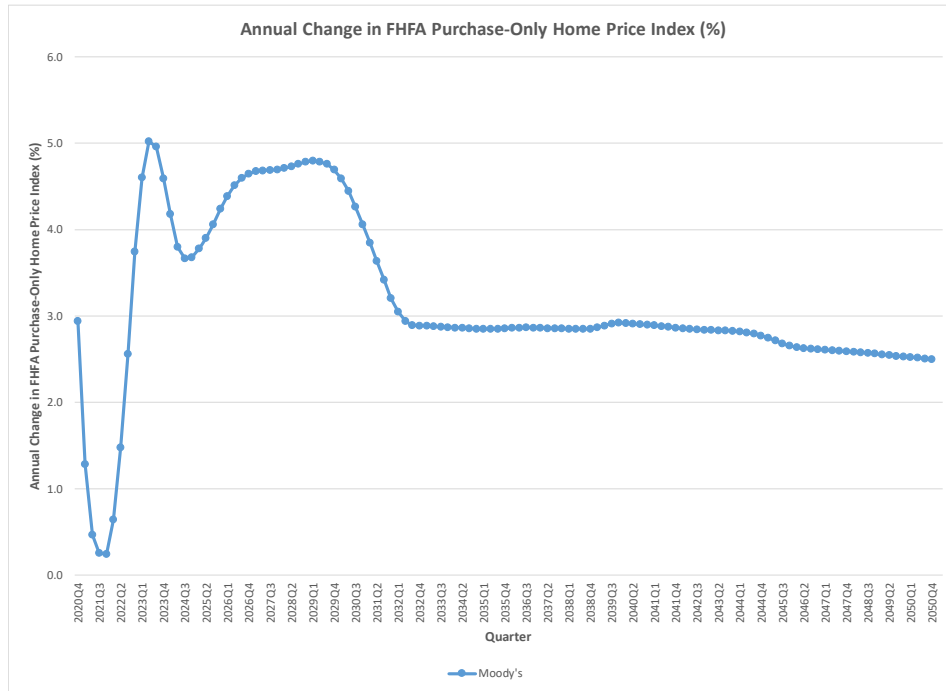
Moody's projects the home price index to 2050. Moody's also produces a forecast for local areas, including metropolitan areas and states. The annual percentage change in the countrywide projected Federal Housing Finance Agency (FHFA) Purchase Only House Price Index by quarter is shown below for Moody's baseline projections.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 27

Figure 6: FHFA Purchase Only House Price Index



For Moody’s projections, the annual percentage change for the index decreases from about 2.9% to 0.2% in 2021. The rate then increases sharply to 5.0% by 2023, then decreases and stabilizes long-term near 3.0%.

## Unemployment Rate

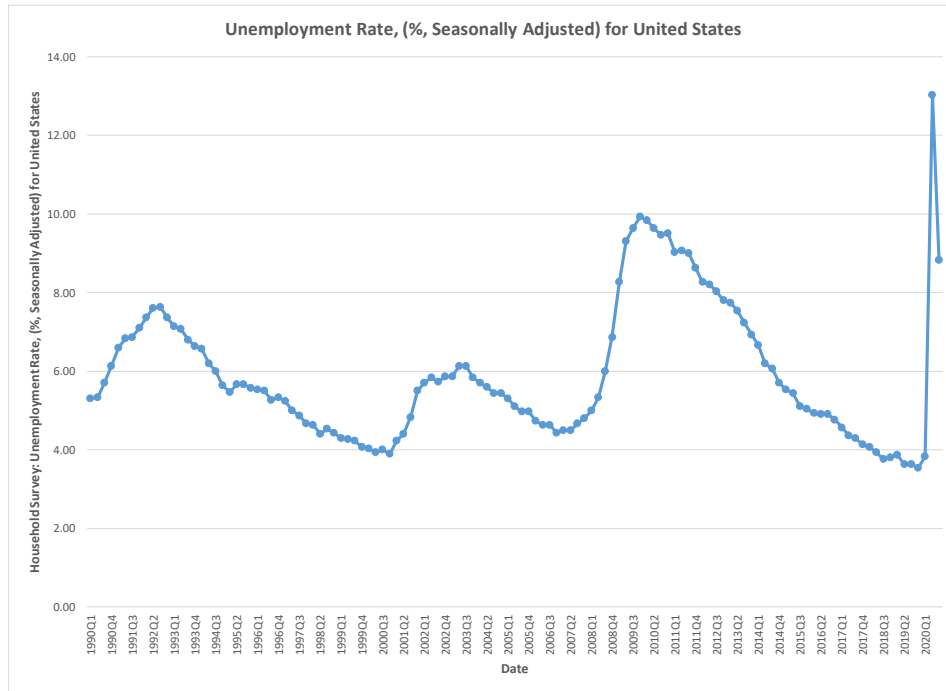
The unemployment rate has an impact on the ability of homeowners to make their mortgage payments. This impacts the default rates and ultimate projections of the MMI. The historical unemployment rate is shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 28

Figure 7: Historical Unemployment Rate



Beginning in 2008, as the economic downturn occurred, the seasonally adjusted unemployment rate nearly doubled from 5% to just under 10% by the end of 2009. Since 2009, the rate had decreased steadily to 3.5% by year-end 2019. In 2020, the economic issues associated with the COVID-19 pandemic resulted in an unemployment rate of 13% in the second quarter of 2020. The rate has dropped to 8.83% in the third quarter of 2020.

The projected unemployment rates from Moody’s are shown in Figure 8.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 29

Figure 8: Unemployment Rate Projection



Moody’s projections show a significantly decreasing trend through 2024. The unemployment rate then continues to decrease slowly through the remainder of the projection period, remaining long-term at approximately 4.5%.

## Mortgage Volume

The mortgage endorsement volume for FHA and the U.S. home market is shown in Table 5. The health and capacity of the private mortgage insurance market can impact the projected value of the MMI. If the private mortgage insurance market increases capacity and is successful in providing insurance to borrowers who are less likely to default, it could have an impact on the Cash Flow NPV of the MMI.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 30

Table 5: FHA Share of Home Sales

Calendar Year	Volume of Home Sales (\$ Billions)		
	FHA	Market	FHA Share (%)
2001	89	958	9.3%
2002	82	1,096	7.5%
2003	71	1,273	5.6%
2004	53	1,306	4.1%
2005	37	1,506	2.5%
2006	36	1,401	2.5%
2007	39	1,142	3.5%
2008	129	741	17.5%
2009	185	653	28.3%
2010	167	539	31.0%
2011	129	503	25.7%
2012	127	598	21.2%
2013	119	731	16.3%
2014	107	762	14.0%
2015	154	896	17.2%
2016	176	1,049	16.7%
2017	174	1,140	15.2%
2018	158	1,207	13.1%
2019	170	1,270	13.4%
2020	135	963	14.0%

Sources: FHA Volume from FHA Data Warehouse, September 30, 2020 extract. Market volume from Mortgage Bankers Association.

FHA’s share of the volume of home sales has increased significantly from its low of 2.5% in 2005 and 2006. From 2002 to 2006, FHA’s share of the number and volume of home sales declined as the subprime mortgage market expanded from 2003 to 2007. The housing and economic crisis that occurred in 2008 decreased the availability of mortgages in general, and significantly impacted the availability of subprime mortgages. Private mortgage insurers were also facing significant losses and decreased the volume of insurance they were providing. As a result, FHA’s market share began to increase significantly. The volume of FHA endorsed mortgages increased from 2.5% to 31.0% from 2006 to 2010. As the housing market has recovered, the percentage of loans endorsed by FHA had decreased steadily through 2018 to 13.1%. As of the third quarter of 2020, the FHA share has now increased to 14.0%. The increase in 2020 may be due in part to tightening of loan underwriting standards by private mortgage insurers in response to COVID-19.

## Report Structure

The remainder of this report is divided into the following sections:

- **Section 2. Summary of Findings and Comparison with Fiscal Year 2019 Actuarial Review** – presents the MMI Economic Net Worth for Fiscal Year 2020 and the projected Cash Flow NPV by cohort and product. This section also provides a reconciliation and explanation of the major differences between the Fiscal Year 2019 and Fiscal Year 2020 Reports.
- **Section 3. Cash Flow NPV Based on Alternative Scenarios** – presents estimates of the MMI Cash Flow

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 31

NPV using a range of alternative economic assumptions.

- **Section 4. Characteristics of the Fiscal Year 2020 Insurance Portfolio** – describes the Fiscal Year 2020 insurance portfolio and compares the risk characteristics of the origination books of business across historical Fiscal Years.
- **Section 5. Summary of Methodology** – presents an overview of the data processing, transition, loss severity and cash flow models used in the analysis.
- **Appendix A: Data Sources – Processing and Reconciliation** – provides a description of the data sources used for the analysis, the data processing required to prepare the data for analysis and the data reconciliation performed.
- **Appendix B: Transition Models** – provides a technical description of our predictive models of current and default transitions, the model parameters and model validation results.
- **Appendix C: Loss Severity Models** – provides a technical description of our predictive models of loss severity rates, the model parameters and model validation results.
- **Appendix D: Economic Scenarios** – describes the forecast of future values of economic factors that affect the performance of the MMI and presents the variation in estimated Cash Flow NPV based on the additional economic scenarios. Details of the stochastic analysis are also provided.
- **Appendix E: Cash Flow Analysis** – describes the process used to project future cash flows.
- **Appendix F: Review of HUD Analysis of Economic Net Worth, Comparison of HUD and Pinnacle Models, and Assessment of Vulnerabilities** – high-level review of HUD models developed to project Economic Net Worth, comparison of the models developed by HUD with the models developed by Pinnacle, and assessment of the vulnerabilities of the models developed.
- **Appendix G: Summary of Historical and Projected Claim Rates, Non-Claim Termination Rates and Loss Severities** – historical and projected claim, non-claim termination and loss severity rates.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 32

### Section 2 - Summary of Findings and Comparison with Fiscal Year 2019 Actuarial Review

---

This section presents the Economic Net Worth and the details of the Cash Flow NPV of the MMI Forward Loan portfolio as of the end of Fiscal Year 2020, and also shows a comparison of the elements of the Economic Net Worth between the 2019 Actuarial Review and this review.

#### Economic Net Worth Estimate

The Economic Net Worth is defined as cash available to the Fund plus the Cash Flow NPV of all future cash outflows and inflows that are expected to result from the mortgages currently insured by the MMI. The 2020 Actuarial Review estimates the Cash Flow NPV of the MMI as of the end of Fiscal Year 2020 using data through September 30, 2020. We developed this estimate by analyzing historical loan performance using data provided by FHA, developing predictive models for loan transition and losses, and using these model results along with economic projections from the OMB and Moody's to project future cash flows of the MMI. The NPV of these cash flows along with the MMI's capital resources represent the economic value of the MMI.

The predictive models used in this report are similar conceptually to the models developed in the 2019 Actuarial Review. We have developed binomial logistical models by product type to predict each transition type independently. The binomial model results are then combined in the final simulation to reflect the multiple possible transition outcomes.

Appendices A through G describe the individual models, the assumptions used and the detailed projection model results. Our main findings are as follows.

The Cash Flow NPV is computed from the projected cash flows occurring during Fiscal Year 2021 and subsequent. It is computed based on economic projections associated with the OMB Economic Assumptions. **As of the end of Fiscal Year 2020, Pinnacle estimates that the MMI Cash Flow NPV is \$23.397 billion.** The Cash Flow NPV estimate provided by FHA to be used in FHA's Annual Report to Congress is \$10.4 billion.

The capital resource available to the MMI is \$67.368 billion, which results in an Economic Net Worth of \$90.765 billion.

In addition to the overall estimate of the Cash Flow NPV, we have estimated the Cash Flow NPV by cohort. The Pinnacle estimate compared to the FHA estimate by cohort is shown below.



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 33

Table 6: Cash Flow NPV by Cohort (\$ in billions)

Cohort	Pinnacle	FHA	Dollar
			Difference
1992	0.0	0.0	0.0
1993	0.0	0.0	0.0
1994	0.0	0.0	0.0
1995	0.0	0.0	0.0
1996	0.0	0.0	0.0
1997	0.0	0.0	0.0
1998	0.0	0.0	0.0
1999	0.0	0.0	0.0
2000	0.0	0.0	0.0
2001	0.0	0.0	0.0
2002	-0.1	0.0	0.0
2003	-0.1	-0.1	0.0
2004	-0.2	-0.1	0.0
2005	-0.2	-0.2	0.0
2006	-0.2	-0.2	0.0
2007	-0.3	-0.3	0.0
2008	-0.7	-0.6	0.0
2009	-0.9	-0.8	-0.1
2010	-0.8	-0.6	-0.1
2011	-0.5	-0.3	-0.2
2012	-0.4	-0.2	-0.2
2013	-0.4	0.5	-0.9
2014	1.8	1.4	0.4
2015	3.5	2.3	1.2
2016	4.4	2.9	1.4
2017	4.0	2.7	1.3
2018	1.5	0.8	0.7
2019	2.0	-0.3	2.3
2020	10.9	3.6	7.3

The Pinnacle estimates by cohort are consistent with the FHA estimates through 2007, slightly lower for cohorts 2008 – 2012, increasingly lower for 2013, and higher for cohorts 2014 and 2020. The total Pinnacle Cash Flow NPV estimate is \$13.0 billion higher than the FHA estimate, which as a percentage of unamortized IIF is 0.95%. The current unamortized IIF is \$1,374 billion. The difference between the Pinnacle and FHA estimate as a percentage of amortized IIF is 1.06%. The current amortized IIF is \$1,226 billion.

The housing and economic crisis that occurred in 2008 has resulted in higher claim rates for mortgages originated during Fiscal Years 2005 - 2010. Given that their upfront MIP has already been collected and is included as part of the current capital resources, and due to their large origination volume, the Fiscal Year 2008 - 2010 cohorts are estimated to experience larger negative Cash Flow NPVs than any other cohort. However, at the end of the housing recession, house prices bottomed out and then turned positive, and as a result

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 34

mortgages originated in Fiscal Years 2014 - 2020 have positive Cash Flow NPVs. The NPV is also being positively impacted for these more recent cohorts due to MIP now being collected over the life of the mortgage.

Also, the 2020 Cash Flow NPV is influenced by the significant increase in new originations. There has been a significant increase in refinance activity. While this results in a decrease in Cash Flow NPV for older cohorts, it results in an increase in Cash Flow NPV for the 2020 cohort as these loans refinance into the 2020 cohort.

The table below shows Pinnacle's Cash Flow NPV estimates by cohort and product.

Table 7: Cash Flow NPV by Cohort and Product

Cohort	Fixed Rate 30	Fixed Rate 15	Adjustable Rate Mortgage	Total
1992	(357,852)	-	(81,230)	(439,081)
1993	(814,965)	-	(139,304)	(954,269)
1994	(1,763,493)	-	(126,089)	(1,889,582)
1995	(1,221,310)	-	(150,734)	(1,372,044)
1996	(3,484,182)	-	(718,795)	(4,202,977)
1997	(4,733,549)	-	(1,088,038)	(5,821,587)
1998	(9,809,192)	-	(608,777)	(10,417,969)
1999	(15,701,392)	-	(621,549)	(16,322,941)
2000	(12,202,704)	-	(1,000,170)	(13,202,874)
2001	(43,940,995)	-	(1,011,027)	(44,952,022)
2002	(67,738,409)	-	(4,659,137)	(72,397,546)
2003	(105,458,676)	-	(3,103,828)	(108,562,504)
2004	(153,115,135)	-	(10,907,290)	(164,022,425)
2005	(142,173,872)	(1,325)	(12,301,688)	(154,476,885)
2006	(169,227,056)	(11,844)	(5,331,314)	(174,570,213)
2007	(251,514,715)	(183,485)	(3,945,638)	(255,643,837)
2008	(680,655,568)	(452,740)	(7,774,853)	(688,883,160)
2009	(900,599,648)	(1,994,808)	(22,516,389)	(925,110,846)
2010	(742,534,887)	(2,750,023)	(24,883,402)	(770,168,313)
2011	(455,377,470)	(3,701,037)	(25,045,495)	(484,124,002)
2012	(419,389,894)	(5,080,639)	(10,023,225)	(434,493,758)
2013	(361,646,127)	(3,546,396)	(2,036,012)	(367,228,535)
2014	1,829,553,992	8,788,311	10,484,092	1,848,826,395
2015	3,521,353,579	12,561,607	8,071,309	3,541,986,495
2016	4,396,783,295	17,335,597	(15,748,581)	4,398,370,311
2017	3,974,683,339	24,014,332	677,256	3,999,374,927
2018	1,543,437,770	15,894,632	(7,972,574)	1,551,359,828
2019	2,126,299,581	13,702,738	(8,945,348)	2,131,056,971
2020	11,064,193,137	21,174,198	1,339,975	11,086,707,311
Total	23,912,843,600	95,749,119	(150,167,854)	23,858,424,865

The value of the overall Cash Flow NPV is influenced primarily by the fixed rate 30-year mortgage (FRM30) product, which has the largest volume of mortgages historically. The total Cash Flow NPV is positive for the FRM30 and Fixed Rate 15 year (FRM15) products, and is negative for the ARM products.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 35

### Change in the Economic Net Worth

Table 8 shows the comparison of our estimate of the MMI's Cash Flow NPV and IIF at the end of Fiscal Year 2020 to the Cash Flow NPV estimate in the 2019 Review.

Table 8: Estimate of Cash Flow NPV as of the end of Fiscal Year 2020 (\$ in millions)

Item	2019	2020	Dollar Difference	Percent Change
Cash Flow NPV	18,643	23,397	4,754	25.5%
Capital Resources	54,600	67,368	12,768	23.4%
Economic Net Worth	73,243	90,765	17,522	23.9%
Unamortized Insurance-In-Force	1,363,985	1,373,960	9,975	0.7%

As seen in Table 8, the estimated Fiscal Year 2020 Cash Flow NPV of the MMI has increased by \$4.754 billion from the level estimated in Fiscal Year 2019, from \$18.643 billion to \$23.397 billion. The capital resources available to the MMI have increased by 23.4%, from \$54.600 billion to \$67.368 billion. The unamortized IIF increased by 0.7% from \$1.364 trillion to \$1.374 trillion. The change in the Cash Flow NPV represents the net impact of several significant factors, which are described in the next section.

### Sources of Change in the Cash Flow NPV from the Fiscal Year 2019 Review

Table 9 provides a summary of the decomposition of changes in the Cash Flow NPV of the MMI as of the end of Fiscal Year 2020 as compared to the Cash Flow NPV in the Fiscal Year 2019 report. The overall net change in the Cash Flow NPV is positive.

Table 9: Changes in Projected Cash Flow NPV

	Change in NPV	Cash Flow NPV - 9/30/20
<b>Baseline FY1992-FY2019</b>		18,642,778,021
Impact of assumption change	-12,151,853,792	6,490,924,229
Impact of model change	9,168,552,903	15,659,477,132
Impact of book change	-3,151,725,013	12,507,752,119
FY1992-FY2019	-6,135,025,902	
FY2020	10,888,930,652	23,396,682,771
<b>Cumulative Change</b>	4,753,904,750	

This section describes the sources of change in estimates of Cash Flow NPV between this year's review and last year's review. Separating out the specific impacts can be done only up to a certain degree of accuracy as the results can vary depending on the order in which the decomposition is done. The interdependency among the various components of the analysis prevents us from identifying and analyzing these as purely independent effects. Given this limitation, this section presents a description of the approximate differences in the Cash Flow NPV from that presented in the Fiscal Year 2019 Review by source of change.

### Updated Economic Scenario Forecast

For this decomposition step, we updated the forecasts for the purchase-only HPI and the interest and unemployment rates from 2020 PEA forecast to the 2021 PEA forecast. This step also replaces the projection

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 36

used in 2019 Actuarial Review with the actual economic experience for the fourth quarter of 2019 and the first three quarters of 2020. The significant increase in unemployment in 2020 has a negative impact on the projected Cash Flow NPV.

The cumulative result of these economic assumption changes is a decrease of \$12.152 billion in the projected Cash Flow NPV.

### [Updated Predictive Models](#)

With this analysis, we have continued to refine the predictive models to better capture the termination behavior and projected claim amounts of loans in the MMI. We re-estimated the models using updated data and revised variable specifications, and the model assumptions have been adjusted to better reflect the expected ultimate projected claim rates. We have also adjusted our models for the impact of changes to forbearance rules and the economic challenges of COVID-19. For details about these model updates and refinements, refer to Appendices B, C and E. The most significant changes in the model parameters reflect continuing improvements in claim rates, default rates, and ultimate claim amounts.

These model changes led to an increase in estimated economic value in the Cash Flow NPV of \$9.169 billion.

### [Actual Performance of Cohorts 2019 and Prior in Fiscal Year 2020](#)

The actual performance of the MMI 2019 and prior cohorts realized during Fiscal Year 2020 affects the Cash Flow NPV of the MMI estimate of the in-force portfolio. The actual experience for this period was \$3.152 billion worse than expected. This is driven in part by the impacts of COVID-19, resulting in increased defaults, increased loss mitigations and increased refinance activity.

### [Fiscal Year 2020 Origination Volume](#)

The addition of the origination volume for the Fiscal Year 2020 book of business had a positive impact on the NPV. This impact is due in part to the significant increase in volume of refinances. This additional origination volume increased the Cash Flow NPV projection by \$10.889 billion.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 37

### Section 3 - Cash Flow NPV Based on Alternative Scenarios

---

The Cash Flow NPV of the MMI will vary from our estimates if the actual economic drivers of mortgage performance deviate from the baseline projections associated with the OMB Economic Assumptions. In this section, we develop additional estimates of the Cash Flow NPV based on the following approaches:

1. Moody's economic scenarios
2. Stochastic simulation of key economic variables
3. Sensitivity testing of key economic variables

We use these additional estimates of the Cash Flow NPV to develop a range of estimates. These alternative estimates are compared to the Cash Flow NPV resulting from the OMB Economic Assumptions to determine the sensitivity of the Cash Flow NPV estimate to alternative assumptions.

Each Moody's scenario produces an estimate of the Cash Flow NPV using future interest, unemployment and HPI rates as a deterministic path. We are including 10 Moody's scenarios in the analysis. These scenarios are consistent with the scenarios used in the 2019 Actuarial Review.

The Moody's scenarios are:

- Baseline
- Alternative 0 – Upside (4<sup>th</sup> Percentile)
- Alternative 1 – Upside (10<sup>th</sup> Percentile)
- Alternative 2 – Downside (75<sup>th</sup> Percentile)
- Alternative 3 – Downside (90<sup>th</sup> Percentile)
- Alternative 4 – Downside (96<sup>th</sup> Percentile)
- Slower Trend Growth
- Stagflation
- Next-Cycle Recession
- Low Oil Price

The resulting Cash Flow NPV associated with each alternative scenario is summarized in Table 10. Below, we discuss the characteristics of each Moody's scenario.

#### Baseline Scenario

In the Baseline scenario, the HPI is flat through the third quarter of 2021, and then increases over the remainder of the projection period. The rate of increase is just under 5% per year through 2029, and then decreases to about 3% per year for the remainder of the projection period. The mortgage interest rate decreases to about 3% through the second quarter of 2021 and then increases through 2028. The mortgage rate levels off at approximately 5.5% by 2029. The unemployment rate is projected to decrease through 2023 to approximately 4.5%, and then remain steady at that level for the remainder of the projection period. Under this scenario, it is

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 38

projected that it will take approximately three years for unemployment to fully return to more stable levels, and it is projected to stabilize at a level higher than pre-COVID-19 unemployment levels.

### **Alternative Scenario 0 – Upside (4<sup>th</sup> Percentile)**

In the Alternative Scenario 0 – Upside (4<sup>th</sup> Percentile), the HPI is projected to increase throughout the entire projection period. The rate of increase is about 4 - 5% per year through 2029, and then decreases to about 3% per year for the remainder of the projection period. The mortgage interest rate increases through 2027, then levels off at approximately 5.4% for the remainder of the projection period. The unemployment rate is projected to decrease through 2024 to approximately 3.6%, and then increase gradually until it stabilizes at approximately 4.5%. Under this scenario, unemployment recovers to better than pre-COVID-19 levels over the next three years.

### **Alternative Scenario 1 – Upside (10<sup>th</sup> Percentile)**

In the Alternative Scenario 1 – Upside (10<sup>th</sup> Percentile), the HPI is projected to increase throughout the entire projection period. The rate gradually increases from 2.5% per year in the first quarter of 2022 to 5% per year by the second quarter of 2023. The rate then decreases to about 3% per year for the remainder of the projection period. The mortgage interest rate increases for the entire projection period, leveling off at approximately 5.4% by 2026. The unemployment rate is projected to decrease through 2024 to approximately 3.8%, and then increase gradually until it stabilizes at approximately 4.5%. Under this scenario, unemployment recovers to pre-COVID-19 levels over the next three years.

### **Alternative Scenario 2 – Downside (75<sup>th</sup> Percentile)**

In the Alternative Scenario 2 – Downside (75<sup>th</sup> Percentile), the HPI decreases through the fourth quarter of 2021, and then increases throughout the remainder of the projection period. Mortgage interest rates are projected to decrease through the second quarter of 2021, and then increase through 2027. Mortgage rates level off for the remainder of the projection period at approximately 5.4%. The unemployment rate is projected to decrease slowly to 4.5% by 2024. Under this scenario, the recovery in the unemployment rate occurs over a longer period, and is projected to stabilize at a level higher than pre-COVID-19 unemployment levels.

### **Alternative Scenario 3 – Downside (90<sup>th</sup> Percentile)**

In the Alternative Scenario 3 – Downside (90<sup>th</sup> Percentile), the HPI decreases through the first quarter of 2022, and then begins to increase. Mortgage interest rates decrease through the third quarter of 2021, and then begin to increase until they reach the long-term average of about 5.4%. The unemployment rate increases to 10.8% in 2021, then decreases to 4.9% by the end of 2026. Under this scenario, the recovery in the unemployment rate occurs over a longer period, and is projected to stabilize at a level higher than pre-COVID-19 unemployment levels.

### **Alternative Scenario 4 – Downside (96<sup>th</sup> Percentile)**

In Alternative Scenario 4 – Downside (96<sup>th</sup> Percentile), the HPI decreases through the second quarter of 2022, and then begins to increase. Mortgage interest rates drop through the fourth quarter of 2021, and then begin to

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 39

slowly increase until they reach the long-term average of 5.4% in 2029. The unemployment rate spikes to 12% by 2022, and then decreases to 4.9% by 2031. Under this scenario, the recovery in the unemployment rate occurs over a longer period, and is projected to stabilize at a level higher than pre-COVID-19 unemployment levels.

### **Slower Trend Growth**

In the Slower Trend Growth scenario, the HPI increases more slowly than in the Baseline scenario. Mortgage interest rates decrease to 2.9% by the second quarter of 2021, and then settle at a long-term average of 5.0%. The unemployment rate decreases to 4.9% by 2024. Under this scenario, the recovery in the unemployment rate occurs over a longer period, and is projected to stabilize at a level higher than pre-COVID-19 unemployment levels.

### **Stagflation**

In the Stagflation scenario, the HPI decreases through the third quarter of 2022, and then begins to increase. Mortgage interest rates increase to 3.5% by the first quarter of 2021, and then drop through the fourth quarter of 2021. Mortgage interest rates then begin to increase to the long-term average of 5.4%. Unemployment rates decrease to 8.8% by the end of 2020, and then increase to 10.1% by the second quarter of 2021. Unemployment rates then decrease to a long-term average of 4.9% by 2026.

### **Next-Cycle Recession**

In the Next-Cycle Recession scenario, the HPI increases through the first quarter of 2022, and then decreases significantly through the third quarter of 2024. The HPI then increases for the remainder of the projection period. The mortgage interest rates increase through the fourth quarter of 2022, and then decrease through the fourth quarter of 2023. The rates then settle in at a long-term average of about 5.4%. The unemployment rate is equal to the Baseline assumptions through the second quarter of 2022, and then increases to 7.8% by the end of 2023. The rate then decreases to 4.5% by 2034, where it remains for the remainder of the projection period.

### **Low Oil Price**

In the Low Oil Price scenario, the HPI increases throughout the entire projection period, similar to the Baseline scenario. Mortgage interest rates decrease to 2.7% by the second quarter of 2021, and then increase to 5.8% by 2027. The mortgage rate then decreases gradually through the remainder of the projection period. Unemployment rates decrease through the fourth quarter of 2023, and then increase gradually to a long-term average of 4.5%.

### **Summary of Alternative Scenarios**

Table 10 shows the projected Cash Flow NPV from the 11 deterministic scenarios. The range of projected results is between negative \$18.993 billion and positive \$23.397 billion.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 40

Table 10: Cash Flow NPV Summaries from Alternative Scenarios

Cohort	Pinnacle ACE	Baseline	Alternative 2 –					Slower-Trend Growth	Stagflation	Next-Cycle	
			Alternative 0 – Upside (4th Percentile)	Alternative 1 – Upside (10th Percentile)	Downside (75th Percentile)	Alternative 3 – Downside (90th Percentile)	Alternative 4 – Downside (96th Percentile)			Recession	Low Oil Price
1992	-348,460	-648,848	-352,641	-418,546	-655,138	-570,573	-753,996	-640,623	-427,011	-782,392	-599,121
1993	-1,160,429	-1,641,309	-804,291	-1,223,154	-1,813,742	-2,134,182	-2,526,301	-1,616,900	-2,088,079	-1,715,591	-1,215,603
1994	-1,915,290	-3,200,205	-1,289,654	-2,570,084	-3,752,078	-4,298,142	-5,593,574	-3,011,993	-4,061,086	-3,523,820	-3,135,095
1995	-1,435,867	-3,345,439	-1,547,001	-2,756,001	-4,156,746	-3,397,446	-4,060,881	-3,946,279	-3,083,563	-4,331,916	-3,144,783
1996	-3,362,930	-7,475,774	-3,494,661	-5,585,264	-6,684,724	-8,975,147	-11,299,129	-7,921,433	-7,200,386	-8,480,563	-7,106,914
1997	-6,759,911	-10,373,901	-5,427,475	-7,214,633	-11,816,491	-13,647,901	-16,150,162	-11,056,101	-12,557,399	-12,310,906	-11,501,223
1998	-10,775,983	-20,099,777	-10,715,992	-15,319,848	-22,626,231	-24,855,094	-31,401,145	-22,602,922	-23,045,205	-21,963,464	-20,958,950
1999	-14,869,717	-28,826,012	-12,986,980	-20,520,356	-34,530,836	-33,605,057	-40,738,443	-34,243,748	-32,673,878	-32,023,370	-29,049,189
2000	-13,245,634	-23,032,688	-13,534,865	-17,741,990	-26,951,260	-28,400,348	-35,550,197	-25,527,044	-27,320,456	-28,087,539	-25,539,614
2001	-46,115,845	-67,388,042	-44,463,335	-57,188,375	-76,313,326	-80,771,952	-92,531,506	-73,919,731	-73,851,594	-71,888,651	-69,735,324
2002	-69,343,144	-100,895,733	-69,164,994	-85,293,540	-111,694,065	-120,580,632	-148,451,651	-106,005,362	-115,501,048	-105,542,859	-102,826,041
2003	-106,768,867	-148,193,793	-101,805,066	-124,279,286	-168,288,007	-186,696,949	-236,159,244	-164,155,075	-179,101,039	-162,560,228	-153,215,840
2004	-163,750,202	-238,048,860	-170,863,484	-198,489,886	-257,493,349	-284,550,253	-347,647,999	-259,551,116	-274,829,872	-252,466,322	-245,705,319
2005	-156,305,021	-232,686,022	-158,830,227	-191,443,437	-251,130,829	-277,944,590	-334,837,348	-254,350,892	-269,862,843	-253,264,668	-244,368,000
2006	-173,081,954	-253,358,029	-177,971,332	-205,876,476	-263,395,489	-285,876,199	-329,381,867	-270,924,834	-283,306,294	-260,429,798	-253,519,477
2007	-255,907,972	-375,642,778	-267,135,056	-314,879,133	-401,161,898	-418,127,046	-477,102,446	-400,804,983	-410,422,291	-392,386,355	-377,699,848
2008	-669,157,326	-961,104,788	-704,487,625	-806,818,474	-1,026,399,601	-1,118,228,901	-1,287,932,150	-1,055,968,242	-1,093,220,948	-1,031,121,486	-970,325,035
2009	-918,788,943	-1,248,854,720	-864,698,522	-1,022,694,188	-1,288,432,843	-1,458,294,733	-1,706,927,364	-1,309,796,782	-1,302,158,660	-1,351,975,548	-1,203,591,190
2010	-776,487,875	-1,030,353,623	-725,226,777	-872,259,201	-1,110,436,672	-1,202,457,193	-1,444,542,742	-1,165,445,253	-1,141,915,013	-1,073,619,344	-1,056,607,047
2011	-503,559,927	-646,768,804	-456,364,706	-510,221,708	-700,562,748	-784,796,826	-1,023,443,426	-757,363,797	-742,929,967	-703,869,292	-678,720,171
2012	-447,634,443	-673,570,725	-418,413,129	-511,350,735	-784,531,586	-942,627,918	-1,184,828,811	-765,158,901	-818,842,913	-735,319,470	-735,190,821
2013	-387,410,293	-830,504,848	-272,239,654	-441,488,478	-983,919,524	-1,397,556,865	-1,818,670,219	-968,252,571	-1,125,752,174	-963,778,965	-833,014,559
2014	1,831,341,873	1,282,736,242	1,720,389,697	1,511,848,610	1,170,356,748	849,945,230	470,857,913	1,014,790,872	1,144,369,279	1,148,872,588	1,180,487,235
2015	3,463,919,332	2,183,484,181	3,120,528,409	2,704,672,261	1,745,148,589	1,026,046,646	135,809,331	1,441,738,082	1,629,341,850	1,778,572,788	1,731,776,190
2016	4,365,037,310	2,008,339,131	3,544,681,256	2,840,556,439	1,300,300,662	300,598,503	-899,924,897	1,238,686,766	1,433,752,837	1,588,934,552	1,704,602,146
2017	4,000,572,745	908,930,608	3,167,237,022	2,046,642,819	225,137,935	-952,261,615	-2,358,464,241	110,922,546	53,765,483	472,364,889	717,148,828
2018	1,533,469,469	-743,840,439	1,214,815,815	230,712,843	-1,522,724,030	-2,320,507,071	-3,506,232,692	-1,822,895,632	-1,632,735,361	-1,310,344,833	-986,399,686
2019	2,041,597,422	-720,373,521	1,313,835,166	273,019,311	-1,470,942,484	-2,393,482,158	-3,667,822,960	-1,815,944,121	-1,686,472,996	-1,452,881,532	-1,143,332,939
2020	10,888,930,652	7,096,067,391	10,306,253,638	8,743,295,803	5,720,241,638	3,560,114,896	1,413,145,707	5,930,688,125	5,738,569,404	6,211,501,871	6,293,051,596
Total	23,396,682,771	5,109,328,875	19,905,923,534	12,935,115,293	-369,228,238	-8,607,939,515	-18,993,162,441	-1,564,277,946	-1,263,561,223	965,577,777	2,470,564,208

The Pinnacle ACE is based on the PEA, which were developed in 2019 prior to the impacts of COVID-19 on the economy. The Moody’s projections incorporate the effects of COVID-19. This has the effect of assuming an immediate economic recovery for the PEA, whereas the Moody’s scenarios project an economic recovery over a longer period. As a result, the NPV projection based on the PEA is significantly higher than the Moody’s Baseline projection.

## Stochastic Simulation

The stochastic simulation approach provides information about the probability distribution of the Cash Flow NPV of the MMI with respect to 100 different possible future economic conditions and the corresponding prepayments, claims and loss rates. The simulation provides the Cash Flow NPV associated with each one of the 100 future economic paths. The distribution of Cash Flow NPV based on these scenarios allows us to gain insights into the sensitivity of the MMI’s Cash Flow NPV to different economic conditions.

Figure 9 below shows the range of Cash Flow NPV resulting from the 100 simulated scenarios.

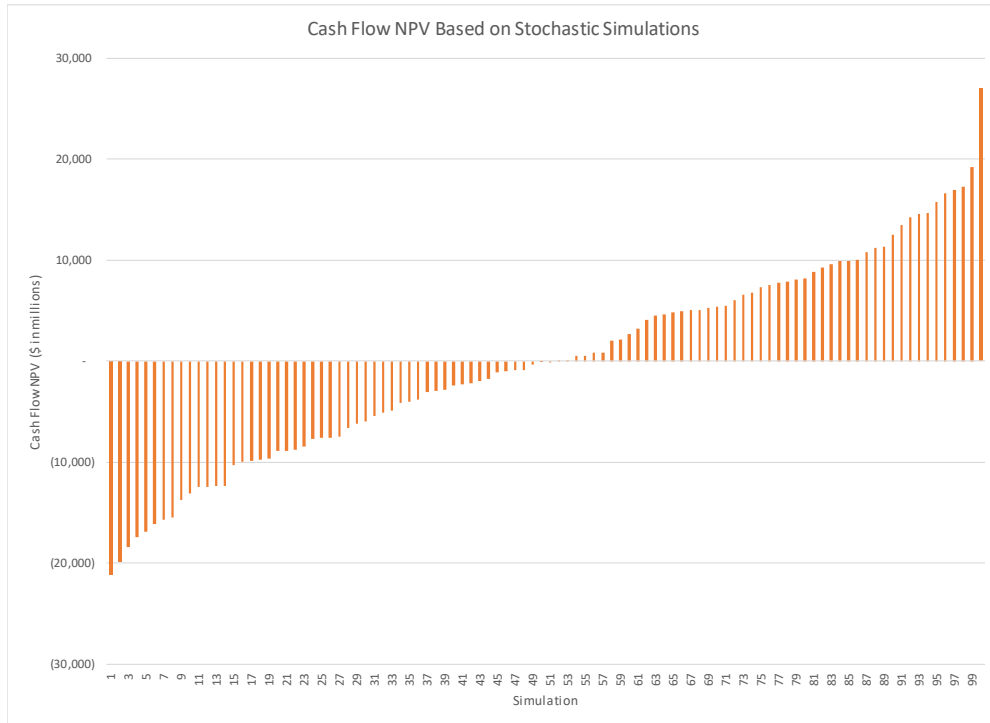


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 41

Figure 9: Stochastic Simulation Results



Based on the stochastic simulation results, the range of Cash Flow NPV estimates is negative \$21.162 billion to positive \$26.989 billion.

The range of Cash Flow NPV estimates may not include all conceivable outcomes. For example, it would not include extreme events where the contribution of such events to an expected value is not reliably estimable.

The Cash Flow NPV estimate provided by FHA to be used in the FHA Annual Report to Congress is \$10.4 billion. Based on Pinnacle’s ACE and range estimates, we conclude that the FHA estimate of Cash Flow NPV is reasonable.

## Sensitivity Tests of Economic Variables

The scenario analyses described above were conducted to estimate the distribution of the Cash Flow NPV of the MMI with different possible combinations of the interest rate and housing price movements in the future. It is also useful to understand the marginal impact of a change in each single economic factor on the Cash Flow NPV. Below, we show the sensitivity of the Cash Flow NPV with respect to the change of a single economic factor at a time. This sensitivity test is conducted for:

- Interest rates, including:
  - 10-year CMT rate
  - One-year CMT rate

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 42

- Commitment rate on 30-year fixed-rate mortgages
- Unemployment Rate

The marginal impact is measured by the change in Cash Flow NPV from the OMB Economic Assumption scenario result. These simulations change each of these variables one at a time from the baseline scenario. The changes are parallel shifts in the path of each variable in the OMB Economic Assumption scenario, where all three interest rates are shifted together and at the same magnitudes, but are kept from going negative.

Figure 10 shows the sensitivity of the Cash Flow NPV with respect to changes in future interest rates. Specifically, we applied parallel shift to the one-year CMT rate, 10-year CMT rate and the mortgage rates up and down from the Baseline scenario by 20, 50, 100 and 200 basis points. Interest rates are not allowed to be negative. The results show a positive slope, indicating that the Cash Flow NPV of the MMI is positively related to future interest rates. Higher future interest rates benefit the MMI in two ways. First, a higher future interest rate means lower refinance incentive for existing borrowers. Thus, there would be fewer prepayments, which lead to a longer stream of annual MIP revenue. Second, higher future interest rates imply that the mortgage payments of existing borrowers would be lower than that of a new mortgage with the market interest rate. The below-market mortgage payment serves as an incentive for borrowers to keep their mortgages longer and thus is a disincentive to default in order to continue to benefit from their below-market payments. A 100 basis point fall in interest rates will incur a decrease in Cash Flow NPV of \$6.291 billion, and a positive 100 basis point change in interest rates will result in an increase in Cash Flow NPV of \$3.364 billion. For the interest rate sensitivity, the range of Cash Flow NPV impacts are -0.97% to +0.31% of IIF, as shown in Figure 11.

Figure 10 also reports the sensitivity of the Cash Flow NPV with respect to the unemployment rate. The results show a negative slope, indicating that the Cash Flow NPV of the MMI is negatively related to future unemployment rates. A negative 100 basis point change in the unemployment rates will produce an increase in Cash Flow NPV of positive \$7.013 billion, and a positive 100 basis point change in the unemployment rate will result in a decrease in Cash Flow NPV of \$8.783 billion. This results from the fact that as unemployment increases, the likelihood of defaults and claims increase, and the average net loss increases as well. For the unemployment rate sensitivity, the range of Cash Flow NPV impacts are -1.18% to +0.64% of IIF, as shown in Figure 11.

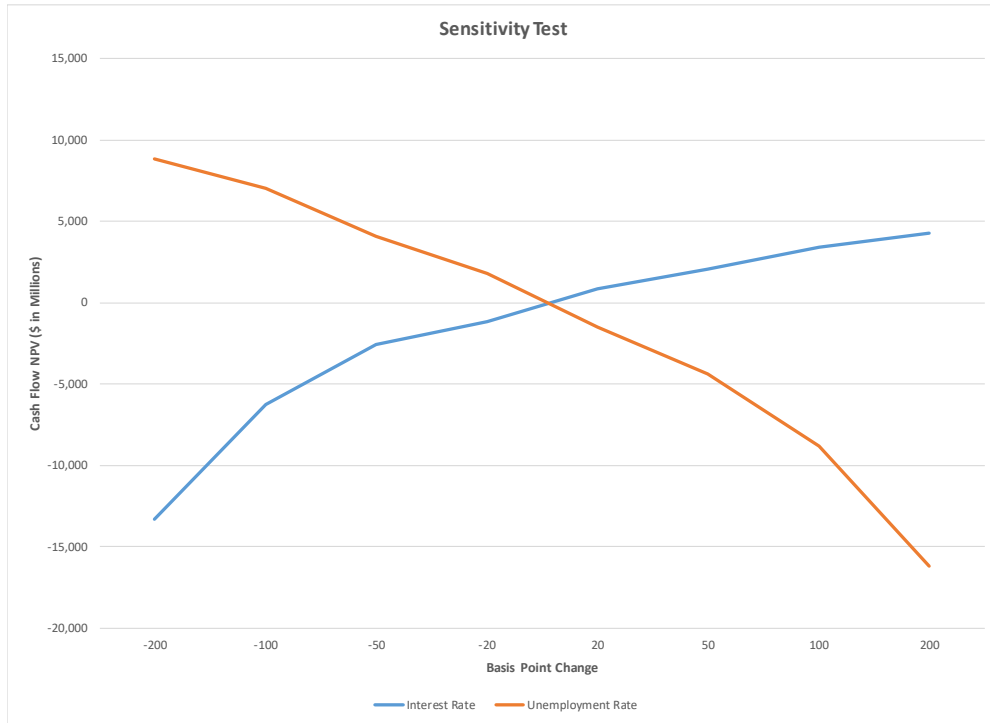
These sensitivity analyses show that Cash Flow NPV of the MMI portfolio would be significantly affected by changes in unemployment rates, while a change in interest rates has a smaller impact.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 43

Figure 10: Sensitivity Test of Selected Economic Variables

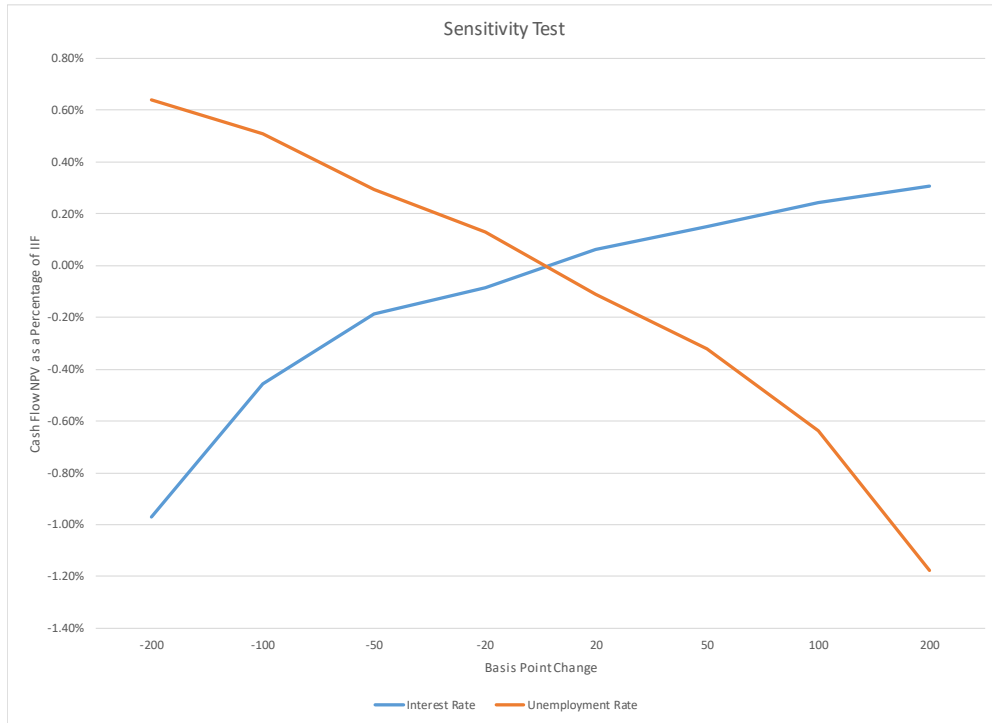


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 44

Figure 11: Sensitivity Test of Selected Economic Variables as a Percentage of IIF



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 45

### Section 4 - Characteristics of the Fiscal Year 2020 Insurance Portfolio

---

This section analyzes the characteristics of the loan portfolio insured by the MMI as of Fiscal Year 2020. This discussion covers the following three areas:

1. analysis of the volume and composition of loan types,
2. comparison of new purchase loans versus refinances and
3. the distribution of loans by loan characteristics.

This section also examines and compares the 2020 cohort with previous cohorts in order to determine how the 2020 cohort is likely to influence the future performance of the MMI.

#### Volume and Share of Mortgage Originations

FHA insured \$304 billion in single-family forward mortgages in Fiscal Year 2020, bringing the MMI's total unamortized IIF to \$1.374 trillion. This represents an increase of 41.6% above the volume insured in Fiscal Year 2019.

Table 11 shows FHA's origination count and volume by cohort. The new purchase count dropped significantly from Fiscal Year 2003 to Fiscal Year 2007, increased dramatically through Fiscal Year 2010, then returned to levels similar to those in Fiscal Years 2001 - 2003. The decline and subsequent rise were due to the Government Sponsored Enterprise (GSE)<sup>59</sup> and non-conforming lenders aggressive marketing strategies during the subprime era and their capital limitations when the housing market crashed. The capital impairment of the private mortgage insurance companies also contributed to FHA's rising volume after the crash. As the private mortgage insurance industry faced severe capital constraints, the GSEs had been unable to purchase or guarantee loans with less than a 20% down payment. FHA became the primary source of high LTV loans after Fiscal Year 2008. Private mortgage insurance companies have begun underwriting more policies during the past eight years.

The volumes show a similar pattern, for the same reasons cited above, but the volumes subsequent to the housing crisis were much higher than volumes in the early 2000s. The loan size limits were increased to the levels of the GSEs, making more loans eligible for FHA insurance. The private mortgage insurers and non-conforming lenders faced capital constraints, making FHA the only feasible channel for high LTV loans.

In Fiscal Year 2020, the new purchase counts increased by 7.8%, while the fully underwritten refinances increased by 1.1% and the streamline refinances increased by 440%. The new purchase volume increased by 15.6%, the fully underwritten refinance volume increased by 6.2% and the streamline refinance volume increased by 421%. The drop in interest rates due to the economic crisis has led to a substantial increase in refinance activity, and the implementation of shelter-in-place orders and the closing of physical offices has led to a dramatic increase in the volume of streamline refinance activity. This level of increase in refinance activity is similar to the refinance volume increase seen during the economic crisis of 2008 and 2009.

---

<sup>59</sup> Fannie Mae, Freddie Mac and the Federal Home Loan Banks

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 46

Table 11: Total Count and Volume of FHA-Insured Originations

Cohort	Count of Originations			Volume of Originations (\$ Billions)		
	New Purchase	Fully		New Purchase	Fully	
		Underwritten Refinance	Streamline Refinance		Underwritten Refinance	Streamline Refinance
1985	340,286	7	45	20.19	0.00	0.00
1986	737,217	18	7,023	45.56	0.00	0.43
1987	1,119,343	21	143,403	69.83	0.00	9.08
1988	670,354	2	42,198	40.95	0.00	2.60
1989	557,895	3	16,287	34.85	0.00	0.97
1990	689,946	127	27,516	45.25	0.01	1.69
1991	629,189	464	27,063	42.87	0.03	1.74
1992	524,680	1,889	72,353	37.19	0.13	4.88
1993	537,868	12,251	300,984	39.99	0.89	21.78
1994	652,711	16,968	549,688	51.84	1.21	38.70
1995	476,712	4,298	41,917	38.08	0.32	2.83
1996	590,486	27,110	91,107	49.85	2.22	7.44
1997	629,615	28,624	43,590	54.82	2.44	3.82
1998	742,465	54,577	174,645	68.04	5.02	17.41
1999	831,805	73,511	258,376	80.86	7.17	25.14
2000	763,063	36,640	31,843	79.40	3.83	3.04
2001	730,105	59,782	172,664	79.71	6.85	20.99
2002	787,093	87,444	293,642	91.02	10.64	34.47
2003	602,452	94,268	522,214	73.03	12.12	62.17
2004	540,314	77,985	274,123	66.84	10.28	30.51
2005	328,543	42,858	106,952	40.20	5.87	11.91
2006	293,257	72,064	34,585	37.10	10.65	3.98
2007	261,166	120,291	20,887	35.00	18.51	3.00
2008	591,326	376,522	63,733	95.37	65.78	10.65
2009	995,101	506,822	329,395	171.67	92.90	65.82
2010	1,109,164	344,877	212,871	191.60	62.61	43.29
2011	777,101	239,344	180,227	134.36	44.36	38.92
2012	733,700	176,767	274,033	124.45	31.83	56.99
2013	702,415	130,588	511,842	124.93	24.07	91.11
2014	594,998	76,315	115,038	105.72	13.19	16.31
2015	753,387	130,032	232,811	140.26	24.75	48.11
2016	879,511	165,506	213,030	171.63	32.14	41.64
2017	882,077	200,259	164,099	178.62	40.54	31.79
2018	776,275	185,815	52,510	160.89	38.10	10.06
2019	743,279	189,212	57,934	159.37	40.54	14.72
2020	800,986	191,322	312,977	184.26	43.03	76.64

Table 12 shows FHA's origination volume and market share in home purchase mortgages from Calendar Year 2001 through Calendar Year 2020.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 47

Table 12: FHA's Market Share in the Home Purchase Mortgage Market

Calendar Year	Volume of Home Sales (\$ Billions)		
	FHA	Market	FHA Share (%)
2001	89	958	9.3%
2002	82	1,096	7.5%
2003	71	1,273	5.6%
2004	53	1,306	4.1%
2005	37	1,506	2.5%
2006	36	1,401	2.5%
2007	39	1,142	3.5%
2008	129	741	17.5%
2009	185	653	28.3%
2010	167	539	31.0%
2011	129	503	25.7%
2012	127	598	21.2%
2013	119	731	16.3%
2014	107	762	14.0%
2015	154	896	17.2%
2016	176	1,049	16.7%
2017	174	1,140	15.2%
2018	158	1,207	13.1%
2019	170	1,270	13.4%
2020	135	963	14.0%

Sources: FHA Volume from FHA Data Warehouse, September 30, 2020 extract. Market volume from Mortgage Bankers Association. Calendar year 2020 includes data through September 30, 2020.

FHA's market share declined to a low of 2.5% in 2005. This trend reversed during the next several years and by Fiscal Year 2010, FHA's market share was up to 31.0%. Subsequently, the market share decreased through 2011. The FHA share has increased since 2019, and for the first nine months of Calendar Year 2020 is 14.0%.

### Originations by Location

FHA insures loans in all regions of the United States, but over half of FHA's total dollar volume is concentrated in ten states. Table 13 shows the percentage of FHA's total dollar volume originated in these ten states from Fiscal Year 2013 through Fiscal Year 2020. The states are ordered based on the dollar volume endorsed during Fiscal Year 2020.

Table 13: Percentage of Mortgage Origination Volume in the Top 10 States

State	Fiscal Year							
	2013	2014	2015	2016	2017	2018	2019	2020
California	17.1%	16.3%	18.8%	17.5%	16.8%	14.7%	14.3%	14.4%
Texas	7.1%	8.9%	7.3%	7.5%	7.6%	8.0%	8.3%	9.4%
Florida	4.8%	6.0%	6.0%	6.8%	7.5%	8.5%	8.9%	8.9%
Georgia	3.1%	3.4%	3.2%	3.7%	3.7%	4.0%	4.0%	4.1%
New Jersey	3.5%	3.1%	3.5%	3.4%	3.5%	3.5%	3.5%	3.7%
Colorado	3.5%	3.1%	3.6%	3.6%	3.5%	3.3%	3.3%	3.6%
Maryland	3.3%	3.2%	3.4%	3.3%	3.5%	3.5%	3.7%	3.5%
Arizona	2.9%	3.5%	3.7%	3.4%	3.2%	3.1%	3.2%	3.4%
New York	3.1%	2.6%	3.0%	3.1%	3.0%	3.0%	3.0%	3.0%
Washington	3.4%	3.3%	3.1%	3.1%	3.2%	3.2%	3.0%	3.0%

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 48

Currently, loans in California comprise the largest percentage of all FHA loans based on dollar volume, which is 14.4%. The percentage of loan volume in California had been decreasing from 2015 – 2019, but increased slightly in 2020. Texas is now the second largest state again in 2020, after dropping to third in 2018. The percentage of loan volume in Florida has increased by 4.1% since 2013. Florida passed Texas in 2018, but a significant surge in origination volume in Texas in 2020 has caused Florida to drop back to third place.

### **Originations by Product**

Table 14 shows that the fully underwritten 30-year FRM has comprised the majority of FHA's single-family business, representing a dollar-weighted average share of approximately 75.5% of the business over Fiscal Years 1986 - 2020. The share of total mortgages represented by 30-year FRMs began to change in the early 1990s when FHA started insuring ARMs and streamline refinancing mortgages (SRs). For the next few years, ARM and SR mortgages gradually assumed a larger share of annual loan originations and the 30-year FRM share decreased. The 1993 and 1994 cohorts recorded the lowest shares of 30-year FRMs. An opposite trend emerged from Fiscal Year 2003 through Fiscal Year 2007, in which 30-year FRM endorsements increased from 52.4% to 92.1%, while 30-year SR endorsements dropped from 36.0% to 5.1%. However, the share of 30-year FRMs in Fiscal Year 2009 through Fiscal Year 2013 dropped from 77.1% to 58.3%. From this point, the percentage increased to 91.8% in Fiscal Year 2019. In Fiscal Year 2020, the percentage of 30-year FRMs has dropped to 74.3%.

The ARM share of the portfolio, including SR ARMs, shrank dramatically from 12.0% in Fiscal Year 2005 to 1.1% in Fiscal Year 2009. It subsequently rose to 6.0% in Fiscal Year 2011, and then has decreased since then. ARMs account for only 0.04% of the endorsements in the 2020 cohort. The drop in the ARM share and the virtual non-existence in 2020 has been related to the low interest rates. The 15-year FRMs increased from 1.2% in Fiscal Year 2007 to 6.4% in Fiscal Year 2012, but have declined in the last six years and are at 0.4% in Fiscal Year 2020. The 15-year SR continues to be a minor product type in the MMI.



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 49

Table 14: Percentage of Origination Volume by Mortgage Product

Fiscal Year	Fully Underwritten Mortgages			Streamline Refinance			
	30-Year FRM	15-Year FRM	ARMs	30-Year SRs	15-Year SRs	ARMs SRs	SRs
1986	89.88	8.30	0.88	0.80	0.15	0.00	
1987	81.83	5.52	1.15	9.85	1.61	0.05	
1988	85.55	3.99	4.50	5.27	0.66	0.03	
1989	92.82	2.70	1.76	2.55	0.17	0.00	
1990	92.91	2.79	0.70	3.33	0.26	0.00	
1991	89.52	3.13	3.45	3.37	0.50	0.02	
1992	70.24	2.62	15.57	8.75	1.71	1.11	
1993	49.91	2.21	13.11	26.43	6.46	1.87	
1994	40.92	1.83	15.07	30.66	8.75	2.77	
1995	62.66	1.54	28.93	4.43	1.62	0.82	
1996	62.29	1.32	23.89	8.98	1.74	1.77	
1997	61.57	1.19	30.98	3.64	0.81	1.80	
1998	60.20	1.09	19.46	15.35	1.21	2.68	
1999	73.04	1.14	3.61	19.48	1.79	0.95	
2000	84.29	0.73	11.45	2.50	0.35	0.67	
2001	77.30	0.90	2.28	18.37	0.58	0.57	
2002	68.13	1.19	5.36	21.11	1.48	2.73	
2003	52.38	1.31	4.11	35.97	2.92	3.32	
2004	62.19	1.37	8.10	21.49	2.60	4.26	
2005	69.14	1.26	9.06	16.17	1.41	2.96	
2006	88.10	1.36	2.85	6.96	0.48	0.25	
2007	92.13	1.22	1.33	5.12	0.11	0.07	
2008	90.78	1.61	1.42	5.91	0.14	0.15	
2009	77.11	2.18	0.79	19.26	0.37	0.29	
2010	78.99	3.63	2.83	13.16	0.36	1.02	
2011	72.29	5.64	4.19	15.46	0.62	1.80	
2012	65.41	6.38	1.49	24.54	1.18	1.00	
2013	58.28	3.08	0.69	36.59	0.96	0.39	
2014	82.47	2.51	2.96	11.01	0.37	0.68	
2015	74.46	1.67	1.30	21.93	0.19	0.45	
2016	81.14	1.34	0.55	16.66	0.25	0.06	
2017	85.65	1.27	0.40	12.30	0.36	0.00	
2018	93.58	1.13	0.48	4.66	0.14	0.01	
2019	91.81	0.90	0.44	6.78	0.07	0.00	
2020	74.31	0.44	0.04	25.08	0.13	0.00	
1986-2020	75.49	2.24	3.90	16.58	0.93	0.86	

## Initial Loan to Value Distributions

Based on studies of mortgage behavior, a borrower’s equity position in the mortgaged house is one of the most important drivers of default behavior. The larger the equity position a borrower has, the greater the incentive to avoid default on the loan. The original LTV is the complement of the borrower’s equity at origination. Table 15 shows the distribution of mortgage originations by original LTV categories.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 50

Table 15: Percentage of Origination Volume by Original LTV Category

Cohort	Unknown	> 80% ≤		> 90% ≤		> 95% <	
		≤ 80%	90%	95%	97%	≥ 97	
1986	0.67%	17.98%	30.59%	27.02%	20.75%	2.99%	
1987	0.23%	18.27%	29.17%	27.97%	21.24%	3.12%	
1988	0.08%	10.15%	21.72%	33.84%	29.51%	4.70%	
1989	0.43%	7.58%	18.46%	35.95%	32.36%	5.22%	
1990	20.77%	5.90%	14.77%	28.84%	25.63%	4.08%	
1991	3.42%	5.99%	16.06%	30.32%	29.59%	14.61%	
1992	10.92%	4.52%	13.29%	24.87%	33.23%	13.17%	
1993	27.25%	3.73%	11.22%	19.57%	23.24%	15.00%	
1994	34.40%	3.56%	9.67%	16.38%	19.79%	16.20%	
1995	5.64%	3.15%	10.39%	22.94%	31.68%	26.21%	
1996	9.48%	2.97%	10.55%	23.07%	30.84%	23.09%	
1997	4.55%	3.41%	11.29%	24.94%	32.49%	23.31%	
1998	13.34%	3.62%	11.76%	23.29%	29.09%	18.89%	
1999	12.89%	4.00%	10.94%	14.77%	25.17%	32.23%	
2000	1.44%	2.66%	6.86%	7.26%	31.89%	49.89%	
2001	9.52%	3.61%	8.77%	8.63%	22.75%	46.71%	
2002	0.27%	4.67%	11.08%	9.99%	23.74%	50.25%	
2003	0.00%	6.03%	12.57%	11.73%	23.67%	45.99%	
2004	0.00%	6.56%	11.70%	10.33%	22.46%	48.94%	
2005	0.01%	6.39%	10.72%	9.06%	22.17%	51.65%	
2006	0.01%	7.12%	10.72%	14.35%	19.89%	47.91%	
2007	0.01%	7.38%	11.68%	21.24%	18.20%	41.50%	
2008	0.14%	6.18%	12.18%	24.03%	14.11%	43.35%	
2009	0.01%	4.99%	13.33%	18.82%	35.68%	27.17%	
2010	0.01%	4.81%	14.53%	12.63%	58.79%	9.24%	
2011	0.01%	4.86%	14.80%	14.07%	59.89%	6.37%	
2012	0.01%	5.50%	13.45%	20.00%	57.17%	3.87%	
2013	0.01%	5.66%	16.15%	27.25%	48.60%	2.34%	
2014	0.01%	6.07%	14.09%	12.92%	65.04%	1.86%	
2015	0.01%	6.06%	14.84%	12.95%	63.83%	2.30%	
2016	0.01%	6.86%	16.11%	11.14%	64.12%	1.75%	
2017	0.02%	7.84%	17.19%	10.08%	63.65%	1.23%	
2018	0.02%	7.80%	16.81%	8.10%	66.16%	1.11%	
2019	0.02%	7.57%	17.45%	7.76%	65.45%	1.74%	
2020	0.01%	10.51%	12.12%	12.20%	62.66%	2.50%	

The distribution among original LTV categories shifted significantly after Fiscal Year 1998. Almost half of the loans insured during from Fiscal Year 2000 to Fiscal Year 2006 had LTVs greater than or equal to 97%. This concentration in the highest risk category gradually declined during the next few years. In 2008, MMI placed a limit of 96.5% on original LTV, with no additional allowance for the financing of closing costs. During Fiscal Year 2009, 27.2% of mortgages had LTV ratios of 97% or more. In Fiscal Years 2010 - 2018, this concentration continued to decline, but has increased in Fiscal Years 2019 and 2020 to 2.5%. Since Fiscal Year 2014, over 60% of mortgages have LTV ratios between 95 to 97%.

The original LTV concentration of individual books of business affects the predictive models in two ways. First, it serves as the starting position for updating the current LTV. Holding everything else constant, loans with higher original LTVs will experience a higher current LTV in future years. Second, the original LTV itself is also included in the models to capture potential behavioral differences among borrowers who self-select into different original LTV categories. For SR loans, we use the original LTV of the prior fully underwritten mortgage, updated

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 51

for the local house price index and amortization, as a proxy for this variable.

The LTV position of cash-out refinances has also been an issue of concern for HUD. The share of cash-out refinances had increased significantly through the mid-2000's, however as the housing market weakened in the late 2000's, this was shown to have contributed to an increase in the number of foreclosures. In response, FHA decreased the LTV requirement for cash out refinances from 95% to 85% in 2009. FHA data shows that the number of cash out refinances is increasing significantly again, and as a result in 2019 decreased the LTV requirement again from 85% to 80% effective September 1, 2019.<sup>60</sup>

### **Borrower Credit History Distribution**

Credit score data has been collected from two different sources. The first source includes credit scores collected for a sample of FHA applications from Fiscal Years 1992, 1994, and 1996, and subsequently extended to loan applications during Fiscal Years 1997 - 2004. This credit score data is particularly useful because these loans have existed for many years and provide valuable historical delinquency, claim and prepayment performance information. The limitation of this data source is that it covers only a limited sample of FHA loans. In addition, the sample was originally collected for policy research purposes and represents a choice-based sample. For example, there was over-sampling of loans that defaulted early among applications over Fiscal Years 1997 - 2004.

Since May 2004, all lenders originating loans for FHA insurance have been required to report borrower credit scores directly to HUD if any credit scores were ordered as part of the underwriting process. All loans going through the FHA TOTAL scorecard have credit scores obtained electronically by the affiliated automated underwriting systems. This is the second source of credit score data. As there are no exceptions to this requirement, the credit scores collected from this source are considered to be comprehensive and unbiased. These loans have grown to be the dominant source of credit score information for our analysis.

Table 16 shows the distribution of fully underwritten FHA mortgage loans by borrower credit score categories and cohort. The distribution among credit score categories remained relatively stable for the 2005 - 2008 cohorts. For loans originated after Fiscal Year 2008, the credit score distribution showed significant improvement over the previous years. Approximately 39% of the Fiscal Year 2020 loans have credit scores above 680. Loans with credit scores below 600 are only 3.4% of the loans originated in Fiscal Year 2020, which is substantially lower than in the Fiscal Year 2007 book, where 32.8% of the loans had credit scores below 600. However, despite the distributions having improved since 2007, the trend in credit scores from 2012 through 2019 is concerning. The proportion of loans with credit scores below 600 has been increasing slowly from 2012 through 2019, rising from 0.6% to 5.2%. Also, the proportion of loans with credit scores above 680 has decreased from 2016 through 2019 from 46.0% to 34.5%. In Fiscal Year 2020, the percentage of loans with credit scores below 600 decreased to 3.4%, and the percentage with scores of 680 or higher increased to 38.5%. If the previous deterioration in credit scores continues, it could result in worse default and loss experience, and thus

---

<sup>60</sup> Mortgagee Letter 2019-11, August 1, 2019: Maximum Loan-To-Value and Combined Loan-To-Value Percentages for Cash-out Refinance Mortgages.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 52

would contribute negatively to the economic value of the MMI for the more recent cohorts.

In the predictive models, we also controlled for missing and uncollected credit scores. In Table 16, the category “Missing” refers to loans with insufficient borrower credit history to generate a credit score, and the category “Not Collected” refers to loans where no attempt was made to obtain the credit score for some of the Fiscal Year 2004 and earlier loans. These categories have been combined in the table. Since credit scores became a requirement for fully underwritten loans, the Missing/Not Collected category has been a negligible percentage of the overall book.

Table 16: Percentage of Origination Volume by Credit Score for Fully Underwritten Loans

Cohort	Missing / Not Collected						
	Collected	300-499	500-559	560-599	600-639	640-679	680-850
1997	100.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%
1998	100.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%
1999	100.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%
2000	100.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%
2001	100.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%
2002	100.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%
2003	99.96%	0.00%	0.00%	0.01%	0.01%	0.01%	0.01%
2004	75.76%	0.20%	2.20%	4.19%	6.21%	5.23%	6.22%
2005	6.86%	0.90%	9.24%	16.70%	24.18%	19.89%	22.22%
2006	4.81%	0.94%	8.75%	16.61%	24.50%	20.70%	23.69%
2007	4.18%	1.53%	11.76%	19.47%	25.09%	18.93%	19.04%
2008	2.21%	0.83%	6.93%	14.09%	24.21%	22.71%	29.03%
2009	1.03%	0.05%	1.13%	5.10%	18.01%	24.83%	49.86%
2010	1.06%	0.01%	0.16%	0.86%	12.39%	25.02%	60.51%
2011	0.89%	0.00%	0.07%	0.48%	8.40%	27.11%	63.05%
2012	0.52%	0.00%	0.09%	0.52%	8.23%	30.77%	59.87%
2013	0.44%	0.00%	0.08%	0.43%	6.50%	36.42%	56.14%
2014	0.27%	0.00%	0.08%	0.96%	11.27%	41.52%	45.90%
2015	0.25%	0.00%	0.11%	1.58%	14.55%	37.88%	45.63%
2016	0.21%	0.00%	0.11%	1.81%	15.48%	36.41%	45.97%
2017	0.20%	0.00%	0.19%	2.52%	17.67%	36.10%	43.31%
2018	0.17%	0.00%	0.40%	3.90%	20.96%	36.88%	37.69%
2019	0.14%	0.00%	0.53%	4.72%	22.54%	37.63%	34.45%
2020	0.08%	0.00%	0.31%	3.13%	18.84%	39.14%	38.50%

## Initial Relative Loan Size Distribution

The relative loan size variable is computed by comparing the mortgage origination amount with the average loan size of all FHA-insured loans originated within the same period and in the same state. Empirical results show that this variable is very significant in predicting prepayments.

FHA experience indicates that larger loans tend to perform better compared with smaller loans in the same geographical area, all else being equal. Larger loans incur claims at a lower probability and in those cases where a claim occurs, loss severity tends to be lower. Prior to the increase in FHA’s loan limits in Fiscal Year 2008, houses securing larger FHA loans tended to fall into the average house price range within their surrounding areas. Since this market is relatively liquid and there are a relatively large number of similar-quality homes in the area, the house price volatility of these houses tends to be relatively low in comparison to the house price volatility of extremely low- and high-priced houses. With the increased FHA loan size limit, FHA started

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 53

endorsements of higher-priced houses after Fiscal Year 2008.

Table 17 shows the percentage of new fully underwritten mortgage originations within each relative loan size category. The distribution has been reasonably stable over time with the largest share in the 75-to-125 percent of area average loan size categories. However, since Fiscal Year 2000, there has been a steady increase in the dispersion among loan size categories. The proportion in the highest loan size category increased from 11.1% in Fiscal Year 2001 to 25.1% in Fiscal Year 2011, but has decreased since then to 16.3% in 2020. On the other hand, the share in lowest loan size category also increased from 1.8% percent in Fiscal Year 2004 to 5.2% in Fiscal Year 2012, and has since decreased to 2.8% in Fiscal Year 2020. The increase in both the highest and lowest loan size categories demonstrated the penetration of FHA products into high-balance loans and the resurgence of the low-balance loan, but this penetration has decreased slightly since 2011.

Table 17: Percentage of Origination Count by Relative Loan Size

Cohort	0-50% of Average Loan Size	50-75% of Average Loan Size	75-100% of Average Loan Size	100-125% of Average Loan Size	125-150% of Average Loan Size	>150% of Average Loan Size
1985	1.75%	10.64%	26.03%	34.72%	21.12%	5.75%
1986	1.37%	10.11%	27.00%	38.76%	18.86%	3.91%
1987	1.17%	9.80%	26.62%	38.84%	19.89%	3.67%
1988	1.49%	10.72%	25.59%	35.52%	20.45%	6.22%
1989	1.73%	11.18%	25.34%	32.46%	21.16%	8.12%
1990	1.76%	11.33%	25.08%	31.18%	21.08%	9.58%
1991	1.84%	11.42%	25.14%	30.04%	21.63%	9.93%
1992	1.72%	11.09%	25.35%	31.30%	21.60%	8.95%
1993	1.50%	10.62%	25.57%	31.92%	22.03%	8.37%
1994	1.19%	9.26%	22.81%	30.13%	24.62%	11.98%
1995	1.61%	11.45%	24.67%	30.38%	22.47%	9.41%
1996	1.61%	11.32%	24.71%	31.28%	22.93%	8.15%
1997	1.75%	11.89%	24.98%	31.66%	21.94%	7.78%
1998	1.64%	11.15%	24.54%	32.83%	22.18%	7.66%
1999	1.80%	11.37%	24.47%	30.74%	20.80%	10.83%
2000	2.02%	11.73%	24.44%	29.27%	20.36%	12.18%
2001	2.22%	12.12%	25.69%	29.52%	19.34%	11.11%
2002	2.06%	11.14%	24.59%	29.61%	19.97%	12.64%
2003	1.81%	10.35%	23.49%	29.85%	20.81%	13.69%
2004	1.79%	10.06%	22.41%	28.83%	21.57%	15.34%
2005	1.92%	10.94%	22.92%	28.28%	21.07%	14.89%
2006	2.17%	11.94%	23.10%	28.04%	20.11%	14.64%
2007	2.49%	12.58%	23.37%	27.55%	19.48%	14.52%
2008	2.80%	12.99%	24.33%	25.44%	17.01%	17.42%
2009	3.94%	14.58%	23.42%	21.70%	15.10%	21.25%
2010	4.39%	15.01%	22.50%	20.33%	14.25%	23.52%
2011	5.06%	15.39%	21.34%	19.31%	13.78%	25.12%
2012	5.18%	15.63%	21.81%	19.71%	13.85%	23.83%
2013	4.10%	13.80%	21.06%	20.10%	14.72%	26.23%
2014	3.59%	13.18%	21.48%	20.91%	15.50%	25.34%
2015	3.85%	13.88%	23.01%	21.74%	15.65%	21.87%
2016	3.39%	12.93%	22.76%	22.41%	16.66%	21.86%
2017	3.14%	12.46%	22.90%	23.32%	17.44%	20.74%
2018	3.11%	12.53%	23.33%	24.34%	17.10%	19.59%
2019	3.19%	12.75%	24.23%	24.97%	16.92%	17.94%
2020	2.82%	12.32%	24.84%	25.98%	17.76%	16.28%

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 54

### Initial Contract Interest Rate

Table 18 shows the average mortgage contract rate by mortgage type since Fiscal Year 1997. Prior to Fiscal Year 2020, average contract rates in Fiscal Year 2013 were the lowest of this entire time period. Rates had been higher since 2013, but have decreased significantly in Fiscal Year 2020 by almost one full percentage point. Interest rates for 30-year SRs are at the lowest level since 1997, which is one of the reasons for the significant surge in refinance activity in 2020.

In general, an FRM with a lower initial contract rate tends to prepay at a slower speed. As interest rates are projected to rise, the prepayment rates of the recent originations are likely to remain low. As these loans will have longer durations, as reflected in our predictive models, more insurance premium income will be generated, thus tending to improve the economic value of these recent books with historically low contract rates.

Also, a mortgage with a contract rate lower than the market rate tends to experience a lower probability of default because the borrower has the incentive to keep the below-market rate mortgage longer even when experiencing some negative equity. This tendency is reflected in our predictive models. As mortgage rates rise in the future, the recent low-interest-rate books are projected to incur fewer defaults and claims. This also tends to improve the economic value.

*Table 18: Average Contract Interest Rate by Loan Type (Percent)*

Fiscal Year	30-Year	15-Year	30-Year		15-Year		Book of Business
	FRM	FRM	ARMs	SRs	SRs	ARMs SRs	
1997	8.01	7.77	6.60	8.30	8.04	6.86	7.62
1998	7.42	7.23	6.25	7.62	7.24	6.54	7.22
1999	7.21	6.94	5.96	7.20	6.91	6.11	7.15
2000	8.22	7.95	6.87	8.07	7.81	6.15	8.07
2001	7.69	7.25	6.57	7.44	6.89	6.22	7.61
2002	7.07	6.60	5.37	7.02	6.46	5.38	6.92
2003	6.21	5.62	4.59	6.07	5.55	4.56	6.02
2004	6.08	5.52	4.41	5.92	5.46	4.34	5.84
2005	5.94	5.64	4.78	5.85	5.65	4.67	5.80
2006	6.29	6.14	5.36	6.10	6.02	5.03	6.25
2007	6.51	6.40	5.62	6.38	6.22	5.59	6.49
2008	6.33	5.95	5.39	6.09	5.64	5.33	6.30
2009	5.62	5.14	5.05	5.26	4.81	4.54	5.53
2010	5.14	4.62	3.98	5.13	4.65	4.28	5.08
2011	4.65	4.16	3.51	4.63	4.16	3.69	4.57
2012	3.98	3.46	3.14	3.98	3.53	3.38	3.93
2013	3.62	3.16	2.82	3.71	3.36	2.86	3.63
2014	4.30	3.71	3.31	4.51	3.91	3.39	4.28
2015	4.03	3.47	3.26	3.99	3.69	3.36	4.00
2016	3.91	3.40	3.23	3.87	3.53	3.35	3.89
2017	4.03	3.50	3.18	3.75	3.59	3.02	3.98
2018	4.54	3.87	3.51	4.08	4.03	3.49	4.50
2019	4.68	4.15	4.00	4.23	4.44	4.02	4.64
2020	3.64	3.50	3.47	3.51	3.44	3.50	3.61

### Source of Down Payment Assistance

Table 19 shows the distribution of annual loan endorsements by source of down payment assistance. Secondary loans provided by governments were included in the category of down payment assistance, and typically these

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 55

were local government units.

Starting in Fiscal Year 2000, there was a rapid increase in the share of loans with gift letters from non-profit, religious, or community institutions. Home sellers contributed a large share of these funds to the non-profit organizations, which subsequently provided the gift to the buyers of the same properties to fulfill the down payment requirements. This concentration increased to over 20% in the 2005 - 2007 cohorts. FHA effectively terminated seller-financed down payment assistance on October 1, 2008 because of the high losses associated with these loans. The share of loans with this type of assistance declined to negligible amounts after Fiscal Year 2008.

From 2008 to 2018, the percentage of loans with down payment assistance from a relative had increased from 6.8% to 21.7%. In Fiscal Year 2020, this percentage has decreased to 15.8%. Also, the share of loans with government down payment assistance increased from 2013 to 2016, but has decreased since then.

Table 19: Percentage of Down payment assist Loan Counts by Source

Cohort	No Gift	Relative	Non-Profit, Religious or Community	
			Community	Government
1998	76.81%	22.76%	0.20%	0.23%
1999	81.69%	17.11%	0.53%	0.68%
2000	77.56%	18.97%	1.69%	1.78%
2001	83.35%	11.72%	3.75%	1.17%
2002	83.21%	9.32%	6.29%	1.18%
2003	81.92%	7.61%	9.33%	1.13%
2004	71.69%	9.75%	16.95%	1.61%
2005	64.64%	9.91%	22.96%	2.48%
2006	64.13%	9.44%	23.04%	3.39%
2007	68.25%	7.66%	21.27%	2.81%
2008	74.46%	6.82%	17.38%	1.33%
2009	86.54%	10.34%	2.70%	0.42%
2010	83.99%	15.42%	0.09%	0.51%
2011	85.25%	13.91%	0.12%	0.72%
2012	85.76%	13.44%	0.13%	0.68%
2013	86.89%	12.33%	0.09%	0.70%
2014	77.73%	20.66%	0.29%	1.32%
2015	79.44%	17.88%	0.72%	1.95%
2016	77.31%	19.26%	0.91%	2.53%
2017	77.40%	19.70%	0.74%	2.16%
2018	76.34%	21.71%	0.41%	1.54%
2019	78.19%	20.58%	0.22%	1.01%
2020	82.93%	15.80%	0.19%	1.09%

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 56

## Section 5 – Summary of Methodology

---

This section provides an overview of the analytical approach used in this analysis.

### Data Sources

In our analysis, we have relied on data from FHA, Moody's and the OMB.

From FHA, we have received the following data:

1. Claims 601 Case Data: used for the cash entry from note sales
2. IDB: core case data; this table is derived based on fields from IDB\_1, IDB\_2, and the Decision\_FICO\_Score (one file each for 1975 – 2020)
3. Lossmit Costs: derived table based on the Loss Mitigation table and IDB\_1, used to obtain mitigation claim amounts
4. Sams case record: used to determine the status of the conveyances, the capital income/expense amounts, the sales and real estate owned (REO) expenses and sales proceeds to FHA, where applicable
5. SFDW Default History: used to create period information related to default histories
6. Fannie FICO pre2004: used for supplemental credit data
7. Current Status: table displaying the current status of each loan
8. SFDW Dictionary for Pinnacle: data dictionary for the tables provided by FHA

From Moody's, we have received the following data elements:

1. Historical Economic Data
2. Baseline Economic Scenario Projections
3. Modified Economic Scenario Projections

From OMB, we have received the Economic Assumptions for the 2021 Budget.

The economic data that is included in the analysis is shown below:

1. HPI
2. Mortgage rates
3. Treasury rates
4. Unemployment rates
5. GDP
6. Consumer Confidence Index
7. Small Business Optimism Index

### Data Processing – Mortgage Level Modeling (Appendix A)

Starting with the raw data, Pinnacle processed the data to create datasets for developing the mortgage level transition and loss severity models. The first step in preparing the data for analysis was the processing of the



## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 57

economic data. Historical economic data was imported by quarter, additional data elements were derived, and data was joined to the FHA mortgage data.

Once the economic data was prepared, the core data processing occurred. We used mortgage-level data to reconstruct quarterly mortgage-event histories by relating mortgage origination information to other data reflecting events that occurred over the history of the mortgage. In the process of creating quarterly event histories, each mortgage contributed an observed transition for every quarter from origination up to and including the period of mortgage termination, or until the third quarter of Fiscal Year 2020 if the mortgage remained active.

### **Data Reconciliation**

To reconcile the data processed by Pinnacle with the data provided by FHA, Pinnacle compared summaries of key data elements with summaries provided by FHA. The summaries for the number of active mortgages, IIF, number of 90-day delinquencies, and the number of claims to date are shown in the following tables.

The following tables are based on data as of September 30, 2020.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 58

Table 20: Data Reconciliation - Number of Active Loans

Number of Active Loans				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	10,156	10,123	(33)	0%
1993	16,952	16,877	(75)	0%
1994	25,046	24,937	(109)	0%
1995	12,676	12,645	(31)	0%
1996	20,933	20,901	(32)	0%
1997	22,747	22,706	(41)	0%
1998	35,772	35,651	(121)	0%
1999	45,228	45,053	(175)	0%
2000	25,416	25,270	(146)	-1%
2001	44,185	44,042	(143)	0%
2002	64,460	64,036	(424)	-1%
2003	93,021	92,214	(807)	-1%
2004	116,133	114,992	(1,141)	-1%
2005	84,556	83,825	(731)	-1%
2006	68,570	68,470	(100)	0%
2007	65,537	65,531	(6)	0%
2008	152,662	152,651	(11)	0%
2009	331,410	331,399	(11)	0%
2010	414,277	414,261	(16)	0%
2011	333,745	333,745	0	0%
2012	417,660	417,660	0	0%
2013	586,382	586,382	0	0%
2014	269,885	269,885	0	0%
2015	488,122	488,122	0	0%
2016	707,384	707,384	0	0%
2017	800,804	800,804	0	0%
2018	680,155	680,155	0	0%
2019	713,490	713,490	0	0%
2020	1,252,492	1,252,492	0	0%
<b>Total</b>	<b>7,899,856</b>	<b>7,895,703</b>	<b>(4,153)</b>	<b>0%</b>

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 59

Table 21: Data Reconciliation - Insurance in Force

Insurance in Force (\$M)				
= Original Loan Amount on Active Loans				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	632,737,045	630,175,704	(2,561,341)	0%
1993	1,128,051,113	1,122,662,281	(5,388,832)	0%
1994	1,693,390,286	1,685,534,003	(7,856,283)	0%
1995	804,863,327	802,945,779	(1,917,548)	0%
1996	1,383,145,048	1,381,194,526	(1,950,522)	0%
1997	1,538,664,165	1,536,111,497	(2,552,668)	0%
1998	2,622,750,438	2,614,282,837	(8,467,601)	0%
1999	3,477,643,199	3,465,625,793	(12,017,406)	0%
2000	1,928,948,049	1,917,580,035	(11,368,014)	-1%
2001	3,784,816,154	3,774,058,838	(10,757,316)	0%
2002	5,986,934,870	5,952,126,416	(34,808,454)	-1%
2003	9,760,137,449	9,687,453,499	(72,683,950)	-1%
2004	12,226,545,193	12,130,291,064	(96,254,129)	-1%
2005	9,134,628,096	9,072,357,217	(62,270,879)	-1%
2006	7,782,880,704	7,773,600,757	(9,279,947)	0%
2007	8,006,143,056	8,005,729,158	(413,898)	0%
2008	21,311,279,293	21,310,167,626	(1,111,667)	0%
2009	50,244,615,492	50,243,397,129	(1,218,363)	0%
2010	61,134,262,611	61,132,626,092	(1,636,519)	0%
2011	50,658,951,615	50,658,951,615	0	0%
2012	65,322,259,638	65,322,259,638	0	0%
2013	94,545,227,961	94,545,227,961	0	0%
2014	37,222,658,900	37,222,658,900	0	0%
2015	80,619,068,501	80,619,068,501	0	0%
2016	125,913,138,455	125,913,138,455	0	0%
2017	150,269,903,430	150,269,903,430	0	0%
2018	129,528,758,809	129,528,758,809	0	0%
2019	144,553,787,700	144,553,787,700	0	0%
2020	289,995,649,771	289,995,649,771	0	0%
Total	1,373,211,840,368	1,372,867,325,031	(344,515,337)	0%

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 60

Table 22: Data Reconciliation - Number of 90 Day Delinquencies

Number of 90 Day Delinquencies				
= Current Number of 90 Day Delinquencies				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	557	557	0	0%
1993	871	873	2	0%
1994	1,446	1,447	1	0%
1995	1,028	1,029	1	0%
1996	1,892	1,894	2	0%
1997	2,101	2,101	0	0%
1998	3,339	3,339	0	0%
1999	4,689	4,690	1	0%
2000	3,206	3,208	2	0%
2001	5,153	5,158	5	0%
2002	7,252	7,253	1	0%
2003	10,201	10,210	9	0%
2004	14,173	14,185	12	0%
2005	11,566	11,576	10	0%
2006	10,204	10,207	3	0%
2007	10,741	10,747	6	0%
2008	26,057	26,075	18	0%
2009	43,241	43,280	39	0%
2010	46,407	46,438	31	0%
2011	35,032	35,045	13	0%
2012	40,869	40,894	25	0%
2013	52,392	52,426	34	0%
2014	34,410	34,427	17	0%
2015	61,439	61,468	29	0%
2016	88,411	88,447	36	0%
2017	105,748	105,792	44	0%
2018	102,729	102,793	64	0%
2019	104,098	104,175	77	0%
2020	71,257	71,352	95	0%
Total	900,509	901,086	577	0%

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 61

Table 23: Data Reconciliation - Number of Claims to Date

Number of Claims To Date				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	36,778	36,778	0	0%
1993	52,278	52,276	(2)	0%
1994	65,920	65,919	(1)	0%
1995	44,678	44,678	0	0%
1996	63,473	63,466	(7)	0%
1997	59,869	59,860	(9)	0%
1998	67,469	67,459	(10)	0%
1999	84,217	84,204	(13)	0%
2000	71,330	71,321	(9)	0%
2001	85,345	85,335	(10)	0%
2002	90,497	90,476	(21)	0%
2003	91,202	91,188	(14)	0%
2004	115,820	115,798	(22)	0%
2005	92,054	92,045	(9)	0%
2006	94,239	94,238	(1)	0%
2007	106,321	106,321	0	0%
2008	223,769	223,768	(1)	0%
2009	225,483	225,483	0	0%
2010	115,004	115,004	0	0%
2011	47,109	47,109	0	0%
2012	29,148	29,148	0	0%
2013	26,684	26,684	0	0%
2014	15,349	15,349	0	0%
2015	14,681	14,681	0	0%
2016	12,201	12,201	0	0%
2017	8,224	8,224	0	0%
2018	3,678	3,678	0	0%
2019	533	533	0	0%
2020	5	5	0	0%
<b>Total</b>	<b>1,943,353</b>	<b>1,943,224</b>	<b>(129)</b>	<b>0%</b>

**Specification of Mortgage Transition Models (Appendix B)**

The purpose of the transition predictive models is to estimate the likelihood of future occurrences of claim and prepayment terminations for FHA forward mortgages in the MMI portfolio. The models are used to project future outstanding balances, cash flows, and ultimately the Cash Flow NPV.

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 62

The predictive models reflect the fact that mortgage borrowers possess two mutually exclusive options to terminate the mortgage, one to prepay the mortgage and the other to default by permanently ceasing payment. From FHA's point of view, prepayment and claim events are the corresponding outcomes of "competing risks" in the sense that they are mutually exclusive, and realization of one of these events precludes the other.

Prepayment means cessation of cash inflows from MIP, but at the same time eliminates any chance of incurring claim losses. Conversely, termination through foreclosure means claim costs are incurred and MIP inflows cease, but uncertainty about the possibility and timing of prepayment is eliminated.

The models developed for this analysis also include additional transitions. These include the transition from current to 90 days or more delinquent (Default), cures from Default separated into cures by mortgage modification, and self-cures with no modification or with "light" modifications. We track the post-cure behavior of modified mortgages and self-cured mortgages separately with modification-related variables, namely a modification flag and the payment reduction ratio. We also track the status of mortgages post-default by including a prior default flag and the time since the most recent default.

We model five possible transitions from a mortgage in current status: remain current, default (become 90 or more days delinquent), prepay by streamlined refinance (SR), other prepayments or self-cure. (There is also one additional transition possible – cure with a modification. This transition rarely occurs for a mortgage in Current status, but most often occurs with a mortgage in Default Status. Therefore, we have include these transitions in the Default transition model development). Given that these are mutually exclusive outcomes, the sum of the probabilities for all possible transitions is 100%. For a mortgage in default status at the beginning of a particular time period, the five possible transitions are that it may be prepaid, transition into a claim, self-cure, cure with a mortgage modification, or remain in default.

For this Actuarial Review, we have separately identified claims in default and in COVID-19 forbearance. Borrowers who experienced an adverse impact on their ability to make on-time mortgage payments due to the COVID-19 pandemic are eligible for forbearance for an initial period of six months, and this initial period can be extended by up to six additional months. All borrowers are eligible for COVID-19 forbearance; therefore, if a borrower is granted this forbearance, it will likely delay the transition of the mortgage in default to a subsequent status. Therefore, we develop additional transition assumptions for COVID-19 forbearances to reflect the potential slow-down in resolution over the next twelve months. Over the projected period that loans can be in a COVID-19 forbearance, Pinnacle projects that a portion of the loans eligible for loss mitigation will exit forbearance as either a loss mitigation claim, a loan still in default or a payoff. For loans that are in COVID-19 forbearance but not eligible for loss mitigation, Pinnacle projects that a portion of these loans will exit forbearance as a default loan. As loans can enter COVID-19 forbearance through the end of 2020, this adjustment will persist into Fiscal Year 2021.

In the 2017 and 2018 Actuarial Reviews, Pinnacle used multinomial logistic models to estimate the probability of transition for current and default mortgages. In the 2019 Actuarial Review, we used binomial logistic models to predict each transition separately, and once all the binomial models were completed, we adjusted the binomial probabilities to reflect the multinomial nature of the transitions. The primary reason for making this change was

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 63

that it allowed us to better model each transition using the independent variables that were significant for that transition. The multinomial structure used in the 2017 and 2018 Actuarial Reviews did not allow for the use of variables just for individual transitions – (i.e., if a variable was included in the model it applied to all transitions). This resulted in over-specification of the transition models, as there are some independent variables that were not significant for some transitions. To address this, Pinnacle used binomial models for each transition and applied an adjustment to reflect the multinomial nature of the process. Pinnacle has continued the use of binomial models for this Actuarial Review.

Pinnacle investigated the use of Multinomial Discrete Choice (MDC) models for this analysis. MDC models allow all transitions to be modeled simultaneously, and also allows for the use of independent variables only for specific transitions. Pinnacle compared the MDC approach to the binomial logistic approach, and concluded that the two approaches produce identical results. We also observed that the MDC approach took significantly longer to complete as it was more computationally intensive. Because the results of the two methods were identical and the binomial logistic models ran more efficiently, we decided to continue with the binomial logistic approach with the multinomial adjustment.

There are several benefits to using a multinomial logistic model structure. First, it ensures that the event probabilities sum to unity. This means that, at any point in time, a mortgage must experience only one of the possible transitions over the next period. Second, the possible values of each probability are constrained to be between zero and one. Third, as the probability of one transition type increases, the probabilities of the others are automatically reduced, reflecting the competing-risk nature among the transition events. Finally, it allows the conditional termination rates using mortgage-level data to be estimated. With mortgage-level observations, the possible outcomes at each point in time are either 0 (the event did not happen), or 1 (the event happened).

In the 2017 and 2018 Actuarial Reviews, we developed the predictive models based on estimation samples of the data for the Current Status transition models with ending condition of Current, Prepayment of Streamline Refinance. For Default Status transition models, we sampled data with the ending condition of Default. With this analysis, for the transition models with the initial condition of C for the FRM30 non-SR product, we used a random sample of 50% of the data. For all other products, we used 100% of the data in the model development. For Default transition models, we used 100% of the data in the model development for all products.

### **Loss Severity Model (Appendix C)**

FHA incurs a loss from a mortgage claim event. This loss amount depends on many factors, including the disposition channel. In practice, foreclosed properties generally have higher severity compared to pre-foreclosure-sales (PFS). Foreclosure mortgages can be further separated into REO and Claims Without Conveyance of Title (CWCOT). We have developed multiple models to predict loss severity: models to predict whether the property is disposed by PFS, REO or CWCOT, and separate loss severity models for PFS, REO and CWCOT cases. The loss severity models capture characteristics of the mortgage, the collateral, the borrower, and the housing market environment when a claim occurs. The claim disposition selection model was estimated using multinomial logistic regression, while Generalized Linear Models (GLM) were developed for loss severity

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 64

models.

In addition to the loss severity models, we have also developed separate models to project the frequency of loss mitigation claims and the severity associated with these claims.

All loans granted a COVID-19 forbearance must be evaluated for eligibility for a partial claim and/or loan modification. Borrowers who were current or less than 30 days past due as of March 1, 2020 must be evaluated for COVID-19 loss mitigation options. Once a loan is projected to exit COVID-19 forbearance, Pinnacle will project the transition path of the loan based on the percentages estimated from forbearance exits that have occurred in 2020. If the loan is projected to be a COVID-19 loss mitigation claim, the severity will be estimated based on the loss mitigation severity model.

### **Cash Flow Projections (Appendix E)**

After developing the transition and severity predictive models, we use this information to project future cash flows. The cash flow model includes the calculation of five types of cash flows:

1. Upfront MIP
2. Annual MIP
3. Claim payments
4. Loss mitigation related expenses
5. Premium refunds

The federal credit subsidy present value conversion factors provided by OMB are used to discount future cash flows to determine their present value as of the end of Fiscal Year 2020.

FHA executed note sales in November 2015 and September 2016. Based on information provided by HUD, there are no current planned or pending note sales. Therefore, we have not projected any future note sales in our analysis.

We have calculated the Cash Flow NPV based on multiple deterministic economic scenario paths. The ACE projection is based on the OMB Economic Assumptions, and the variation in the estimate is calculated in part by using ten alternative economic projection scenarios from Moody's. These scenarios include both more favorable than expected and less favorable than expected economic assumptions. The resulting Cash Flow NPV is then calculated based on these varying assumptions. The following are the economic variables that drive the variation in the MMI Cash Flow NPV:

- One-year CMT rates
- Three-year CMT rates
- Five-year CMT rates
- 10-year CMT rates
- 30-year CMT rates



## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 65

- 30-year Fixed Rate Mortgage (FRM) rates
- FHFA national purchase-only HPI
- Unemployment rates by state
- Change in unemployment rate
- One-year GDP ratio

# **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 66

## **Appendices**

---

- A. Data - Sources, Processing and Reconciliation
- B. Transition Models
- C. Loss Severity Models
- D. Economic Scenarios
- E. Cash Flow Analysis
- F. Review of HUD Analysis of Economic Net Worth, Comparison of HUD and Pinnacle Models, and Assessment of Vulnerabilities
- G. Summary of Historical and Projected Claim Rates, Non-Claim Termination Rates and Loss Severities

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 67

## Appendix A: Data – Sources, Processing and Reconciliation

---

### Data Sources

In our analysis, we have relied on data from FHA, Moody's and the OMB.

From FHA, we have received the following data:

1. Claims 601 Case Data: used for the cash entry from note sales
2. IDB: core case data; this table is derived based on fields from IDB\_1, IDB\_2, and the Decision\_FICO\_Score (one file each for 1975 – 2020)
3. Lossmit Costs: derived table based on the Loss Mitigation table and IDB\_1, used to obtain mitigation claim amounts
4. Sams case record: used to determine the status of the conveyances, the capital income/expense amounts, the sales and REO expenses, and sales proceeds to FHA, where applicable
5. SFDW Default History: used to create period information related to default histories
6. Fannie FICO pre2004: used for supplemental credit data
7. Current Status: table displaying the current status of each loan
8. SFDW Dictionary for Pinnacle: data dictionary for the tables provided by FHA

From Moody's, we have received the following data elements:

1. Historical Economic Data
2. Baseline Economic Scenario Projections
3. Modified Economic Scenario Projections

From OMB, we have received the Economic Assumptions for the 2021 Budget.

The economic data that is included in the analysis is shown below:

1. HPI
2. Mortgage rates
3. Treasury rates
4. Unemployment rates
5. GDP
6. Consumer Confidence Index
7. Small Business Optimism Index

### Data Processing – Mortgage Level Modeling

Starting with the raw data, Pinnacle processed the data to create datasets for developing the mortgage level transition and loss severity models. The first step in preparing the data for analysis was the processing of the economic data. Historical economic data was imported by quarter, additional data elements were derived, and data was joined to the FHA mortgage data.

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 68

Once the economic data was prepared, the core data processing occurred. We used mortgage-level data to reconstruct quarterly mortgage-event histories by relating mortgage origination information to other data reflecting events that occurred over the history of the mortgage. In the process of creating quarterly event histories, each mortgage contributed an observed transition for every quarter from origination up to and including the period of mortgage termination, or until the third quarter of Fiscal Year 2020, if the mortgage remained active.

### **Data Reconciliation**

To reconcile the data processed by Pinnacle with the data provided by FHA, Pinnacle compared summaries of key data elements with summaries provided by FHA. The summaries for the number of active mortgages, IIF, number of 90-day delinquencies, and the number of claims to date are shown in the following tables.

The following tables are based on data as of September 30, 2020, as this was the data used to develop the transition and net loss models.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 69

Table 24: Data Reconciliation - Number of Active Loans

Number of Active Loans				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	10,156	10,123	(33)	0%
1993	16,952	16,877	(75)	0%
1994	25,046	24,937	(109)	0%
1995	12,676	12,645	(31)	0%
1996	20,933	20,901	(32)	0%
1997	22,747	22,706	(41)	0%
1998	35,772	35,651	(121)	0%
1999	45,228	45,053	(175)	0%
2000	25,416	25,270	(146)	-1%
2001	44,185	44,042	(143)	0%
2002	64,460	64,036	(424)	-1%
2003	93,021	92,214	(807)	-1%
2004	116,133	114,992	(1,141)	-1%
2005	84,556	83,825	(731)	-1%
2006	68,570	68,470	(100)	0%
2007	65,537	65,531	(6)	0%
2008	152,662	152,651	(11)	0%
2009	331,410	331,399	(11)	0%
2010	414,277	414,261	(16)	0%
2011	333,745	333,745	0	0%
2012	417,660	417,660	0	0%
2013	586,382	586,382	0	0%
2014	269,885	269,885	0	0%
2015	488,122	488,122	0	0%
2016	707,384	707,384	0	0%
2017	800,804	800,804	0	0%
2018	680,155	680,155	0	0%
2019	713,490	713,490	0	0%
2020	1,252,492	1,252,492	0	0%
<b>Total</b>	<b>7,899,856</b>	<b>7,895,703</b>	<b>(4,153)</b>	<b>0%</b>

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 70

Table 25: Data Reconciliation - Insurance in Force

Insurance in Force (\$M)				
= Original Loan Amount on Active Loans				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	632,737,045	630,175,704	(2,561,341)	0%
1993	1,128,051,113	1,122,662,281	(5,388,832)	0%
1994	1,693,390,286	1,685,534,003	(7,856,283)	0%
1995	804,863,327	802,945,779	(1,917,548)	0%
1996	1,383,145,048	1,381,194,526	(1,950,522)	0%
1997	1,538,664,165	1,536,111,497	(2,552,668)	0%
1998	2,622,750,438	2,614,282,837	(8,467,601)	0%
1999	3,477,643,199	3,465,625,793	(12,017,406)	0%
2000	1,928,948,049	1,917,580,035	(11,368,014)	-1%
2001	3,784,816,154	3,774,058,838	(10,757,316)	0%
2002	5,986,934,870	5,952,126,416	(34,808,454)	-1%
2003	9,760,137,449	9,687,453,499	(72,683,950)	-1%
2004	12,226,545,193	12,130,291,064	(96,254,129)	-1%
2005	9,134,628,096	9,072,357,217	(62,270,879)	-1%
2006	7,782,880,704	7,773,600,757	(9,279,947)	0%
2007	8,006,143,056	8,005,729,158	(413,898)	0%
2008	21,311,279,293	21,310,167,626	(1,111,667)	0%
2009	50,244,615,492	50,243,397,129	(1,218,363)	0%
2010	61,134,262,611	61,132,626,092	(1,636,519)	0%
2011	50,658,951,615	50,658,951,615	0	0%
2012	65,322,259,638	65,322,259,638	0	0%
2013	94,545,227,961	94,545,227,961	0	0%
2014	37,222,658,900	37,222,658,900	0	0%
2015	80,619,068,501	80,619,068,501	0	0%
2016	125,913,138,455	125,913,138,455	0	0%
2017	150,269,903,430	150,269,903,430	0	0%
2018	129,528,758,809	129,528,758,809	0	0%
2019	144,553,787,700	144,553,787,700	0	0%
2020	289,995,649,771	289,995,649,771	0	0%
Total	1,373,211,840,368	1,372,867,325,031	(344,515,337)	0%

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 71

Table 26: Data Reconciliation - Number of 90 Day Delinquencies

Number of 90 Day Delinquencies				
= Current Number of 90 Day Delinquencies				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	557	557	0	0%
1993	871	873	2	0%
1994	1,446	1,447	1	0%
1995	1,028	1,029	1	0%
1996	1,892	1,894	2	0%
1997	2,101	2,101	0	0%
1998	3,339	3,339	0	0%
1999	4,689	4,690	1	0%
2000	3,206	3,208	2	0%
2001	5,153	5,158	5	0%
2002	7,252	7,253	1	0%
2003	10,201	10,210	9	0%
2004	14,173	14,185	12	0%
2005	11,566	11,576	10	0%
2006	10,204	10,207	3	0%
2007	10,741	10,747	6	0%
2008	26,057	26,075	18	0%
2009	43,241	43,280	39	0%
2010	46,407	46,438	31	0%
2011	35,032	35,045	13	0%
2012	40,869	40,894	25	0%
2013	52,392	52,426	34	0%
2014	34,410	34,427	17	0%
2015	61,439	61,468	29	0%
2016	88,411	88,447	36	0%
2017	105,748	105,792	44	0%
2018	102,729	102,793	64	0%
2019	104,098	104,175	77	0%
2020	71,257	71,352	95	0%
Total	900,509	901,086	577	0%

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 72

Table 27: Data Reconciliation - Number of Claims to Date

Number of Claims To Date				
Credit Subsidy Cohort	Federal Housing Administration (Data as of September 2020)	Independent Actuary (Data as of September 2020)	Absolute Difference (Actuary - FHA)	Percent Difference (Actuary - FHA) / FHA
1992	36,778	36,778	0	0%
1993	52,278	52,276	(2)	0%
1994	65,920	65,919	(1)	0%
1995	44,678	44,678	0	0%
1996	63,473	63,466	(7)	0%
1997	59,869	59,860	(9)	0%
1998	67,469	67,459	(10)	0%
1999	84,217	84,204	(13)	0%
2000	71,330	71,321	(9)	0%
2001	85,345	85,335	(10)	0%
2002	90,497	90,476	(21)	0%
2003	91,202	91,188	(14)	0%
2004	115,820	115,798	(22)	0%
2005	92,054	92,045	(9)	0%
2006	94,239	94,238	(1)	0%
2007	106,321	106,321	0	0%
2008	223,769	223,768	(1)	0%
2009	225,483	225,483	0	0%
2010	115,004	115,004	0	0%
2011	47,109	47,109	0	0%
2012	29,148	29,148	0	0%
2013	26,684	26,684	0	0%
2014	15,349	15,349	0	0%
2015	14,681	14,681	0	0%
2016	12,201	12,201	0	0%
2017	8,224	8,224	0	0%
2018	3,678	3,678	0	0%
2019	533	533	0	0%
2020	5	5	0	0%
<b>Total</b>	<b>1,943,353</b>	<b>1,943,224</b>	<b>(129)</b>	<b>0%</b>



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 73

## Appendix B – Transition Models

---

This appendix describes the technical details of the predictive models used to estimate the transition behavior of forward mortgages.

Section 1 summarizes the model specifications used to analyze FHA mortgage status transitions and the subsequent ultimate claim and prepayment rates. This section also presents the statistical theory behind multinomial logistic models.

Section 2 describes the explanatory variables used in the models.

Section 3 shows the model parameters.

Section 4 shows the model validation of the binomial logistic models.

### Section 1: Model Specification

Prior to the 2010 Actuarial Review, a competing-risk framework based on multinomial logistic models for quarterly conditional probabilities of prepayment and claim terminations was used. Starting with the 2010 Review, a third “competing risk” was introduced: 90-day delinquency, or default. The date from which a mortgage is first reported to be 90 or more days late is used to identify the start of a default episode, and this episode continues until ended by cure or the mortgage terminates through claim or prepayment. Active mortgages that are not in a 90-day default episode at the beginning of the quarter are classified as current.

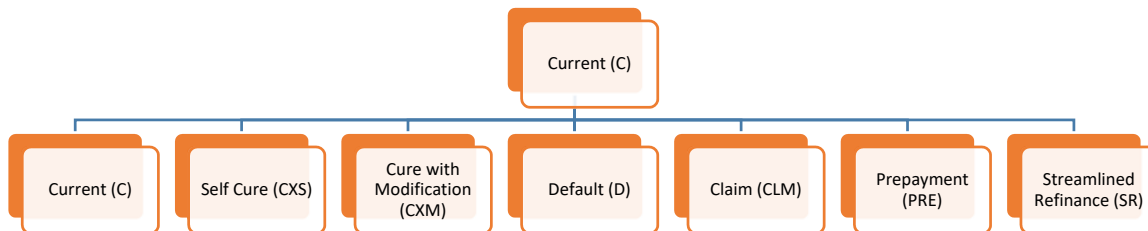
Figure 12 below shows the possible “current” status transitions that have been modeled using the multinomial framework.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 74

Figure 12: Transition Models – Initial Current Status



Mortgages in current status (C) at the beginning of the quarter can default and cure in the same quarter (CXS and CXM), transition to default status (D) at the start of the next quarter, result in a claim (CLM) or terminate as a prepayment due to an FHA Streamlined Refinance (SR) or as a prepayment (PRE) for any reason other than SR. There are two types of cures, a self-cure (CXS) and a cure that includes a mortgage modification (CXM). Also, due to the very low likelihood of a current mortgage transitioning into to a CLM in one quarter, we have combined D and CLM into one category (DCLM).

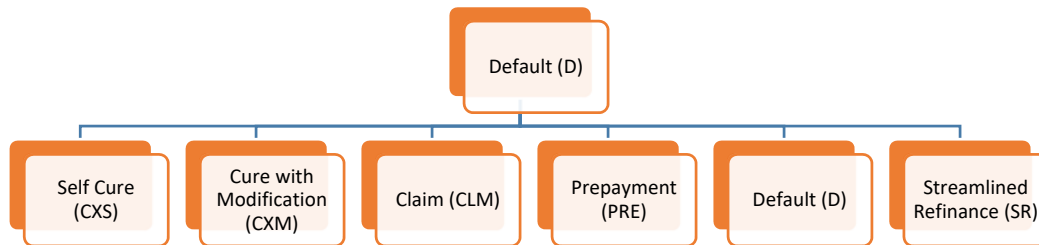
The figure below shows the possible default status transitions that have been modeled using the multinomial framework.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 75

Figure 13: Transition Models – Initial Default Status



For mortgages that begin the quarter in default, they can cure either by the borrower becoming current on their own (CXS), or they can cure with a modification in the terms of the mortgage (CXM). The mortgage can also terminate as a prepayment due to an SR or as a prepayment (PRE) for any reason other than SR, turn into a claim (CLM) or remain in default (D). For the development of the transition models, we have combined PRE and SR into one category (END).

As the mortgage transitions through multiple stages, the historical status of the mortgage is retained. At any point in the life of the mortgage, we track both the number of prior times the mortgage was either in default or modified as well as the length of time since the mortgage was in the prior stage.

As a result of the COVID-19 pandemic, borrowers who experienced an adverse impact on their ability to make on-time mortgage payments are eligible for forbearance for an initial period of six months, and this initial period can be extended by up to six additional months. Borrowers are eligible to receive COVID-19 forbearance through December 31, 2020. This may result in loans being in forbearance through the end of 2021. While a loan is in forbearance, the borrower does not have to make mortgage payments, which technically means the loan is in default. As no action can be taken on these loans by the lender while the loan is in forbearance, the path of these loans cannot be projected by the normal default models.

For loans in forbearance, some may be eligible for a partial claim or loan modification if they were current on their payments as of March 1, 2020. Based on the forbearance criteria, Pinnacle has developed an adjustment to the simulation process to handle these COVID-19 forbearance loans. Loans in COVID-19 forbearance as of

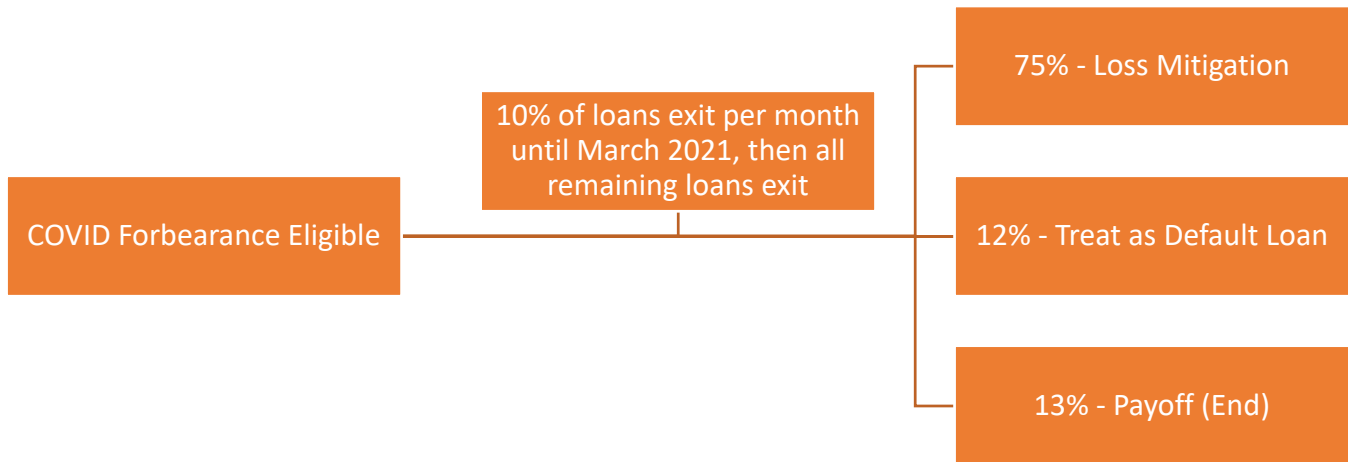
# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 76

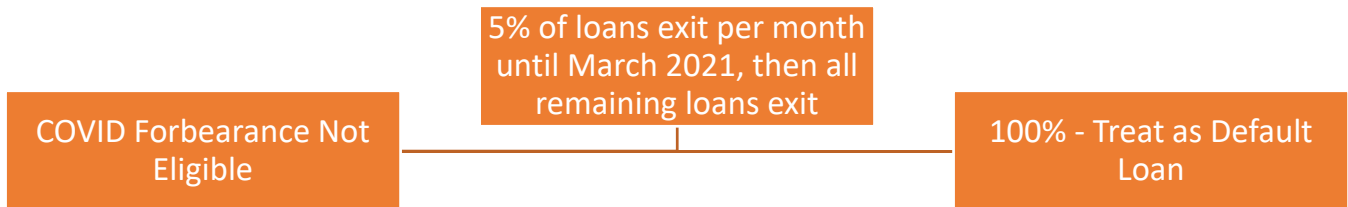
September 30, 2020 that are eligible for a loan modification or partial claim will be simulated as follows:

Figure 14: COVID-19 Forbearance Simulation – Loans Eligible for Partial Claim or Loan Modification



Loans in COVID-19 forbearance as of September 30, 2020 that are not eligible for a loan modification or partial claim will be simulated as follows:

Figure 15: COVID-19 Forbearance Simulation – Loans Not Eligible for Partial Claim or Loan Modification



Given that loans can enter COVID-19 forbearance through December 31, 2020, it is theoretically possible for loans to remain in forbearance through the end of 2021. However, based on data from HUD and Black Knight, the number of loans still entering forbearance is small. Therefore, we are assuming that the impact of loans in

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 77

forbearance after March, 2021 will be negligible. Also, the treatment of loans exiting COVID-19 forbearance was determined based on data from HUD and Black Knight.

### Multinomial Logistic Regression Theory and Model Specification

Multinomial logistic regression is used to model the relationship between a collection of predictor variables and the distributional behavior of a polytomous response variable. It is a likelihood-based methodology and may be viewed as the generalization of logistic regression for a response variable with more than two levels.

To formalize its description, let the response variable  $Y$  take  $m$  possible levels, denoted for simplicity as  $1, \dots, m$ , and assume there is a collection of  $g$  predictors  $X_1, \dots, X_g$ , that are used to model  $Y$ 's distribution. We assume that  $Y$  and  $X_1, \dots, X_g$  are jointly observed  $n$  times with the  $i^{\text{th}}$  random observation being labeled as

$Y_i, X_{1i}, \dots, X_{gi}$  and its realized value  $y_i, x_{1i}, \dots, x_{gi}$ .

In a multinomial logistic regression, the mathematical structure of the model is set by the following two assumptions:

1. The  $g+1$  length random vectors  $\langle Y_i, X_{1i}, \dots, X_{gi} \rangle$  are jointly independent across all  $i$
2. Given that  $X_{1i}, \dots, X_{gi}$  have been observed at  $x_{1i}, \dots, x_{gi}$ ,  $Y_i$ 's distribution is assumed to be multinomial with

$$P(Y_i = l) = \exp(\mu^l + \sum_{k=1}^g \beta_k^l \cdot x_{ki}) / (\sum_{j=1}^m \exp(\mu^j + \sum_{k=1}^g \beta_k^j \cdot x_{ki})),$$

where the  $\beta_k^j$  are unknown regression parameters and the  $\mu^j$  are unknown intercept parameters. [Note: To prevent over-specification of the model due to the constraint that the above probabilities sum to 1 over  $l=1, \dots, m$ , a base level  $j$  is chosen such that  $\beta_k^j$  and  $\mu^j$  are set equal to zero.] Thus, if  $j = 1$ , then

$$P(Y_i=1) = 1 / (1 + \sum_{j=2}^m \exp(\mu^j + \sum_{k=1}^g \beta_k^j \cdot x_{ki})).$$

It now follows the likelihood equation for this model is given by

$$\prod_{i=1}^n P(Y_i=y_i) = \prod_{i=1}^n \exp(\mu^{y_i} + \sum_{k=1}^g \beta_k^{y_i} \cdot x_{ki}) / (\sum_{j=1}^m \exp(\mu^j + \sum_{k=1}^g \beta_k^j \cdot x_{ki})).$$

The multinomial logistic regression procedure optimizes the above likelihood over the unknown parameters in order to find those parameters that are most likely to have given rise to the data.

In the 2017 and 2018 Actuarial Reviews, we used multinomial logistic models to estimate the probability of transition for current and default mortgages. For the 2019 and 2020 Actuarial Reviews, we are using binomial logistic models to predict each transition separately, and once all the binomial models are completed, we compute multinomial probabilities from the binomial models. The primary reason for making this change is that it allows us to better model each transition with the variables that impact that transition, whereas the specific multinomial model structure requires us to include a variable for all transitions even if it is only predictive of one

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 78

of the transitions.

The multinomial structure used in the 2017 and 2018 reports did not allow for the use of variables just for individual transitions, if a variable was included in the model it applied to all transitions. This can result in model over-specification, as there are some independent variables that are not significant for some transitions. To address this, Pinnacle used binomial models for each transitions and applied an adjustment to reflect the multinomial nature of the process.

Pinnacle investigated the use of Multinomial Discrete Choice (MDC) models for this analysis. MDC models allow all transitions to be modeled simultaneously, and also allows for the use of independent variables only for specific transitions. Pinnacle compared the MDC approach to the binomial logistic approach, and concluded that the two approaches produce identical model results. We also observed that the MDC approach took significantly longer to complete as it was more computationally intensive. Because the results of the two methods were identical and the binomial logistic models ran more efficiently, we decided to continue with the binomial logistic approach with the multinomial adjustment.

The target variables for the current and default transition models are shown above in Figure 12 and Figure 13. The independent variables used in the models are described in the following section. 31 models were built, 15 for the current (C) transitions and 16 for the Default (D) transitions. Four product groups are modeled: non-SR fixed rate 30-year term (FRM30NSR), SR fixed rate 30-year term (FRM30SR), fixed rate 15-year term (FRM15) and adjustable rate mortgages (ARM). The model development was completed using a train/validate approach. A random sample of the data is used to train the model, to determine inclusion and exclusion of explanatory variables, and to calculate model parameters. The remaining sample, the validation, is used as a final validation step to confirm the predictive power of the final model.

To generate the random sample, random numbers were added to the dataset at the case level using a random number generator. The random numbers were drawn from a uniform distribution between 0 and 1. Based on these random numbers, 60% of the cases were assigned to the train dataset and 40% were assigned to the validation dataset.

There are over 36 million single-family mortgages insured by FHA originated between the first quarter of Fiscal Year 1975 and the fourth quarter of Fiscal Year 2020. For the transition models with the initial condition of C for the FRM30NSR, we used a random sample of 50% of the data. For all other products, we used 100% of the data in the model development.

For transition models with the initial condition of D we used 100% of the data for all ending condition models for all products.

### Computation of Multinomial Logistic Probabilities from Binomial Models

As stated above, we compute multinomial probabilities from the binomial models described developed. To arrive at the multinomial logit model for  $K$  possible outcomes,  $K-1$  independent binary logistic regression models

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 79

are run and the  $K$ th outcome is derived from the  $K-1$  models. The linear predictor ( $lp$ ) is formulated by a binomial logistic regression for all transitions except for the transition representing remaining in the same state (C\_C or D\_D), which is the  $K$ th outcome. This is consistent with the approach developed by Begg and Gray (1984)<sup>61</sup>, in which separate binomial logistic models for each possible transition type are developed, and then the estimates are recombined to derive the multinomial logistic probabilities.

For the C transitions:

$$lp(C\_D) = e^{\alpha^{C\_D} + X^{C\_D}(t)\beta^{C\_D}}$$

$$lp(C\_CXS) = e^{\alpha^{C\_CXS} + X^{C\_CXS}(t)\beta^{C\_CXS}}$$

$$lp(C\_SR) = e^{\alpha^{C\_SR} + X^{C\_SR}(t)\beta^{C\_SR}}$$

$$lp(C\_PRE) = e^{\alpha^{C\_PRE} + X^{C\_PRE}(t)\beta^{C\_PRE}}$$

The probabilities can then be derived for each of the  $K-1$  transitions:

$$Prob(C\_D) = lp(C\_D) / [1 + lp(C\_D) + lp(C\_CXS) + lp(C\_SR) + lp(C\_PRE)]$$

$$Prob(C\_CXS) = lp(C\_CXS) / [1 + lp(C\_D) + lp(C\_CXS) + lp(C\_SR) + lp(C\_PRE)]$$

$$Prob(C\_SR) = lp(C\_SR) / [1 + lp(C\_D) + lp(C\_CXS) + lp(C\_SR) + lp(C\_PRE)]$$

$$Prob(C\_PRE) = lp(C\_PRE) / [1 + lp(C\_D) + lp(C\_CXS) + lp(C\_SR) + lp(C\_PRE)]$$

The  $K$ th probability is

$$Prob(C\_C) = 1 - Prob(C\_D) - Prob(C\_CXS) - Prob(C\_SR) - Prob(C\_PRE)$$

For the D transitions:

$$lp(D\_CLM) = e^{\alpha^{D\_CLM} + X^{D\_CLM}(t)\beta^{D\_CLM}}$$

---

<sup>61</sup> Begg, C.B. and R. Gray, "Calculation of Polychotomous Logistic Regression Parameters Using Individualized Regressions," *Biometrika*, 71(1):11-18, 1984.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 80

$$lp(D\_CXS) = e^{\alpha^{D\_CXS} + X^{D\_CXS}(t)\beta^{D\_CXS}}$$

$$lp(D\_CXM) = e^{\alpha^{D\_CXM} + X^{D\_CXM}(t)\beta^{D\_CXM}}$$

$$lp(D\_END) = e^{\alpha^{D\_END} + X^{D\_END}(t)\beta^{D\_END}}$$

The probabilities can then be derived for each of the  $K-1$  transitions:

$$Prob(D\_CLM) = lp(D\_CLM) / [1 + lp(D\_CLM) + lp(D\_CXS) + lp(D\_CXM) + lp(D\_END)]$$

$$Prob(D\_CXS) = lp(D\_CXS) / [1 + lp(D\_CLM) + lp(D\_CXS) + lp(D\_CXM) + lp(D\_END)]$$

$$Prob(D\_CXM) = lp(D\_CXM) / [1 + lp(D\_CLM) + lp(D\_CXS) + lp(D\_CXM) + lp(D\_END)]$$

$$Prob(D\_END) = lp(D\_END) / [1 + lp(D\_CLM) + lp(D\_CXS) + lp(D\_CXM) + lp(D\_END)]$$

The  $K$ th probability is

$$Prob(D\_D) = 1 - Prob(D\_CLM) - Prob(D\_CXS) - Prob(D\_CXM) - Prob(D\_END)$$

Finally, a check is built into the simulation to assure the sum of all transition probabilities does not exceed 1.0.

### Section 2: Transition Model Explanatory Variables

Multiple categories of explanatory variables were considered in development of the transition models.

- Fixed initial mortgage characteristics: market rate, initial mortgage size, spread at origination, refinance indicator
- Fixed initial borrower characteristics: down payment assistance, first-time home buyer, credit score, cohort year
- Property characteristics: the number of living units, initial home values
- Dynamic variables based on mortgage information: prior default indicator, number of prior default episodes, prior mortgage modification, number of prior modifications, LTV ratio, interest rate spread, TEI (expense to income ratio), mortgage period, duration of default episode, time since last default episode
- Dynamic variables derived by combining mortgage information and external economic data: spread, season
- Dynamic macroeconomic variables: average unemployment rate over multiple time periods, change in



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 81

the unemployment rate, HPI, change in HPI, treasury rates, GDP measures, slope of yield curve. Consumer Confidence Index, Small Business Confidence Index

- Geographic variables: judicial state, collateral state

The following explanatory variables are used in the transition models. A general description of the variable is provided below, and more specific detail is included in the Model Parameters section.

- **Periodnbr**: the number of quarters since the inception of the mortgage. This variable is incorporated as a piecewise variate and a grouped categorical variable.
- **Refiincent**: refinance incentive - the ratio of the difference in the initial mortgage rate to the current market mortgage rate. This variable is calculated as  $(100 * \text{mortgage interest rate}) / (\text{market FRM30 rate})$ . This variable is incorporated as a piecewise variate.
- **Priordef**: number of prior default episodes. This variable is incorporated as a grouped categorical variable and a piecewise variate.
- **Timesinced**: time since most recent default. This variable is incorporated as a grouped categorical variable.
- **Credit**: credit score. This variable is incorporated as a piecewise variate.
- **Ratiotmptei**: front end ratio, the portion of an individual's income allocated to mortgage payments. This variable is incorporated as a piecewise variate.
- **Deltaue**: change in unemployment rate from mortgage inception to current. This variable is incorporated as a piecewise variate.
- **Deltauepr3**: change in unemployment rate from three quarters prior to current. This variable is incorporated as a piecewise variate.
- **Hpa2yb**: house price appreciation over the past two years. This variable is calculated as  $(\text{current hpi\_index} / \text{hpi\_index 8 quarters prior})$ . This variable is incorporated as a piecewise variate.
- **LTV**: ratio of the amortized loan balance to the current home value. This variable is incorporated as a piecewise variate.
- **Loanraw**: the initial mortgage amount. This variable is incorporated as a piecewise variate.
- **Frst tm by**: first time home buyer. This variable is incorporated as a categorical variable.
- **Season**: the quarter of the year. Possible values are 1 – January through March, 2 – April through June, 3 – July through September, and 4 – October through December. This variable is incorporated as a grouped categorical variable.
- **Rfnc ind**: an indicator of whether the mortgage was a refinance. This variable is incorporated as a categorical variable.
- **Dpa**: down payment assistance. This variable is incorporated as a categorical variable.
- **Ueblend**: current unemployment rate. This variable is incorporated as a piecewise variate.
- **Ycslope**: yield curve. This variable is incorporated as a grouped categorical variable.
- **Sato**: spread at origination. This variable is calculated as the difference between the prevailing interest rate and the mortgage interest rate at time of origination. This variable is incorporated as a piecewise

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 82

variate.

- **Calperiod**: calendar year and quarter. This variable is incorporated as a grouped categorical variable.
- **Judicial**: whether the property is in a judicial state. This variable is incorporated as a categorical variable.
- **Cred\_subs\_coht**: credit subsidy cohort. This variable is incorporated as a grouped categorical variable.
- **Treasury\_yr30**: 30-year CMT rate. This variable is incorporated as a grouped categorical variable.
- **Deltaty1**: change in one-year CMT rate from policy inception to current. This variable is incorporated as a piecewise variate.
- **Deltaty10init**: 10-year CMT rate at policy inception. This variable is incorporated as a grouped categorical variable.
- **Durdefep**: duration of default episode. This variable is incorporated as a grouped categorical variable.

For variables that are incorporated as a piecewise variate, further information is provided on how these variates are specified in the Model Parameter section.

The overall percentage of records in each final condition category for the initial condition of Current is shown in the table below.

Table 28: Distribution of Final Condition – Current Transition Models

<u>Final Condition</u>	<u>Percentage</u>
CXS	0.45%
DCLM	2.45%
CXM	0.01%
SR	0.77%
PRE	2.30%
C	93.98%

The overall percentage of records in each final condition category for the initial condition of Default is shown in the table below.

Table 29: Distribution of Final Condition - Default Transition Models

<u>Final Condition</u>	<u>Percentage</u>
CLM	3.79%
CXM	2.62%

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 83

<u>Final Condition</u>	<u>Percentage</u>
CXS	19.80%
END	1.50%
D	72.25%

### Section 3: Binomial Model Results

#### Current Transition Model Parameters – FRM30NSR C\_SR

The model parameters for the FRM30NSR current to streamlined refinance transition are shown below.

Table 30: Current to Streamlined Refinance Transition FRM30NSR Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-8.6089	0.0542	<.0001
mjudicial	1		Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.1874	0.00149	<.0001
mjudicial	2		Categorical of judicial (judicial state)	base level: else			
mperiodnbr_CSR	L03		Categorical of period_number	period_number <= 3	-0.3538	0.00345	<.0001
mperiodnbr_CSR	L04		Categorical of period_number	period_number = 4	0.358	0.00315	<.0001
mperiodnbr_CSR	L05		Categorical of period_number	period_number = 5	0.366	0.00304	<.0001
mperiodnbr_CSR	L06		Categorical of period_number	period_number = 6	0.265	0.00309	<.0001
mperiodnbr_CSR	L07		Categorical of period_number	period_number = 7	0.1479	0.00316	<.0001
mperiodnbr_CSR	Z08		Categorical of period_number	base level: else			
vperiodnbr_CSR_pw1			Variate piecewise of period_number	median(0,period_number-8,22-8)	-0.0621	0.000273	<.0001
vperiodnbr_CSR_pw2			Variate piecewise of period_number	median(0,period_number-22,39-22)	-0.0654	0.000327	<.0001
vperiodnbr_CSR_pw3			Variate piecewise of period_number	median(0,period_number-39,56-39)	-0.0535	0.000712	<.0001
vperiodnbr_CSR_pw4			Variate piecewise of period_number	median(0,period_number-56,70-56)	-0.0317	0.00173	<.0001
vperiodnbr_CSR_pw5			Variate piecewise of period_number	median(0,period_number-70,88-70)	-0.0655	0.00275	<.0001
vrefiincent_CSR_pw1			Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent_r-0,93-0)	-0.00362	0.000522	<.0001
vrefiincent_CSR_pw2			Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(93,refi_incent_r-113,113-93)	0.1117	0.000227	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 84

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vrefiincident_CSR_pw3			Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent2_r-113,130-113)	0.068	0.000145	<.0001
vrefiincident_CSR_pw4			Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent2_r-130,180-130)	0.0185	0.000084	<.0001
vrefiincident_CSR_pw5			Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent2_r-180,250-180)	-0.00548	0.00034	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	-0.8973	0.00841	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	-0.8052	0.00943	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	-0.6376	0.01	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	-0.2879	0.00961	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	-0.2371	0.0104	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	-0.2721	0.0114	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; 7 <= cx_time <= 9	-0.2075	0.00754	<.0001
mpriordef_csr*mtimesinceD_CSR	L01	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time >= 9	-0.0945	0.00724	<.0001
mpriordef_csr*mtimesinceD_CSR	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	-1.5376	0.0164	<.0001
mpriordef_csr*mtimesinceD_CSR	L02	L02	Interaction of categorical of	prior_default_cnt = 2; cx_time = 2	-1.328	0.018	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 85

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			prior_default_cnt and categorical of cx_time <sup>1</sup>				
mpriordef_csr*mtimesinceD_CSR	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	-0.9741	0.018	<.0001
mpriordef_csr*mtimesinceD_CSR	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	-0.4305	0.0159	<.0001
mpriordef_csr*mtimesinceD_CSR	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	-0.2698	0.0165	<.0001
mpriordef_csr*mtimesinceD_CSR	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 6	-0.282	0.0184	<.0001
mpriordef_csr*mtimesinceD_CSR	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; 7 <= cx_time <= 9	-0.2642	0.0126	<.0001
mpriordef_csr*mtimesinceD_CSR	L02	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time >= 9	-0.1541	0.0104	<.0001
mpriordef_csr*mtimesinceD_CSR	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	-1.8959	0.0154	<.0001
mpriordef_csr*mtimesinceD_CSR	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	-1.4955	0.0158	<.0001
mpriordef_csr*mtimesinceD_CSR	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	-0.9936	0.0151	<.0001
mpriordef_csr*mtimesinceD_CSR	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	-0.2935	0.0129	<.0001
mpriordef_csr*mtimesinceD_CSR	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	-0.1482	0.0137	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 86

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_csr*mtimesinceD_CSR	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	-0.1926	0.0156	<.0001
mpriordef_csr*mtimesinceD_CSR	L03	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; 7 <= cx_time <= 9	-0.2127	0.0115	<.0001
mpriordef_csr*mtimesinceD_CSR	L03	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time >= 9	-0.1965	0.0106	<.0001
mpriordef_csr*mtimesinceD_CSR	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vpriordef_CSR_pw1			Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	0.082	0.00249	<.0001
vcredit_CSR_pw1			Variate piecewise of credit_score	median(0,credit_score-500,650-500)	-0.00378	0.000018	<.0001
vcredit_CSR_pw2			Variate piecewise of credit_score	median(0,credit_score-650,680-650)	0.00236	0.000107	<.0001
vcredit_CSR_pw3			Variate piecewise of credit_score	median(0,credit_score-680,720-680)	-0.00278	0.0001	<.0001
vcredit_CSR_pw4			Variate piecewise of credit_score	median(0,credit_score-720,800-720)	-0.00185	0.000068	<.0001
mRatioTmpTei_CSR	L00		Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	1.0086	0.00519	<.0001
mRatioTmpTei_CSR	Z00		Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_CSR_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-11,18-11)	0.0246	0.000684	<.0001
vratiotmptei_CSR_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-18,22-18)	0.0119	0.000811	<.0001
vratiotmptei_CSR_pw3			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-22,29-22)	0.00264	0.000408	<.0001
vratiotmptei_CSR_pw4			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-29,37-29)	-0.00256	0.000332	<.0001
vtimesinced_CSR_pw1			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-9,40-7)	0.00947	0.000683	<.0001
vdeltaUEinit_CSR_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-0,60-0)	-0.00349	0.000345	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 87

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vdeltaUEinit_CSR_pw2			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-60,77-60)	0.0231	0.000279	<.0001
vdeltaUEinit_CSR_pw3			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-77,100-77)	-0.0042	0.000162	<.0001
vdeltaUEinit_CSR_pw4			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-100,105-100)	0.0861	0.000621	<.0001
vdeltaUEinit_CSR_pw5			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-105,145-105)	0.00952	0.000084	<.0001
vdeltaUEinit_CSR_pw6			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-145,225-145)	-0.00098	0.000061	<.0001
vhpa2yb_CSR_pw1			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-0,85-0)	0.0119	0.000116	<.0001
vhpa2yb_CSR_pw2			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-85,100-85)	-0.0188	0.000272	<.0001
vhpa2yb_CSR_pw3			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-100,106-100)	0.1175	0.000523	<.0001
vhpa2yb_CSR_pw4			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-106,111-106)	-0.0102	0.000569	<.0001
vhpa2yb_CSR_pw5			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-111,122-111)	0.00569	0.000305	<.0001
vhpa2yb_CSR_pw6			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-122,160-122)	-0.026	0.00032	<.0001
vltv_CSR_pw1			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,70-0)	-0.00438	0.000265	<.0001
vltv_CSR_pw2			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-70,80-70)	0.0311	0.000601	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 88

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vltv_CSR_pw3			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-80,89-80)	0.00595	0.000464	<.0001
vltv_CSR_pw4			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-89,93-89)	-0.0333	0.000812	<.0001
vltv_CSR_pw5			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-93,95-93)	0.0283	0.00143	<.0001
vltv_CSR_pw6			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-95,97-95)	0.1424	0.00166	<.0001
vltv_CSR_pw7			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-97,100-97)	-0.1794	0.00498	<.0001
vloanraw_CSR_pw1			Variate piecewise of loansize_raw	median(0,loansize_raw-47000,74000-47000)	0.000046	1.71E-07	<.0001
vloanraw_CSR_pw2			Variate piecewise of loansize_raw	median(0,loansize_raw-74000,159000-74000)	0.000011	3.11E-08	<.0001
vloanraw_CSR_pw3			Variate piecewise of loansize_raw	median(0,loansize_raw-159000,345000-159000)	4.53E-06	1.77E-08	<.0001
vloanraw_CSR_pw4			Variate piecewise of loansize_raw	median(0,loansize_raw-345000,600000-345000)	2.34E-07	3.04E-08	<.0001
mfrst_tm_by	1		Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.2082	0.00156	<.0001
	2		Categorical of frst_tm_by (first-time buyer)	base level: else			
mDeltaTY1Init_CSR	L01		Categorical of DeltaTy1Init (Change in 1 yr Treasury policy inception to current)	DeltaTY1Init > 1.15	0.3492	0.00217	<.0001
mDeltaTY1Init_CSR	Z00		Categorical of DeltaTy1Init (Change in 1 yr Treasury policy inception to current)	base level: else			

Current Transition Model Parameters – FRM30NSR C\_PRE

The model parameters for the FRM30NSR current to prepayment transition are shown below.

Table 31: Current to Prepayment Transition FRM30NSR Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-6.6377	0.013	<.0001
mseason	1		Categorical of season	season = "winter"	-0.1625	0.00137	<.0001
mseason	2		Categorical of season	season = "spring"	0.0866	0.00129	<.0001
mseason	3		Categorical of season	season = "summer"	0.0723	0.00128	<.0001



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 89

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mseason	4		Categorical of season	base level: season = "fall"			
mfrst_tm_by	1		Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.1433	0.00116	<.0001
mfrst_tm_by	2		Categorical of frst_tm_by (first-time buyer)	base level: else			
mrfnc_ind	2		Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind = "N"	-0.0678	0.00386	<.0001
mrfnc_ind	3		Categorical of rfnc_ind (refinanced loan indicator)	base level: else			
mdpa_govt	LGovt		Categorical of dpa (down payment assistance)	dpa = "govt"	-0.1034	0.00428	<.0001
mdpa_govt	ZOthr		Categorical of dpa (down payment assistance)	base level: else			
mdpa_rel	LRela		Categorical of dpa (down payment assistance)	dpa = "Relative"	0.0503	0.0014	<.0001
mdpa_rel	ZOthr		Categorical of dpa (down payment assistance)	base level: else			
mperiodnbr_CPre	L02		Categorical of period_number	period_number = 2	-2.7089	0.00817	<.0001
mperiodnbr_CPre	L03		Categorical of period_number	period_number = 3	-1.689	0.00521	<.0001
mperiodnbr_CPre	L04		Categorical of period_number	period_number = 4	-1.1247	0.00407	<.0001
mperiodnbr_CPre	L05		Categorical of period_number	period_number = 5	-0.6254	0.00332	<.0001
mperiodnbr_CPre	L06		Categorical of period_number	period_number = 6	-0.3712	0.00303	<.0001
mperiodnbr_CPre	L07		Categorical of period_number	period_number = 7	-0.24	0.00289	<.0001
mperiodnbr_CPre	Z08		Categorical of period_number	base level: else			
vperiodnbr_CPre_pw1			Variate piecewise of period_number	median(0,period_number-8,22-8)	0.0206	0.000175	<.0001
vperiodnbr_CPre_pw2			Variate piecewise of period_number	median(0,period_number-22,35-22)	-0.0107	0.000204	<.0001
vperiodnbr_CPre_pw3			Variate piecewise of period_number	median(0,period_number-35,42-35)	0.00445	0.000487	<.0001
vperiodnbr_CPre_pw4			Variate piecewise of period_number	median(0,period_number-42,70-42)	-0.0272	0.000222	<.0001
vperiodnbr_CPre_pw5			Variate piecewise of period_number	median(0,period_number-70,108-70)	0.00943	0.000349	<.0001
mperiodnbr_CPre*mrfnc_ind	L02	2	Interaction of categorical of period_number and categorical of rfnc_ind	period_number = 2; rfnc_ind = "N"	1.094	0.0137	<.0001
mperiodnbr_CPre*mrfnc_ind	L03	2	Interaction of categorical of period_number and categorical of rfnc_ind	period_number = 3; rfnc_ind = "N"	1.0166	0.00931	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 90

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			period_number and categorical of rfnc_ind				
mperiodnbr_CPre*mrfnc_ind	L04	2	Interaction of categorical of period_number and categorical of rfnc_ind	period_number = 4; rfnc_ind = "N"	0.7846	0.00821	<.0001
mperiodnbr_CPre*mrfnc_ind	L05	2	Interaction of categorical of period_number and categorical of rfnc_ind	period_number = 5; rfnc_ind = "N"	0.4469	0.00773	<.0001
mperiodnbr_CPre*mrfnc_ind	L06	2	Interaction of categorical of period_number and categorical of rfnc_ind	period_number = 6; rfnc_ind = "N"	0.2738	0.00767	<.0001
mperiodnbr_CPre*mrfnc_ind	L07	2	Interaction of categorical of period_number and categorical of rfnc_ind	period_number = 7; rfnc_ind = "N"	0.1793	0.00773	<.0001
mperiodnbr_CPre*mrfnc_ind	Z08	3	Interaction of categorical of period_number and categorical of rfnc_ind	base level: period_number else; rfnc_ind else			
vperiodnbr_CPre_pw1*mrfnc_ind	2		Interaction of variate of period_number and categorical of rfnc_ind	median(0,period_number-8,22-8); rfnc_ind = "N"	-0.0313	0.000444	<.0001
vperiodnbr_CPre_pw2*mrfnc_ind	2		Interaction of variate of period_number and categorical of rfnc_ind	median(0,period_number-22,35-22); rfnc_ind = "N"	-0.00621	0.000621	<.0001
vperiodnbr_CPre_pw3*mrfnc_ind	2		Interaction of variate of period_number and categorical of rfnc_ind	median(0,period_number-35,42-35); rfnc_ind = "N"	-0.0229	0.00167	<.0001
vperiodnbr_CPre_pw4*mrfnc_ind	2		Interaction of variate of period_number and categorical of rfnc_ind	median(0,period_number-42,70-42); rfnc_ind = "N"	0.0167	0.000862	<.0001
vperiodnbr_CPre_pw5*mrfnc_ind	2		Interaction of variate of period_number and categorical of rfnc_ind	median(0,period_number-70,108-70); rfnc_ind = "N"	0.006	0.00245	0.0144
vperiodnbr_CPre_pw*mrfnc_ind	3		Interaction of variate of period_number and categorical of rfnc_ind	base level period_number piecewise; rfnc_ind else			

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 91

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vcredit_CPre_pw1			Variate piecewise of credit_score	median(0,credit_score-450,530-450)	-0.0109	0.000082	<.0001
vcredit_CPre_pw2			Variate piecewise of credit_score	median(0,credit_score-530,630-530)	0.000928	0.000073	<.0001
vcredit_CPre_pw3			Variate piecewise of credit_score	median(0,credit_score-630,680-630)	0.00535	0.00006	<.0001
vcredit_CPre_pw4			Variate piecewise of credit_score	median(0,credit_score-680,720-680)	0.00276	0.000075	<.0001
vcredit_CPre_pw5			Variate piecewise of credit_score	median(0,credit_score-720,760-720)	0.00169	0.000089	<.0001
vcredit_CPre_pw6			Variate piecewise of credit_score	median(0,credit_score-760,800-760)	-0.00074	0.000115	<.0001
vhpa2yb_CPre_pw1			Variate piecewise of hpa2y_blended_r <sup>6</sup> (2 year house price appreciation)	median(0,hpa2y_blended_r-85,100-85)	0.0363	0.000334	<.0001
vhpa2yb_CPre_pw2			Variate piecewise of hpa2y_blended_r <sup>6</sup> (2 year house price appreciation)	median(0,hpa2y_blended_r-100,106-100)	0.099	0.000471	<.0001
vhpa2yb_CPre_pw3			Variate piecewise of hpa2y_blended_r <sup>6</sup> (2 year house price appreciation)	median(0,hpa2y_blended_r-106,111-106)	0.0352	0.000364	<.0001
vhpa2yb_CPre_pw4			Variate piecewise of hpa2y_blended_r <sup>6</sup> (2 year house price appreciation)	median(0,hpa2y_blended_r-111,122-111)	0.0335	0.00017	<.0001
vhpa2yb_CPre_pw5			Variate piecewise of hpa2y_blended_r <sup>6</sup> (2 year house price appreciation)	median(0,hpa2y_blended_r-122,150-122)	0.0335	0.000117	<.0001
vltv_CPRE_pw1			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,78-0)	-0.00681	0.000104	<.0001
vltv_CPRE_pw2			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-78,85-78)	0.00883	0.00038	<.0001
vltv_CPRE_pw3			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-85,87-85)	-0.0141	0.00119	<.0001
vltv_CPRE_pw4			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-87,91-87)	-0.0322	0.000579	<.0001
vltv_CPRE_pw5			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-91,94-91)	-0.0575	0.000704	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 92

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vltv_CPRE_pw6			Variate piecewise of $ltv\_i\_r^7$ (loan-to-value)	median(0,ltv_i_r-94,100-94)	-0.00175	0.000945	0.0643
vueblend_CPre_pw1			Variate piecewise of $ue\_blended\_r^8$ (unemployment rate)	(0,ue_blended_r-0,450-0)	-0.00087	9.56E-06	<.0001
vueblend_CPre_pw3			Variate piecewise of $ue\_blended\_r^8$ (unemployment rate)	(0,ue_blended_r-700,730-700)	-0.00539	0.000085	<.0001
vueblend_CPre_pw4			Variate piecewise of $ue\_blended\_r^8$ (unemployment rate)	(0,ue_blended_r-730, 1000-730)	-0.00101	0.000014	<.0001
vrefiincent_CPre_pw1			Variate piecewise of $refi\_incent2\_r^{13}$ (refinance incentive)	median(0,refi_incent_r-0,115-0)	0.0245	0.000059	<.0001
vrefiincent_CPre_pw2			Variate piecewise of $refi\_incent2\_r^{13}$ (refinance incentive)	median(115,refi_incent_r-115,150-115)	0.00796	0.000059	<.0001
vrefiincent_CPre_pw3			Variate piecewise of $refi\_incent2\_r^{13}$ (refinance incentive)	median(150,refi_incent_r-150,200-150)	-0.00927	0.000105	<.0001
vratiotmptei_CPre_pw1			Variate piecewise of $ratio\_tmp\_tei$ (front-end ratio)	median(0,ratio_tmp_tei-0,5-0)	0.0294	0.000753	<.0001
vratiotmptei_CPre_pw2			Variate piecewise of $ratio\_tmp\_tei$ (front-end ratio)	median(0,ratio_tmp_tei-5,18-5)	-0.0168	0.000256	<.0001
vratiotmptei_CPre_pw3			Variate piecewise of $ratio\_tmp\_tei$ (front-end ratio)	median(0,ratio_tmp_tei-18,47-18)	-0.0101	0.000078	<.0001
vratiotmptei_CPre_pw4			Variate piecewise of $ratio\_tmp\_tei$ (front-end ratio)	median(0,ratio_tmp_tei-47,100-47)	0.00495	0.000349	<.0001
vdeltaUEinit_CPre_pw1			Variate piecewise of $\Delta UEinit\_r^4$ (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-0,88-0)	0.00401	0.000054	<.0001
vdeltaUEinit_CPre_pw2			Variate piecewise of $\Delta UEinit\_r^4$ (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-88,96-88)	0.01	0.00033	<.0001
vdeltaUEinit_CPre_pw3			Variate piecewise of $\Delta UEinit\_r^4$ (change in unemployment rate from policy	median(0,deltaUEinit_r-96,100-96)	0.00638	0.000742	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 93

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			inception to current)				
vdeltaUEinit_CPre_pw4			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-100,126-100)	0.00989	0.000103	<.0001
vdeltaUEinit_CPre_pw5			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-126,200-126)	0.00387	0.000045	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	-0.3604	0.00548	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	-0.423	0.00626	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	-0.4063	0.00677	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	-0.3209	0.00699	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	-0.3101	0.00735	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	-0.3007	0.00779	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 7	-0.2733	0.00399	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	-0.5567	0.00808	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L02	L02	Interaction of categorical of prior_default_cnt	prior_default_cnt = 2; cx_time = 2	-0.6267	0.00975	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 94

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
mpriordef_cpre*mtimesinceD_CPRES	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	-0.5928	0.0109	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	-0.4662	0.0114	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	-0.4512	0.0123	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 6	-0.4505	0.0133	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 7	-0.4365	0.00553	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	-0.7787	0.0062	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	-0.8411	0.00778	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	-0.7777	0.00891	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	-0.6544	0.00958	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	-0.5845	0.0102	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	-0.571	0.0112	<.0001
mpriordef_cpre*mtimesinceD_CPRES	L03	L07	Interaction of categorical of	prior_default_cnt >= 3; cx_time <= 7	-0.5524	0.00518	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 95

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			prior_default_cnt and categorical of cx_time <sup>1</sup>				
mpriordef_cpriemtimesinceD_CPRI	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vtimesinceD_CPRIpw1			Variate piecewise of prior_default_cnt	median(0,cx_time-7,19-7)	0.00547	0.00053	<.0001
vtimesinceD_CPRIpw2			Variate piecewise of prior_default_cnt	median(0,cx_time-19,35-19)	0.00312	0.000587	<.0001
vloanraw_CPRIpw1			Variate piecewise of loansize_raw	median(0,loansize_raw-0,57000-0)	0.000011	1.11E-07	<.0001
vloanraw_CPRIpw2			Variate piecewise of loansize_raw	median(0,loansize_raw-57000,159000-57000)	5.99E-06	1.81E-08	<.0001
vloanraw_CPRIpw3			Variate piecewise of loansize_raw	median(0,loansize_raw-159000,345000-159000)	2.73E-06	1.49E-08	<.0001
vloanraw_CPRIpw4			Variate piecewise of loansize_raw	median(0,loansize_raw-345000,600000-345000)	1.80E-06	2.51E-08	<.0001
mDeltaTY1Init_CPRI	L01		Categorical of DeltaTY1Init (Change in 1 yr Treasury policy inception to current)	DeltaTY1Init < 0.17	-0.5367	0.00257	<.0001
mDeltaTY1Init_CPRI	L02		Categorical of DeltaTY1Init (Change in 1 yr Treasury policy inception to current)	DeltaTY1Init > 2.30	0.1908	0.00151	<.0001
mDeltaTY1Init_CPRI	Z00		Categorical of DeltaTY1Init (Change in 1 yr Treasury policy inception to current)	base level: else			

**Current Transition Model Parameters – FRM30NSR C\_CXS**

The model parameters for the FRM30NSR current to self-cure transition are shown below.

*Table 32: Current to Self-Cure Transition FRM30NSR Model Parameters*

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-3.8506	0.013	<.0001
mseason	1		Categorical of season	season = "winter"	0.3593	0.00227	<.0001
mseason	2		Categorical of season	season = "spring"	-0.1364	0.00247	<.0001
mseason	3		Categorical of season	season = "summer"	0.0936	0.00239	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 96

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mseason	4		Categorical of season	base level: season = "fall"			
mfrst_tm_by	1		Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.0648	0.00188	<.0001
mfrst_tm_by	2		Categorical of frst_tm_by (first-time buyer)	base level: else			
mdpa_govt	LGovt		Categorical of dpa (down payment assistance)	dpa = "govt"	0.0896	0.00516	<.0001
mdpa_govt	ZOthr		Categorical of dpa (down payment assistance)	base level: else			
mdpa_rel	LRela		Categorical of dpa (down payment assistance)	dpa = "Relative"	0.0875	0.00217	<.0001
mdpa_rel	ZOthr		Categorical of dpa (down payment assistance)	base level: else			
mcalperiod_CCXS	L200604		Categorical of Calendar Period	if period < 200604 then mcalperiod_CCXS = "L200604"	-2.4253	0.00501	<.0001
mcalperiod_CCXS	Z		Categorical of Calendar Period	base level: else			
vpriordef_CCXS_pw1			Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	0.1077	0.000623	<.0001
mperiodnbr_cCXS	L02		Categorical of period_number	period_number = 2	-0.1175	0.00561	<.0001
mperiodnbr_cCXS	L03		Categorical of period_number	period_number = 3	0.1296	0.00501	<.0001
mperiodnbr_cCXS	L04		Categorical of period_number	period_number = 4	0.1751	0.00481	<.0001
mperiodnbr_cCXS	L05		Categorical of period_number	period_number = 5	0.1716	0.00478	<.0001
mperiodnbr_cCXS	L06		Categorical of period_number	period_number = 6	0.1857	0.00466	<.0001
mperiodnbr_cCXS	L07		Categorical of period_number	period_number = 7	0.1091	0.00473	<.0001
mperiodnbr_cCXS	Z08		Categorical of period_number	base level: else			
vperiodnbr_CCXS_pw1			Variate piecewise of period_number	median(0,period_number-8,36-8)	-0.0248	0.000145	<.0001
vperiodnbr_CCXS_pw2			Variate piecewise of period_number	median(0,period_number-36,53-36)	-0.0133	0.000293	<.0001
vperiodnbr_CCXS_pw3			Variate piecewise of period_number	median(0,period_number-53,76-53)	-0.0123	0.000356	<.0001
vperiodnbr_CCXS_pw4			Variate piecewise of period_number	median(0,period_number-76,86-76)	-0.0141	0.00103	<.0001
vcredit_CCXS_pw1			Variate piecewise of credit_score	median(0,credit_score-450,500-450)	-0.00096	0.00012	<.0001
vcredit_CCXS_pw2			Variate piecewise of credit_score	median(0,credit_score-500,630-500)	-0.00028	0.000051	<.0001
vcredit_CCXS_pw3			Variate piecewise of credit_score	median(0,credit_score-630,680-630)	-0.00646	0.000063	<.0001
vcredit_CCXS_pw4			Variate piecewise of credit_score	median(0,credit_score-680,800-680)	-0.00867	0.000053	<.0001



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 97

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mRatioTmpTei_CCXS	L00		Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.1904	0.00956	<.0001
mRatioTmpTei_CCXS	Z00		Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_CCXS_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-5,30-5)	0.00873	0.000164	<.0001
vratiotmptei_CCXS_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-30,45-30)	0.00287	0.000272	<.0001
vratiotmptei_CCXS_pw3			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-45,57-45)	-0.0102	0.00208	<.0001
vhpa2yb_CCXS_pw1			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-90,105-90)	0.00957	0.00023	<.0001
vhpa2yb_CCXS_pw2			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-105,117-105)	0.00161	0.000258	<.0001
vhpa2yb_CCXS_pw3			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-117,125-117)	-0.00925	0.000609	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	2.4026	0.00354	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	2.1352	0.00449	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	1.849	0.00572	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	1.7271	0.00662	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	1.3752	0.00861	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	1.2114	0.01	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 7	1.1687	0.011	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 98

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_ccxs*mtimesinceD_CCXS	L01	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time >= 8	1.1585	0.00713	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	2.8387	0.00412	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	2.5664	0.0054	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	2.2554	0.00715	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	2.1172	0.00852	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	1.7547	0.0113	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 6	1.5833	0.0134	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 7	1.5204	0.015	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L02	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time >= 8	1.3836	0.00888	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	3.1201	0.00331	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	2.7787	0.00401	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L03	L03	Interaction of categorical of prior_default_cnt	prior_default_cnt >= 3; cx_time = 3	2.421	0.00508	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 99

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
mpriordef_ccxs*mtimesinceD_CCXS	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	2.2679	0.00599	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	1.8554	0.00795	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	1.6652	0.00947	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L03	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 7	1.564	0.0109	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	L03	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time >= 8	1.386	0.00761	<.0001
mpriordef_ccxs*mtimesinceD_CCXS	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vtimesinceD_CCXS_pw1			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-8,13-8)	-0.0893	0.00186	<.0001
vtimesinceD_CCXS_pw2			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-13,40-13)	-0.0221	0.000705	<.0001
vloanraw_CCXS_pw1			Variate piecewise of loansize_raw	median(0,loansize_raw-0,57000-0)	-9.24E-06	2.14E-07	<.0001
vloanraw_CCXS_pw2			Variate piecewise of loansize_raw	median(0,loansize_raw-57000,159000-57000)	-2.42E-06	2.70E-08	<.0001
vdeltaUEinit_CCXS_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-45,100-45)	0.000246	0.000065	0.0002
vdeltaUEinit_CCXS_pw2			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-100,200-100)	0.00141	0.000037	<.0001

### Current Transition Model Parameters – FRM30NSR C\_D

The model parameters for the FRM30NSR current to default transition are shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 100

Table 33: Current to Default Transition FRM30NSR Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-3.0984	0.0103	<.0001
mseason	1		Categorical of season	season = "winter"	-0.2545	0.00117	<.0001
mseason	2		Categorical of season	season = "spring"	-0.4076	0.00118	<.0001
mseason	3		Categorical of season	season = "summer"	-0.1892	0.00113	<.0001
mseason	4		Categorical of season	base level: season = "fall"			
mjudicial	1		Categorical of judicial (judicial state)	judicial = 1 (yes)	0.0413	0.000869	<.0001
mjudicial	2		Categorical of judicial (judicial state)	base level: else			
myslope_CD	L01		Categorical of ycslope_r <sup>9</sup> (Yield Curve Slope)	100<=ycslope_r <sup>9</sup> <=200	0.0278	0.000992	<.0001
myslope_CD	Z00		Categorical of ycslope_r <sup>9</sup> (Yield Curve Slope)	base level: else			
mfrst_tm_by	1		Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.0676	0.0012	<.0001
mfrst_tm_by	2		Categorical of frst_tm_by (first-time buyer)	base level: else			
mrnc_ind	2		Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind = "N"	0.0783	0.0017	<.0001
mrnc_ind	3		Categorical of rfnc_ind (refinanced loan indicator)	base level: else			
mcalperiod_CD	L200604		Categorical of Calendar Period	period < 200604	-0.9721	0.00186	<.0001
mcalperiod_CD	Z		Categorical of Calendar Period	base level: else			
mperiodnbr_CD	L02		Categorical of period_number	period_number = 2	-0.4396	0.00282	<.0001
mperiodnbr_CD	L03		Categorical of period_number	period_number = 3	-0.0512	0.00252	<.0001
mperiodnbr_CD	L04		Categorical of period_number	period_number = 4	0.0376	0.00251	<.0001
mperiodnbr_CD	L05		Categorical of period_number	period_number = 5	0.0783	0.00253	<.0001
mperiodnbr_CD	L06		Categorical of period_number	period_number = 6	0.0963	0.00257	<.0001
mperiodnbr_CD	L07		Categorical of period_number	period_number = 7	0.0636	0.00269	<.0001
mperiodnbr_CD	Z08		Categorical of period_number	base level: else			
vperiodnbr_CD_pw1			Variate piecewise of period_number	median(0,period_number-8,40-8)	-0.0212	0.000109	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 101

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vperiodnbr_CD_pw2			Variate piecewise of period_number	median(0,period_number-40,53-40)	-0.00978	0.000246	<.0001
vperiodnbr_CD_pw3			Variate piecewise of period_number	median(0,period_number-53,68-53)	-0.0225	0.000726	<.0001
vperiodnbr_CD_pw4			Variate piecewise of period_number	median(0,period_number-68,108-68)	-0.0141	0.000878	<.0001
vcredit_CD_pw1			Variate piecewise of credit_score	median(0,credit_score-450,530-450)	0.00262	0.000034	<.0001
vcredit_CD_pw2			Variate piecewise of credit_score	median(0,credit_score-530,630-530)	-0.00289	0.00003	<.0001
vcredit_CD_pw3			Variate piecewise of credit_score	median(0,credit_score-630,680-630)	-0.00924	0.000039	<.0001
vcredit_CD_pw4			Variate piecewise of credit_score	median(0,credit_score-680,720-680)	-0.0102	0.000072	<.0001
vcredit_CD_pw5			Variate piecewise of credit_score	median(0,credit_score-720,760-720)	-0.00836	0.000115	<.0001
vcredit_CD_pw6			Variate piecewise of credit_score	median(0,credit_score-760,800-760)	-0.0113	0.000193	<.0001
vdeltaUEinit_CD_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-50,100-50)	0.00303	0.000036	<.0001
vdeltaUEinit_CD_pw2			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-100,200-100)	0.00284	0.00002	<.0001
mRatioTmpTei_cd	L00		Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.411	0.00441	<.0001
mRatioTmpTei_cd	Z00		Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_CD_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	0.0184	0.000131	<.0001
vratiotmptei_CD_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	0.0108	0.000113	<.0001
vpriordef_CD_pw1			Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	0.0716	0.000409	<.0001
mperiodnbr_CD*mpriordef_ind	L02	L01	Interaction of categorical period number and categorical prior default count	period number =2; prior_default_cnt NE 0	-1.4404	0.1832	<.0001
mperiodnbr_CD*mpriordef_ind	L03	L01	Interaction of categorical period number and categorical prior default count	period number =3; prior_default_cnt NE 0	-0.5828	0.0121	<.0001
mperiodnbr_CD*mpriordef_ind	L04	L01	Interaction of categorical period number and categorical prior default count	period number =4; prior_default_cnt NE 0	-0.2759	0.00717	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 102

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			number and categorical prior default count				
mperiodnbr_CD*mpriordef_ind	L05	L01	Interaction of categorical period number and categorical prior default count	period number =5; prior_default_cnt NE 0	-0.1573	0.00576	<.0001
mperiodnbr_CD*mpriordef_ind	L06	L01	Interaction of categorical period number and categorical prior default count	period number =6; prior_default_cnt NE 0	-0.0846	0.00518	<.0001
mperiodnbr_CD*mpriordef_ind	L07	L01	Interaction of categorical period number and categorical prior default count	period number =7; prior_default_cnt NE 0	-0.0444	0.00496	<.0001
mperiodnbr_CD*mpriordef_ind	Z08	Z00	Interaction of categorical period number and categorical prior default count	base level: period number = else; prior_default_cnt = else			
vperiodnbr_CD_pw1*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	period number piecewise; prior_default_cnt NE 0	0.00564	0.00012	<.0001
vperiodnbr_CD_pw3*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	period number piecewise; prior_default_cnt NE 0	0.0163	0.000726	<.0001
vperiodnbr_CD_pw4*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	period number piecewise; prior_default_cnt NE 0	0.0147	0.000896	<.0001
vperiodnbr_CD_pw*mpriordef_ind	Z00		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	period number piecewise; base prior_default_cnt else			
vsato_cd_pw1			Variate piecewise of sato (spread at origination)	median(0,sato-(-2.5),-1-(-2.5))	0.0174	0.0017	<.0001
vsato_cd_pw2			Variate piecewise of sato (spread at origination)	median(0,sato-(-.1),7-(-.1))	0.2952	0.00174	<.0001
vsato_cd_pw3			Variate piecewise of sato (spread at origination)	median(0,sato-.7,2.5-.7)	0.2613	0.00307	<.0001
vltv_CD_pw1			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-25,70-25)	0.0039	0.000159	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 103

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vltv_CD_pw2			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-70,88-70)	0.00692	0.00014	<.0001
vltv_CD_pw3			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-88,97-88)	0.024	0.000242	<.0001
mhpa2yb_CD	L00		Categorical of hpa2y_bledned_r <sup>6</sup>	hpa2y_bledned_r = 0	-1.4105	0.0109	<.0001
mhpa2yb_CD	Z00		Categorical of hpa2y_bledned_r <sup>6</sup>	base level: else			
vhpa2yb_CD_pw1			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-50,85-50)	-0.0102	0.000191	<.0001
vhpa2yb_CD_pw2			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-85,100-85)	-0.0071	0.00015	<.0001
vhpa2yb_CD_pw3			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-100,125-100)	-0.00203	0.000074	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	2.5023	0.00237	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	2.2412	0.00265	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	1.9979	0.00305	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	1.6817	0.00367	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	1.4861	0.00426	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	1.3296	0.00484	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 7	1.239	0.00539	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time >= 8	1.0607	0.00351	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 104

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CD*mtimesinceD_CD	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	2.8761	0.00267	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	2.6083	0.00323	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	2.3777	0.0039	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	2.0497	0.00485	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	1.8308	0.00578	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 6	1.649	0.00673	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 7	1.5318	0.00764	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time >= 8	1.2525	0.00455	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	3.1059	0.00249	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	2.8098	0.00281	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	2.5547	0.00322	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L04	Interaction of categorical of prior_default_cnt	prior_default_cnt >= 3; cx_time = 4	2.1901	0.00385	<.0001



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 105

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
mpriordef_CD*mtimesinceD_CD	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	1.945	0.00451	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	1.7462	0.0052	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 7	1.6075	0.00591	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time >= 8	1.2538	0.00403	<.0001
mpriordef_CD*mtimesinceD_CD	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vtimesincd_CD_pw1			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-8,24-8)	-0.0586	0.000397	<.0001
vtimesincd_CD_pw2			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-24,40-24)	-0.00787	0.000875	<.0001

### Current Transition Model Parameters – FRM30SR C\_CXS

The model parameters for the FRM30SR current to self-cure transition are shown below.

*Table 34: Current to Self-Cure Transition FRM30SR Model Parameters*

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-4.7021	0.0543	<.0001
mseason	1		Categorical of season	season = "winter"	0.2802	0.0055	<.0001
mseason	2		Categorical of season	season = "spring"	-0.1122	0.00589	<.0001
mseason	3		Categorical of season	season = "summer"	0.215	0.00548	<.0001
mseason	4		Categorical of season	base level: season = "fall"			
mcalperiod_CCXS	L199501		Categorical of Calendar Period	period < 199501	-3.6466	0.0543	<.0001
mcalperiod_CCXS	L200104		Categorical of Calendar Period	period < 200104	-2.8357	0.0207	<.0001
mcalperiod_CCXS	L200604		Categorical of Calendar Period	period < 200604	-1.9816	0.0144	<.0001
mcalperiod_CCXS	Z201800		Categorical of Calendar Period	base level: else			

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 106

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mltv	L00		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r=.	0.2421	0.0127	<.0001
mltv	Z01		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
mperiodnbr_CCXS	L02		Categorical of period_number	period_number <= 2	-0.0644	0.013	<.0001
mperiodnbr_CCXS	L03		Categorical of period_number	period_number = 3	0.000672	0.0125	0.9571
mperiodnbr_CCXS	L04		Categorical of period_number	period_number = 4	0.0448	0.0119	0.0002
mperiodnbr_CCXS	L05		Categorical of period_number	period_number = 5	0.0538	0.0117	<.0001
mperiodnbr_CCXS	L06		Categorical of period_number	period_number = 6	0.0808	0.0113	<.0001
mperiodnbr_CCXS	L07		Categorical of period_number	period_number = 7	-0.0571	0.0119	<.0001
mperiodnbr_CCXS	Z00		Categorical of period_number	base level: else			
vperiodnbr_CCXS_pw1			Variate piecewise of period_number	median(0,period_number-8,30-8)	-0.0231	0.000427	<.0001
vperiodnbr_CCXS_pw2			Variate piecewise of period_number	median(0,period_number-30,54-30)	-0.00948	0.000523	<.0001
vperiodnbr_CCXS_pw3			Variate piecewise of period_number	median(0,period_number-54,70-54)	-0.0159	0.00123	<.0001
vperiodnbr_CCXS_pw4			Variate piecewise of period_number	median(0,period_number-70,100-70)	-0.0127	0.00133	<.0001
mcredit_score_CCXS	L00		Categorical of credit_score	credit_score=0	-0.3466	0.0182	<.0001
mcredit_score_CCXS	Z00		Categorical of credit_score	base level: else			
vcredit_CCXS_pw1			Variate piecewise of credit_score	median(0,credit_score-525,680-525)	-0.00211	0.000156	<.0001
vcredit_CCXS_pw2			Variate piecewise of credit_score	median(0,credit_score-680,745-680)	-0.00971	0.000441	<.0001
vcredit_CCXS_pw3			Variate piecewise of credit_score	median(0,credit_score-745,800-745)	-0.0114	0.00115	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	2.4611	0.00849	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	2.1542	0.0107	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	1.8838	0.0135	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	1.7486	0.0156	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 107

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CCXS*mtimesinceD_CCXS	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	1.4575	0.0196	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	1.301	0.0225	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 7	1.3	0.0244	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 8	1.1757	0.0276	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 9	1.0627	0.0315	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 10	1.0084	0.0339	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 11	1.0759	0.0356	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 12	0.9916	0.0388	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L01	L13	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time >= 13	0.6963	0.0172	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	2.9975	0.00968	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	2.7001	0.0127	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L03	Interaction of categorical of prior_default_cnt	prior_default_cnt = 2; cx_time = 3	2.3735	0.017	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 108

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
mpriordef_CCXS*mtimesinceD_CCXS	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	2.2381	0.0202	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	1.9049	0.0263	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 6	1.7687	0.0305	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 7	1.6494	0.0355	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 8	1.5648	0.0399	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 9	1.3606	0.0478	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 10	1.3787	0.0504	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 11	1.3485	0.0552	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 12	1.2394	0.0616	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L02	L13	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time >= 13	0.9914	0.0263	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	3.1766	0.00896	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L02	Interaction of categorical of	prior_default_cnt >= 3; cx_time = 2	2.8109	0.0105	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 109

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			prior_default_cnt and categorical of cx_time <sup>1</sup>				
mpriordef_CCXS*mtimesinceD_CCXS	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	2.484	0.0129	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	2.3185	0.0152	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	1.9453	0.0196	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	1.7853	0.0228	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 7	1.7043	0.026	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 8	1.5388	0.0303	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 9	1.3916	0.0354	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 10	1.3693	0.0382	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 11	1.235	0.044	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 12	1.143	0.0491	<.0001
mpriordef_CCXS*mtimesinceD_CCXS	L03	L13	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time >= 13	0.8825	0.023	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 110

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CCXS*mtimesinceD_CCXS	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vpriordef_CCXS_pw1			Variate of prior_default_cnt	median(0,prior_default_cnt-2,10-2)	0.1254	0.00197	<.0001
vpriordef_CCXS_pw2			Variate of prior_default_cnt	median(0,prior_default_cnt-10,15-10)	0.1105	0.00635	<.0001
vhpa2yb_CCXS_pw1			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r <sup>6</sup> -85,130-85)	-0.00138	0.000252	<.0001
vratiotmptei_CCXS_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-5,30-5)	-0.00509	0.000321	<.0001
vratiotmptei_CCXS_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-30,55-30)	0.00462	0.000976	<.0001
vltv_CCXS_pw1			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-78,85-78)	0.00555	0.00115	<.0001
vltv_CCXS_pw2			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-85,88-85)	0.0116	0.00301	0.0001
vltv_CCXS_pw3			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-88,92-88)	-0.0337	0.00251	<.0001
vltv_CCXS_pw4			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-92,95-92)	0.1103	0.00327	<.0001
vloanraw_ccxs_pw1			Variate piecewise of loansize_raw	median(0,loansize_raw-0,57000-0)	-2.53E-06	8.64E-07	0.0034
vloanraw_ccxs_pw2			Variate piecewise of loansize_raw	median(0,loansize_raw-57000,159000-57000)	-2.36E-06	7.49E-08	<.0001
vloanraw_ccxs_pw3			Variate piecewise of loansize_raw	median(0,loansize_raw-159000,345000-159000)	-3.07E-07	4.71E-08	<.0001
vdeltaUEinit_CCXS_pw1			Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-20,95-20)	0.00125	0.000159	<.0001
vSBOI_CCXS_pw1			Variate piecewise of small business optimism index	median(0,mSBOI-85,100-85)	-0.00521	0.000832	<.0001
vSBOI_CCXS_pw2			Variate piecewise of small business optimism index	median(0,mSBOI-100,108-100)	-0.0238	0.00124	<.0001

Current Transition Model Parameters – FRM30SR C\_D

The model parameters for the FRM30SR current to default transition are shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 111

Table 35: Current to Default Transition FRM30SR Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-3.45	0.0395	<.0001
mseason	1		Categorical of season	season = "winter"	-0.2039	0.00264	<.0001
mseason	2		Categorical of season	season = "spring"	-0.3661	0.00267	<.0001
mseason	3		Categorical of season	season = "summer"	-0.1643	0.00256	<.0001
mseason	4		Categorical of season	base level: season = "fall"			
mjudicial	1		Categorical of judicial (judicial state)	judicial = 1 (yes)	0.0239	0.00204	<.0001
mjudicial	2		Categorical of judicial (judicial state)	base level: else			
myslope_CD	L01		Categorical of Yield Curve Slope	1<=ycslope<=2	0.2161	0.00311	<.0001
myslope_CD	Z00		Categorical of Yield Curve Slope	base level: else			
mcalperiod_CD	L199504		Categorical of Calendar Period	period < 199504	-2.0523	0.0119	<.0001
mcalperiod_CD	L200104		Categorical of Calendar Period	period < 200104	-1.2062	0.00653	<.0001
mcalperiod_CD	L200604		Categorical of Calendar Period	period < 200604	-0.4816	0.00453	<.0001
mcalperiod_CD	Z201800		Categorical of Calendar Period	base level: else			
mperiodnbr_CD	L02		Categorical of period_number	period_number = 2	-0.344	0.00592	<.0001
mperiodnbr_CD	L03		Categorical of period_number	period_number = 3	-0.0895	0.00533	<.0001
mperiodnbr_CD	Z00		Categorical of period_number	base level: else			
vperiodnbr_CD_pw1			Variate piecewise of period_number	median(0,period_number-3,45-3)	-0.0163	0.000132	<.0001
vperiodnbr_CD_pw2			Variate piecewise of period_number	median(0,period_number-45,70-45)	-0.00911	0.000332	<.0001
vperiodnbr_CD_pw3			Variate piecewise of period_number	median(0,period_number-70,108-70)	-0.0103	0.00067	<.0001
Mcredit_score_CD	L00		Categorical of credit_score	credit_score=0	-0.3147	0.0072	<.0001
Mcredit_score_CD	Z00		Categorical of credit_score	base level: else			
vcredit_CD_pw1			Variate piecewise of credit_score	median(0,credit_score-600,630-600)	-0.00283	0.000369	<.0001
vcredit_CD_pw2			Variate piecewise of credit_score	median(0,credit_score-630,680-630)	-0.0069	0.000246	<.0001
vcredit_CD_pw3			Variate piecewise of credit_score	median(0,credit_score-680,745-680)	-0.00848	0.000255	<.0001
vcredit_CD_pw4			Variate piecewise of credit_score	median(0,credit_score-745,800-745)	-0.0127	0.000612	<.0001
vratiotmptei_CD_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	-0.00922	0.000161	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 112

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vratiotmptei_CD_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	0.02	0.000572	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	2.5549	0.00414	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	2.2887	0.00509	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	2.0749	0.0061	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	1.7913	0.00755	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	1.5947	0.00896	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	1.4629	0.0102	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 7	1.3853	0.0114	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 8	1.2309	0.0133	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 9	1.1422	0.0149	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 10	1.0444	0.0165	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 11	1.03	0.0178	<.0001



**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 113

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CD*mtimesinceD_CD	L01	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 12	0.992	0.0195	<.0001
mpriordef_CD*mtimesinceD_CD	L01	L13	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time >= 13	0.9391	0.0127	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	3.0547	0.00498	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	2.7864	0.00635	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	2.596	0.00784	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	2.2774	0.0101	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	2.0712	0.0122	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 6	1.8743	0.0146	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 7	1.8225	0.0163	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 8	1.6554	0.0193	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 9	1.5489	0.0219	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L10	Interaction of categorical of prior_default_cnt	prior_default_cnt = 2; cx_time = 10	1.4579	0.0245	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 114

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
mpriordef_CD*mtimesinceD_CD	L02	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 11	1.3738	0.0274	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 12	1.2643	0.031	<.0001
mpriordef_CD*mtimesinceD_CD	L02	L13	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time >= 13	1.215	0.0164	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	3.2329	0.00464	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	2.9459	0.00538	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	2.7262	0.00634	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	2.38	0.00788	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	2.1628	0.00946	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	1.9521	0.0112	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 7	1.8451	0.0128	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 8	1.6383	0.0154	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L09	Interaction of categorical of	prior_default_cnt >= 3; cx_time = 9	1.5312	0.0175	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 115

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			prior_default_cnt and categorical of cx_time <sup>1</sup>				
mpriordef_CD*mtimesinceD_CD	L03	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 10	1.4114	0.0199	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 11	1.3454	0.022	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 12	1.2361	0.0251	<.0001
mpriordef_CD*mtimesinceD_CD	L03	L13	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time >= 13	1.095	0.015	<.0001
mpriordef_CD*mtimesinceD_CD	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vtimesinced_CD_pw1			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-12,24-12)	-0.0322	0.00179	<.0001
vtimesinced_CD_pw2			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-24,40-24)	-0.0203	0.00224	<.0001
vpriordef_CD_pw1			Variate of prior_default_cnt	median(0,prior_default_cnt-2,10-2)	0.1261	0.000999	<.0001
vsato_cd_pw1			Variate piecewise of sato (spread at origination)	median(-2,sato,0)	-0.0648	0.00508	<.0001
vsato_cd_pw2			Variate piecewise of sato (spread at origination)	median(sato,0,2)	0.2918	0.00354	<.0001
vdeltaUEinit_CD_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-100,200-100)	0.00308	0.000049	<.0001
vUEblend_CD_pw1			Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-400,1000-400)	0.000115	8.06E-06	<.0001
mltv	L00		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r=.	0.2346	0.0273	<.0001
mltv	Z01		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 116

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vltv_CD_pw1			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-0,62-0)	0.0023	0.000464	<.0001
vltv_CD_pw2			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-62,84-62)	0.000954	0.000239	<.0001
vltv_CD_pw3			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-86,92-86)	0.0309	0.000623	<.0001
vltv_CD_pw4			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-92,95-92)	0.0748	0.00162	<.0001
vltv_CD_pw5			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-95,97-95)	0.0712	0.00328	<.0001
vltv_CD_pw6			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-97,100-97)	0.0917	0.00536	<.0001
vhpa2yb_CD_pw1			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-0,85-0)	0.00137	0.000334	<.0001
vhpa2yb_CD_pw2			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-85,95-85)	-0.0195	0.000514	<.0001
vhpa2yb_CD_pw3			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-95,113-95)	-0.0182	0.000296	<.0001
vhpa2yb_CD_pw4			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-113,118-113)	-0.00307	0.000842	0.0003
vhpa2yb_CD_pw5			Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-118,130-118)	-0.0118	0.000565	<.0001
vSBOI_CD_pw1			Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-85,100-85)	-0.00391	0.000632	<.0001
vSBOI_cd_pw2			Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-100,108-100)	-0.0417	0.000718	<.0001
vCCI_CD_pw1			Variate piecewise of CCI (consumer confidence index)	median(0,mCCI-50,100-50)	0.000593	0.000148	<.0001

### Current Transition Model Parameters – FRM30SR C\_END

The model parameters for the FRM30SR current to end (refinance or payoff) transition are shown below.

Table 36: Current to End Transition FRM30SR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-14.4717	0.1386	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 117

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mseason	1	Categorical of season	season = "winter"	-0.0957	0.00398	<.0001
mseason	2	Categorical of season	season = "spring"	-0.1094	0.00405	<.0001
mseason	3	Categorical of season	season = "summer"	-0.117	0.00398	<.0001
mseason	4	Categorical of season	base level: season = "fall"			
mcalperiod_CEND	L200104	Categorical of Calendar Period	period < 200104	0.2845	0.00773	<.0001
mcalperiod_CEND	L200604	Categorical of Calendar Period	period < 200604	0.4177	0.00645	<.0001
mcalperiod_CEND	Z201800	Categorical of Calendar Period	base level: else			
myslope_CEND	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope>=9	-0.8421	0.00512	<.0001
myslope_CEND	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.2115	0.038	<.0001
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.134	0.0032	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mperiodnbr_cend	L02	Categorical of period_number	period_number <= 2	-0.0648	0.0082	<.0001
mperiodnbr_cend	L03	Categorical of period_number	period_number = 3	0.6182	0.00674	<.0001
mperiodnbr_cend	L04	Categorical of period_number	period_number = 4	0.802	0.00639	<.0001
mperiodnbr_cend	L05	Categorical of period_number	period_number = 5	0.677	0.0065	<.0001
mperiodnbr_cend	L06	Categorical of period_number	period_number = 6	0.4656	0.0068	<.0001
mperiodnbr_cend	L07	Categorical of period_number	period_number = 7	0.318	0.00713	<.0001
mperiodnbr_cend	Z08	Categorical of period_number	base level: else			
vperiodnbr_cend_pw1		Variate piecewise of period_number	median(0,period_number-8,19-8)	-0.0405	0.000691	<.0001
vperiodnbr_cend_pw2		Variate piecewise of period_number	median(0,period_number-19,31-19)	-0.0801	0.000818	<.0001
vperiodnbr_cend_pw3		Variate piecewise of period_number	median(0,period_number-31,40-31)	-0.0489	0.00165	<.0001
vperiodnbr_cend_pw4		Variate piecewise of period_number	median(0,period_number-40,49-40)	-0.0798	0.00234	<.0001
vperiodnbr_cend_pw5		Variate piecewise of period_number	median(0,period_number-49,108-49)	-0.0587	0.00151	<.0001
vrefiincnt_cend_pw1		Variate piecewise of refi_incent2_r <sup>13</sup>	median(0,refi_incent2_r-0,100-0)	0.0399	0.000579	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 118

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(refinance incentive)				
vrefiincend_pw2		Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent2_r-100,120-100)	0.1111	0.000297	<.0001
vrefiincend_pw3		Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent2_r-120,135-120)	0.0384	0.000402	<.0001
vrefiincend_pw4		Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent2_r-135,155-135)	0.0419	0.000439	<.0001
vrefiincend_pw5		Variate piecewise of refi_incent2_r <sup>13</sup> (refinance incentive)	median(0,refi_incent2_r-155,200-155)	0.0104	0.000518	<.0001
mcredit_score_CEND	L00	Categorical of credit_score	credit_score=0	0.2694	0.0733	0.0002
mcredit_score_CEND	Z00	Categorical of credit_score	base level: else			
vcrcend_pw1		Variate piecewise of credit_score	median(0,credit_score-450,500-450)	0.00289	0.00161	0.0732
vcrcend_pw2		Variate piecewise of credit_score	median(0,credit_score-500,630-500)	0.00181	0.000271	<.0001
vcrcend_pw3		Variate piecewise of credit_score	median(0,credit_score-630,680-630)	-0.00263	0.000354	<.0001
vcrcend_pw4		Variate piecewise of credit_score	median(0,credit_score-680,745-680)	-0.00188	0.00031	<.0001
vcrcend_pw5		Variate piecewise of credit_score	median(0,credit_score-745,800-745)	-0.00338	0.000566	<.0001
mtimesinceD_CEND	L00	Categorical of cx_time <sup>1</sup> (time since default)	prior_default_cnt=0	-0.1088	0.0214	<.0001
mtimesinceD_CEND	L01	Categorical of cx_time <sup>1</sup> (time since default)	cx_time <= 1	-1.1393	0.0257	<.0001
mtimesinceD_CEND	L02	Categorical of cx_time <sup>1</sup> (time since default)	cx_time = 2	-0.9383	0.0264	<.0001
mtimesinceD_CEND	L03	Categorical of cx_time <sup>1</sup> (time since default)	cx_time = 3	-0.6764	0.0265	<.0001
mtimesinceD_CEND	L04	Categorical of cx_time <sup>1</sup> (time since default)	cx_time <= 16	-0.098	0.0218	<.0001
mtimesinceD_CEND	Z00	Categorical of cx_time <sup>1</sup> (time since default)	base level: else			
vtimesinced_cend_pw1		Variate of cx_time <sup>1</sup> (time since default)	median(0,cx_time-16,55-16)	-0.00434	0.00247	0.0793
vhpa2yb_cend_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-0,90-0)	-0.00989	0.000175	<.0001
vhpa2yb_cend_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-90,106-90)	0.0258	0.000473	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 119

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vhpa2yb_cend_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-106,111-106)	-0.0191	0.00131	<.0001
vhpa2yb_cend_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-111,114-111)	0.0318	0.00243	<.0001
vhpa2yb_cend_pw5		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-114,119-114)	0.0156	0.00155	<.0001
vhpa2yb_cend_pw6		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-119,130-119)	-0.0268	0.000751	<.0001
mRatioTmpTei_CEND	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	1.6526	0.0882	<.0001
mRatioTmpTei_CEND	Z01	Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptej_cend_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,12-0)	0.0769	0.00754	<.0001
vratiotmptej_cend_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-12,35-12)	0.0172	0.000593	<.0001
vdeltaUEinit_cend_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-65,78-65)	0.0131	0.000599	<.0001
vdeltaUEinit_cend_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-78,90-78)	-0.00904	0.000665	<.0001
vdeltaUEinit_cend_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-90,97-90)	0.0304	0.000919	<.0001
vdeltaUEinit_cend_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-97,126-97)	0.0184	0.000254	<.0001
vdeltaUEinit_cend_pw5		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-126,150-126)	-0.00206	0.000312	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 120

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vloanraw_cend_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,57000-0)	0.000045	8.32E-07	<.0001
vloanraw_cend_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-57000,159000-57000)	0.000015	6.03E-08	<.0001
vloanraw_cend_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-159000,345000-159000)	2.75E-06	3.35E-08	<.0001
vltv_cend_pw1		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-0,78-0)	-0.00391	0.000091	<.0001
vltv_cend_pw2		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-78,89-78)	0.015	0.000653	<.0001
vltv_cend_pw3		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-89,92-89)	0.039	0.00214	<.0001
vltv_cend_pw4		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-92,97-92)	0.0624	0.00149	<.0001
vltv_cend_pw5		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-97,100-97)	-0.0578	0.00608	<.0001
vsBOI_CEND_pw1		Variate piecewise of (SBOI) small business optimism index	median(0,mSBOI-85,100-85)	-0.00211	0.00071	0.0029
vsBOI_cend_pw2		Variate piecewise of (SBOI) small business optimism index	median(0,mSBOI-100,108-100)	0.00898	0.00109	<.0001

### Current Transition Model Parameters – FRM15 C\_SR

The model parameters for the FRM15 current to streamlined refinance transition are shown below.

Table 37: Current to Streamlined Refinance Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-6.4988	0.0764	0.0000
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (judicial state)	0.0195	0.0085	0.0217
mjudicial	2	Categorical of judicial (judicial state)	base level: else (non-judicial state)			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.4861	0.0189	0.0000
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
mdpa_comb13_CSR	2	Categorical of dpa (down payment assistance)	dpa = "nonprof"	0.7892	0.0384	0.0000



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 121

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mdpa_comb13_CSR	3	Categorical of dpa (down payment assistance)	dpa = "govt" or dpa = "relative"	-0.1565	0.0350	0.0000
mdpa_comb13_CSR	4	Categorical of dpa (down payment assistance)	base level: dpa = "na_other"			
mpriordef_CSR	L01	Categorical of prior default count	prior_default_cnt = 1	-0.0827	0.0191	0.0000
mpriordef_CSR	L02	Categorical of prior default count	prior_default_cnt = 2	-0.2076	0.0357	0.0000
mpriordef_CSR	L03	Categorical of prior default count	prior_default_cnt >= 3	-0.0781	0.0360	0.0302
mpriordef_CSR	Z00	Categorical of prior default count	base level: prior_default_cnt = 0			
mperiodnbr_CSR	L02	Categorical of period_number	period_number = 2	-0.8648	0.0377	0.0000
mperiodnbr_CSR	L03	Categorical of period_number	period_number = 3	0.1483	0.0288	0.0000
mperiodnbr_CSR	L04	Categorical of period_number	period_number = 4	0.6329	0.0260	0.0000
mperiodnbr_CSR	L05	Categorical of period_number	period_number = 5	0.5976	0.0251	0.0000
mperiodnbr_CSR	L06	Categorical of period_number	period_number = 6	0.5908	0.0249	0.0000
mperiodnbr_CSR	L07	Categorical of period_number	period_number = 7	0.5140	0.0247	0.0000
mperiodnbr_CSR	L08	Categorical of period_number	period_number = 8	0.4319	0.0247	0.0000
mperiodnbr_CSR	L09	Categorical of period_number	period_number = 9	0.4017	0.0248	0.0000
mperiodnbr_CSR	L10	Categorical of period_number	period_number = 10	0.3674	0.0252	0.0000
mperiodnbr_CSR	L11	Categorical of period_number	period_number = 11	0.2637	0.0259	0.0000
mperiodnbr_CSR	L12	Categorical of period_number	period_number = 12	0.1460	0.0267	0.0000
mperiodnbr_CSR	L13	Categorical of period_number	period_number = 13	0.0447	0.0277	0.1072
mperiodnbr_CSR	Z14	Categorical of period_number	base level: else			
vperiodnbr_CSR_pw1		Variate piecewise of period_number	median(0,period_number-13,24-13)	-0.0574	0.0026	0.0000
vperiodnbr_CSR_pw2		Variate piecewise of period_number	median(0,period_number-24,43-24)	-0.1040	0.0022	0.0000
mcredit_score_CSR	L00	Categorical of credit_score	credit_score = 0	-0.3294	0.0160	0.0000
mcredit_score_CSR	Z00	Categorical of credit_score	base level: else			
vcredit_CSR_pw2		Variate piecewise of credit_score	median(0,credit_score-650,770-650)	-0.0022	0.0001	0.0000
vcredit_CSR_pw3		Variate piecewise of credit_score	median(0,credit_score-770,800-770)	-0.0072	0.0009	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 122

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vdeltaUEinit_CSR_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-63,91-63)	0.0036	0.0008	0.0000
vdeltaUEinit_CSR_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-91,99-91)	-0.0291	0.0026	0.0000
vdeltaUEinit_CSR_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-99,104-99)	0.0874	0.0042	0.0000
vdeltaUEinit_CSR_pw5		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-104,200-104)	0.0010	0.0003	0.0008
vdeltaUEinit_CSR_pw6		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-200,300-200)	-0.0035	0.0009	0.0001
vratiotmptej_CSR_pw2		Variate piecewise of ratio_tmp_tej (front-end ratio)	median(0,ratio_tmp_tej-11,16-11)	0.0082	0.0030	0.0062
vratiotmptej_CSR_pw3		Variate piecewise of ratio_tmp_tej (front-end ratio)	median(0,ratio_tmp_tej-16,43-16)	0.0104	0.0007	0.0000
vratiotmptej_CSR_pw4		Variate piecewise of ratio_tmp_tej (front-end ratio)	median(0,ratio_tmp_tej-43,50-43)	-0.0641	0.0102	0.0000
vltv_CSR_pw1		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-0,39-0)	-0.0033	0.0008	0.0000
vltv_CSR_pw2		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-39,93-39)	0.0060	0.0004	0.0000
vltv_CSR_pw3		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-93,100-93)	0.0778	0.0106	0.0000
vloanraw_CSR_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,62400-0)	0.0000	0.0000	0.0000
vloanraw_CSR_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-62400,124000-62400)	0.0000	0.0000	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 123

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vloanraw_CSR_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-124000,250000-124000)	0.0000	0.0000	0.0000
vloanraw_CSR_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-250000,425000-250000)	0.0000	0.0000	0.0000
vhpa2yb_CSR_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-88,105-88)	-0.0156	0.0012	0.0000
vhpa2yb_CSR_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-112,117-112)	-0.0113	0.0034	0.0010
vhpa2yb_CSR_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-117,140-117)	-0.0066	0.0016	0.0000
vsato_csr_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-.4)	0.9677	0.0121	0.0000
vsato_csr_pw2		Variate piecewise of sato (spread at origination)	max(sato-.4,0)	0.1904	0.0385	0.0000
vDeltaTY1_CSR_pw1		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-0,73-0)	-0.0143	0.0004	0.0000
vDeltaTY1_CSR_pw2		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-73,150-73)	0.0019	0.0002	0.0000
mdeltaTy10Init_csr	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r >109	-0.9116	0.0138	0.0000
mdeltaTy10Init_csr	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
mseason_grp_CSR	L02	Categorical of season	season = "spring"	0.0524	0.0102	0.0000
mseason_grp_CSR	L03	Categorical of season	season = "summer"	-0.0713	0.0105	0.0000
mseason_grp_CSR	Z0104	Categorical of season	base level: else			
myslope_CSR	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r <=218	-0.2590	0.0184	0.0000
myslope_CSR	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
vCCI_CSR_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0177	0.0011	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 124

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vCCI_CSR_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	-0.0277	0.0009	0.0000
vCCI_CSR_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	0.0395	0.0013	0.0000
vSBOI_CSR_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0122	0.0037	0.0010
vSBOI_CSR_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	0.1618	0.0045	0.0000

### Current Transition Model Parameters – FRM15 C\_D

The model parameters for the FRM15 current to default transition are shown below.

Table 38: Current to Default Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-3.5529	0.0481	0.0000
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	0.0968	0.0485	0.0458
mdpa	2	Categorical of dpa (down payment assistance)	dpa= "nonprof"	0.2722	0.0142	0.0000
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	0.1256	0.0125	0.0000
mdpa	4	Categorical of dpa (down payment assistance)	base level:dpa = "na_other"			
mpriordef_CD	L01	Categorical of prior default count	prior_default_cnt = 1	2.1156	0.0064	0.0000
mpriordef_CD	L02	Categorical of prior default count	prior_default_cnt = 2	2.8158	0.0077	0.0000
mpriordef_CD	L03	Categorical of prior default count	prior_default_cnt >= 3	3.2278	0.0077	0.0000
mpriordef_CD	Z00	Categorical of prior default count	prior_default_cnt = 0			
vpriordef_CD_pw1		Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	0.1679	0.0020	0.0000
mperiodnbr_CD	L02	Categorical of period_number	period_number = 2	-0.5843	0.0174	0.0000
mperiodnbr_CD	L03	Categorical of period_number	period_number = 3	-0.3651	0.0157	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 125

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mperiodnbr_CD	L04	Categorical of period_number	period_number = 4	-0.2642	0.0149	0.0000
mperiodnbr_CD	Z05	Categorical of period_number	base level: else			
vperiodnbr_CD_pw1		Variate piecewise of period_number	median(0,period_number-4,24-4)	-0.0361	0.0006	0.0000
vperiodnbr_CD_pw2		Variate piecewise of period_number	median(0,period_number-24,50-24)	-0.0191	0.0005	0.0000
vperiodnbr_CD_pw3		Variate piecewise of period_number	median(0,period_number-50,57-50)	0.0415	0.0028	0.0000
mcredit_score_CD	L00	Categorical of credit_score	credit_score = 0	-0.3902	0.0127	0.0000
mcredit_score_CD	Z00	Categorical of credit_score	base level: else			
vcredit_CD_pw1		Variate piecewise of credit_score	median(0,credit_score-500,650-500)	-0.0029	0.0001	0.0000
vcredit_CD_pw2		Variate piecewise of credit_score	median(0,credit_score-650,800-650)	-0.0104	0.0001	0.0000
vloanraw_CD_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,62400-0)	0.0000	0.0000	0.0000
vloanraw_CD_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-62400,124000-62400)	0.0000	0.0000	0.0000
vloanraw_CD_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-124000,250000-124000)	0.0000	0.0000	0.0000
vdeltaUEinit_CD_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-0,63-0)	0.0081	0.0005	0.0000
vdeltaUEinit_CD_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-97,200-97)	0.0020	0.0001	0.0000
vdeltaUEinit_CD_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-200,300-200)	0.0011	0.0003	0.0000
vratiotmptei_CD_pw3		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-11,37-11)	0.0128	0.0003	0.0000
vratiotmptei_CD_pw4		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-37,55-37)	-0.0072	0.0017	0.0000
vsato_cd_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-.4)	0.0980	0.0056	0.0000
vsato_cd_pw2		Variate piecewise of sato (spread at origination)	max(sato-.4,0)	0.0755	0.0161	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 126

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mltv_CD	Miss	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r = .	0.4318	0.0223	0.0000
mltv_CD	z00	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_CD_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-0,39-0)	0.0099	0.0006	0.0000
vltv_CD_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-39,90-39)	0.0096	0.0002	0.0000
vltv_CD_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-90,100-90)	0.0508	0.0032	0.0000
vhpa2yb_CD_pw1		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_R-88,105-88)	-0.0113	0.0007	0.0000
vhpa2yb_CD_pw2		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_R-105,112-105)	-0.0234	0.0010	0.0000
vhpa2yb_CD_pw4		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_R-123,140-123)	-0.0309	0.0014	0.0000
mseason_grp_CD	L02	Categorical of season	season = "spring"	-0.2302	0.0056	0.0000
mseason_grp_CD	L03	Categorical of season	season = "summer"	-0.1242	0.0053	0.0000
mseason_grp_CD	Z0104	Categorical of season	base level: else			
vCCI_CD_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	-0.0104	0.0006	0.0000
vCCI_CD_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0181	0.0003	0.0000
vCCI_CD_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	0.0221	0.0007	0.0000
vsBOI_CD_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0193	0.0022	0.0000
vsBOI_CD_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	-0.0914	0.0023	0.0000
vsBOI_CD_pw3		Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	-0.0830	0.0023	0.0000

### Current Transition Model Parameters – FRM15 C\_CXS

The model parameters for the FRM15 current to self-cure transition are shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 127

Table 39: Current to Self-Cure Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-4.4539	0.0863	0.0000
mrfnc_ind	1	Categorical of rfncl_ind (refinanced loan indicator)	refinanced, non-streamlined	-0.0700	0.0130	0.0000
mrfnc_ind	2	Categorical of rfncl_ind (refinanced loan indicator)	streamlined refinanced	-0.3191	0.0208	0.0000
mrfnc_ind	3	Categorical of rfncl_ind (refinanced loan indicator)	base level: else			
mperiodnbr_CCXS	L02	Categorical of period_number	period_number = 2	-0.3699	0.0341	0.0000
mperiodnbr_CCXS	L03	Categorical of period_number	period_number = 3	-0.2833	0.0328	0.0000
mperiodnbr_CCXS	Z04	Categorical of period_number	base level: else			
vperiodnbr_CCXS_pw1		Variate piecewise of period_number	median(0,period_number-3,16-3)	-0.0186	0.0018	0.0000
vperiodnbr_CCXS_pw2		Variate piecewise of period_number	median(0,period_number-16,30-16)	-0.0368	0.0014	0.0000
vperiodnbr_CCXS_pw3		Variate piecewise of period_number	median(0,period_number-30,41-30)	-0.0341	0.0023	0.0000
vperiodnbr_CCXS_pw4		Variate piecewise of period_number	median(0,period_number-41,60-41)	-0.0075	0.0031	0.0152
mcredit_score_CCXS	L00	Categorical of credit_score	credit_score = 0	0.1265	0.0159	0.0000
mcredit_score_CCXS	Z00	Categorical of credit_score	base level: else			
vcredit_CCXS_pw2		Variate piecewise of credit_score	median(0,credit_score-643,800-643)	-0.0084	0.0001	0.0000
vloanraw_CCXS_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,40000-0)	0.0000	0.0000	0.0000
vloanraw_CCXS_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-40000,150000-40000)	0.0000	0.0000	0.0000
vdeltaUEinit_CCXS_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-45,150-45)	0.0012	0.0002	0.0000
vdeltaUEinit_CCXS_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-150,200-150)	0.0016	0.0005	0.0041
vdeltaUEinit_CCXS_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-200,300-200)	0.0014	0.0006	0.0298

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 128

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		rate from policy inception to current)				
mratio_tmp_te_i_CCXS	L00	Categorical of ratio_tmp_te_i (front-end ratio)	ratio_tmp_te_i = 0	0.1304	0.0250	0.0000
mratio_tmp_te_i_CCXS	Z01	Categorical of ratio_tmp_te_i (front-end ratio)	base level: else			
vratiotmpte_i_CCXS_pw2		Variate piecewise of ratio_tmp_te_i (front-end ratio)	median(0,ratio_tmp_te_i-9,16-9)	0.0124	0.0032	0.0001
vratiotmpte_i_CCXS_pw3		Variate piecewise of ratio_tmp_te_i (front-end ratio)	median(0,ratio_tmp_te_i-16,36-16)	0.0061	0.0008	0.0000
mpriordef_CCXS	L01	Categorical of prior default count	prior_default_cnt = 1	1.9162	0.0124	0.0000
mpriordef_CCXS	L02	Categorical of prior default count	prior_default_cnt = 2	2.6039	0.0149	0.0000
mpriordef_CCXS	L10	Categorical of prior default count	prior_default_cnt >= 10	2.9323	0.0478	0.0000
mpriordef_CCXS	PW1	Categorical of prior default count	else	2.7602	0.0177	0.0000
mpriordef_CCXS	Z00	Categorical of prior default count	base level: prior_default_cnt = 0			
vpriordef_CCXS_pw1		Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-2,10-2)	0.2031	0.0047	0.0000
vltv_CCXS_pw1		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-0,40-0)	0.0066	0.0015	0.0000
vltv_CCXS_pw2		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-40,60-40)	0.0029	0.0010	0.0051
vltv_CCXS_pw3		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-60,88-60)	0.0088	0.0008	0.0000
vltv_CCXS_pw4		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-88,100-88)	0.0182	0.0049	0.0002
vhpa2yb_CCXS_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-100,106-100)	-0.0294	0.0027	0.0000
vhpa2yb_CCXS_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-106,115-106)	-0.0065	0.0016	0.0000
mperiod_CCXS	L01	Categorical version of period	period < 200604	-2.0118	0.0364	0.0000
mperiod_CCXS	Z01	Categorical version of period	base level: else			
mseason_grp_CCXS	L02	Categorical of season	season = "spring"	-0.1690	0.0109	0.0000



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 129

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mseason_grp_CCXS	L03	Categorical of season	season = "summer"	0.0073	0.0102	0.4739
mseason_grp_CCXS	Z0104	Categorical of season	base level: else			
vCCI_CCXS_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0307	0.0008	0.0000
vCCI_CCXS_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0130	0.0011	0.0000
vsBOI_CCXS_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0551	0.0025	0.0000
vsBOI_CCXS_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	-0.1208	0.0051	0.0000

### Current Transition Model Parameters – FRM15 C\_PRE

The model parameters for the FRM15 current to prepayment transition are shown below.

Table 40: Current to Prepayment Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-4.8185	0.0472	0.0000
mdpa_comb13_CPRES	2	Categorical of dpa (down payment assistance)	dpa = "nonprof"	-0.1386	0.0317	0.0000
mdpa_comb13_CPRES	3	Categorical of dpa (down payment assistance)	dpa = "govt" or dpa = "relative"	0.1166	0.0126	0.0000
mdpa_comb13_CPRES	4	Categorical of dpa (down payment assistance)	base level: dpa = "na_other"			
mperiodnbr_CPRES	L02	Categorical of period_number	period_number = 2	-2.0207	0.0246	0.0000
mperiodnbr_CPRES	L03	Categorical of period_number	period_number = 3	-1.2493	0.0175	0.0000
mperiodnbr_CPRES	L04	Categorical of period_number	period_number = 4	-0.8830	0.0148	0.0000
mperiodnbr_CPRES	L05	Categorical of period_number	period_number = 5	-0.5963	0.0131	0.0000
mperiodnbr_CPRES	L06	Categorical of period_number	period_number = 6	-0.4185	0.0122	0.0000
mperiodnbr_CPRES	L07	Categorical of period_number	period_number = 7	-0.3200	0.0118	0.0000
mperiodnbr_CPRES	L08	Categorical of period_number	period_number = 8	-0.2184	0.0115	0.0000
mperiodnbr_CPRES	L09	Categorical of period_number	period_number = 9	-0.1350	0.0113	0.0000
mperiodnbr_CPRES	L10	Categorical of period_number	period_number = 10	-0.0939	0.0113	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 130

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mperiodnbr_CPPE	L11	Categorical of period_number	period_number = 11	-0.0732	0.0114	0.0000
mperiodnbr_CPPE	L12	Categorical of period_number	period_number = 12	-0.0556	0.0115	0.0000
mperiodnbr_CPPE	Z13	Categorical of period_number	base level: else			
vperiodnbr_CPPE_pw1		Variate piecewise of period_number	median(0,period_number-12,34-12)	0.0045	0.0004	0.0000
vperiodnbr_CPPE_pw2		Variate piecewise of period_number	median(0,period_number-34,42-34)	0.0058	0.0011	0.0000
vperiodnbr_CPPE_pw3		Variate piecewise of period_number	median(0,period_number-42,56-42)	0.0375	0.0010	0.0000
vperiodnbr_CPPE_pw4		Variate piecewise of period_number	median(0,period_number-56,60-56)	0.3461	0.0041	0.0000
mcredit_score_CPPE	L00	Categorical of credit_score	credit_score = 0	0.5577	0.0244	0.0000
mcredit_score_CPPE	Z00	Categorical of credit_score	base level: else			
vcredit_CPPE_pw1		Variate piecewise of credit_score	median(0,credit_score-500,650-500)	0.0030	0.0002	0.0000
vcredit_CPPE_pw2		Variate piecewise of credit_score	median(0,credit_score-650,800-650)	0.0008	0.0001	0.0000
vloanraw_CPPE_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,62400-0)	0.0000	0.0000	0.0000
vloanraw_CPPE_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-62400,124000-62400)	0.0000	0.0000	0.0000
vloanraw_CPPE_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-124000,250000-124000)	0.0000	0.0000	0.0000
vloanraw_CPPE_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-250000,425000-250000)	0.0000	0.0000	0.0000
vdeltaUEinit_CPPE_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-63,97-63)	0.0045	0.0002	0.0000
vdeltaUEinit_CPPE_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-97,200-97)	0.0023	0.0001	0.0000
mratio_tmp_teI_CPPE	L00	Categorical of ratio_tmp_teI (front-end ratio)	ratio_tmp_teI = 0	-0.3043	0.0327	0.0000
mratio_tmp_teI_CPPE	Z01	Categorical of ratio_tmp_teI (front-end ratio)	base level: else			
vratiotmpteI_CPPE_pw1		Variate piecewise of ratio_tmp_teI (front-end ratio)	median(0,ratio_tmp_teI-0,11-0)	-0.0162	0.0033	0.0000
vratiotmpteI_CPPE_pw2		Variate piecewise of ratio_tmp_teI (front-end ratio)	median(0,ratio_tmp_teI-11,16-11)	-0.0068	0.0019	0.0004

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 131

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vratiotmptei_CPRE_pw3		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-16,36-16)	-0.0063	0.0004	0.0000
vratiotmptei_CPRE_pw4		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-36,50-36)	-0.0056	0.0015	0.0002
mpriordef_CPRE	L01	Categorical of prior default count	prior_default_cnt = 1	-0.0879	0.0075	0.0000
mpriordef_CPRE	L02	Categorical of prior default count	prior_default_cnt = 2	-0.2084	0.0130	0.0000
mpriordef_CPRE	L03	Categorical of prior default count	prior_default_cnt >= 3	-0.2980	0.0110	0.0000
mpriordef_CPRE	Z00	Categorical of prior default count	prior_default_cnt = 0			
vsato_CPre_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-.4)	0.1185	0.0043	0.0000
vsato_CPre_pw2		Variate piecewise of sato (spread at origination)	max(sato-.4,0)	-0.1604	0.0146	0.0000
mltv_CPRE	Miss	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r = .	-0.1702	0.0137	0.0000
mltv_CPRE	z00	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_CPRE_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-0,39-0)	-0.0100	0.0004	0.0000
vltv_CPRE_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-90,100-90)	-0.0749	0.0044	0.0000
mhpa2yb_CPRE	L084	Categorical of hpa2y_bleded_r <sup>6</sup>	0<hpa2y_bleded_R <= 84	0.2586	0.0198	0.0000
mhpa2yb_CPRE	L088	Categorical of hpa2y_bleded_r <sup>6</sup>	hpa2y_bleded_R <= 88	0.0837	0.0215	0.0001
mhpa2yb_CPRE	Z000	Categorical of hpa2y_bleded_r <sup>6</sup>	base level: else			
vhpa2yb_CPRE_pw1		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_R-88,105-88)	0.0454	0.0009	0.0000
vhpa2yb_CPRE_pw2		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_R-105,112-105)	0.0158	0.0011	0.0000
vhpa2yb_CPRE_pw3		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_R-112,117-112)	0.0231	0.0014	0.0000
vhpa2yb_CPRE_pw4		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_R-117,140-117)	0.0129	0.0005	0.0000
mseason_grp_CPRE	L02	Categorical of season	season = "spring"	0.1220	0.0043	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 132

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mseason_grp_CPRE	L03	Categorical of season	season = "summer"	0.1310	0.0043	0.0000
mseason_grp_CPRE	Z0104	Categorical of season	base level: else			
vCCI_CPRE_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0012	0.0006	0.0585
vCCI_CPRE_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	-0.0154	0.0002	0.0000
vCCI_CPRE_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0162	0.0005	0.0000
vSBOI_CPRE_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	0.0192	0.0022	0.0000
vSBOI_CPRE_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	0.1128	0.0016	0.0000
vSBOI_CPRE_pw3		Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	0.0089	0.0014	0.0000

### Current Transition Model Parameters – ARM C\_SR

The model parameters for the ARM current to streamlined refinance transition are shown below.

Table 41: Current to Streamlined Refinance Transition ARM Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-8.5313	0.2627	0.0000
mjudicial	1		Categorical of judicial (judicial state)	judicial = 1 , judicial state	-0.1588	0.0089	0.0000
mjudicial	2		Categorical of judicial (judicial state)	base level: else, non-judicial state			
mdpa_nprof	LNPro		Categorical of dpa (down payment assistance)	dpa= "nonprof"	0.5074	0.0166	0.0000
mdpa_nprof	Z0thr		Categorical of dpa (down payment assistance)	base level: else			
myslope_CSR	L01		Categorical of Yield Curve Slope	1<=y slope<=2	0.1317	0.0120	0.0000
myslope_CSR	Z00		Categorical of Yield Curve Slope	base level: else			
mfrst_tm_by	1		Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.0329	0.0120	0.0062
mfrst_tm_by	2		Categorical of frst_tm_by (first-time buyer)	base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 133

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mrfnc_ind	2		Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind = "Y"	0.1880	0.0151	0.0000
mrfnc_ind	3		Categorical of rfnc_ind (refinanced loan indicator)	base level: else			
mperiodnbr_CSR	L02		Categorical of period_number	period_number = 2	-1.1684	0.0272	0.0000
mperiodnbr_CSR	L03		Categorical of period_number	period_number = 3	-0.1424	0.0193	0.0000
mperiodnbr_CSR	L04		Categorical of period_number	period_number = 4	0.2829	0.0168	0.0000
mperiodnbr_CSR	L05		Categorical of period_number	period_number = 5	0.3762	0.0165	0.0000
mperiodnbr_CSR	L06		Categorical of period_number	period_number = 6	0.1531	0.0179	0.0000
mperiodnbr_CSR	L07		Categorical of period_number	period_number = 7	-0.1423	0.0202	0.0000
mperiodnbr_CSR	Z08		Categorical of period_number	base level: else			
vperiodnbr_CSR_pw1			Variate piecewise of period_number	median(0,period_number-8,40-8)	-0.0637	0.0010	0.0000
vperiodnbr_CSR_pw2			Variate piecewise of period_number	median(0,period_number-40,53-40)	-0.0443	0.0045	0.0000
vperiodnbr_CSR_pw4			Variate piecewise of period_number	median(0,period_number-68,108-68)	-0.0231	0.0050	0.0000
mperiodnbr_CSR*mdpa_nprof	L02	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 2; dpa="nonprof"	-0.3126	0.0722	0.0000
mperiodnbr_CSR*mdpa_nprof	L03	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 3; dpa="nonprof"	-0.5143	0.0497	0.0000
mperiodnbr_CSR*mdpa_nprof	L04	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 4; dpa="nonprof"	-0.7190	0.0461	0.0000
mperiodnbr_CSR*mdpa_nprof	L05	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 5; dpa="nonprof"	-0.4156	0.0417	0.0000
mperiodnbr_CSR*mdpa_nprof	L06	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 6; dpa="nonprof"	-0.2901	0.0460	0.0000
mperiodnbr_CSR*mdpa_nprof	L07	LNPro	Interaction of Categorical of period_number	period_number = 7; dpa="nonprof"	-0.2496	0.0531	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 134

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and Categorical of dpa				
mperiodnbr_CSR*mdpa_nprof	Z08	Zothr	Interaction of Categorical of period_number and Categorical of dpa	base level: else; base level: else			
vcredit_CSR_pw1			Variate piecewise of credit_score	0<credit_score<=450	-0.7246	0.2520	0.0040
vcredit_CSR_pw3			Variate piecewise of credit_score	median(0,credit_score-500,600-500)	-0.0012	0.0001	0.0000
vcredit_CSR_pw6			Variate piecewise of credit_score	median(0,credit_score-680,720-680)	-0.0051	0.0004	0.0000
vcredit_CSR_pw8			Variate piecewise of credit_score	median(0,credit_score-745,800-745)	-0.0059	0.0007	0.0000
vperiodnbr_CSR_pw1*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-8,40-8); prior_default_cnt ne 0	0.0119	0.0018	0.0000
vperiodnbr_CSR_pw2*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-40,53-40); prior_default_cnt ne 0	0.0552	0.0068	0.0000
vperiodnbr_CSR_pw3*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-53,68-53); prior_default_cnt ne 0	-0.0158	0.0067	0.0178
vperiodnbr_CSR_pw*mpriordef_ind	Z00		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	base level: else; base level: else			
vdeltaUEinit_CSR_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-0,90-0)	-0.0095	0.0006	0.0000
vdeltaUEinit_CSR_pw2			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-90,97-90)	0.0054	0.0028	0.0568
vdeltaUEinit_CSR_pw3			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy	median(0,deltaUEinit_r-97,100-97)	0.0593	0.0060	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 135

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			inception to current)				
vdeltaUEinit_CSR_pw5			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-110,140-110)	0.0069	0.0006	0.0000
vdeltaUEinit_CSR_pw7			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-175,200-175)	-0.0046	0.0011	0.0000
vdeltaUEinit_CSR_pw8			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-200,300-200)	0.0041	0.0006	0.0000
mRatioTmpTei_CSR	L00		Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.6859	0.0333	0.0000
mRatioTmpTei_CSR	Z01		Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptej_CSR_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	0.0195	0.0015	0.0000
vratiotmptej_CSR_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	0.0031	0.0013	0.0191
vratiotmptej_CSR_pw3			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-36,50-36)	0.0061	0.0021	0.0032
mpriordef_CSR*mtimesinceD_CSR	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	-0.5962	0.0429	0.0000
mpriordef_CSR*mtimesinceD_CSR	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	-0.5922	0.0511	0.0000
mpriordef_CSR*mtimesinceD_CSR	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	-0.3976	0.0544	0.0000
mpriordef_CSR*mtimesinceD_CSR	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; else	-0.0689	0.0309	0.0257

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 136

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CSR*mtimesinceD_CSR	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	-0.9202	0.0761	0.0000
mpriordef_CSR*mtimesinceD_CSR	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	-0.7753	0.0876	0.0000
mpriordef_CSR*mtimesinceD_CSR	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	-0.4724	0.0900	0.0000
mpriordef_CSR*mtimesinceD_CSR	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; else	-0.0338	0.0445	0.4474
mpriordef_CSR*mtimesinceD_CSR	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	-1.1451	0.0803	0.0000
mpriordef_CSR*mtimesinceD_CSR	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	-1.1939	0.1009	0.0000
mpriordef_CSR*mtimesinceD_CSR	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	-0.6566	0.0950	0.0000
mpriordef_CSR*mtimesinceD_CSR	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; else	-0.0263	0.0504	0.6017
mpriordef_CSR*mtimesinceD_CSR	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vpriordef_CSR_pw1			Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	0.0566	0.0131	0.0000
vsato_csr_pw1			Variate piecewise of sato (spread at origination)	min(0,sato-(-.1))	0.3751	0.0078	0.0000
vsato_csr_pw2			Variate piecewise of sato (spread at origination)	median(sato-(-.1),0,.7-(-.1))	0.7905	0.0511	0.0000
vsato_csr_pw3			Variate piecewise of sato (spread at origination)	max(sato-.7,0)	0.2090	0.1100	0.0573



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 137

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vloanraw_CSR_pw1			Variate piecewise of loansize_raw	median(0,loansize_raw-0,64000-0)	0.0000	0.0000	0.0000
vloanraw_CSR_pw2			Variate piecewise of loansize_raw	median(0,loansize_raw-64000,157000-64000)	0.0000	0.0000	0.0000
vloanraw_CSR_pw3			Variate piecewise of loansize_raw	median(0,loansize_raw-157000,425000-157000)	0.0000	0.0000	0.0000
vlv_CSR_pw1			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-0,70-0)	0.0084	0.0012	0.0000
vlv_CSR_pw2			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-70,80-70)	0.0156	0.0029	0.0000
vlv_CSR_pw3			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-80,94-80)	0.0072	0.0013	0.0000
vlv_CSR_pw4			Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-94,100-94)	0.0173	0.0051	0.0007
vhpa2yb_CSR_pw1			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-0,85-0)	0.0093	0.0019	0.0000
vhpa2yb_CSR_pw2			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-85,95-85)	-0.0116	0.0024	0.0000
vhpa2yb_CSR_pw3			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-95,113-95)	0.0048	0.0011	0.0000
vhpa2yb_CSR_pw5			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-120,136-120)	-0.0135	0.0013	0.0000
vhpa2yb_CSR_pw6			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-136,170-136)	-0.0230	0.0025	0.0000
vUEblend_CSR_pw1			Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_r-0,420-0)	0.0012	0.0002	0.0000
vUEblend_CSR_pw2			Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_r-420,820-420)	-0.0013	0.0000	0.0000
mcalperiod_CSR	L200104		Categorical of Calendar Period	period < 200604	0.1228	0.0247	0.0000
mcalperiod_CSR	L200604		Categorical of Calendar Period	period = 200604	0.4152	0.0356	0.0000
mcalperiod_CSR	L200701		Categorical of Calendar Period	period = 200701	0.6254	0.0353	0.0000
mcalperiod_CSR	L200702		Categorical of Calendar Period	period = 200702	0.9589	0.0331	0.0000
mcalperiod_CSR	L200703		Categorical of Calendar Period	period = 200703	0.8774	0.0353	0.0000
mcalperiod_CSR	Z201800		Categorical of Calendar Period	base level: else			
vdeltaUEpr3_csr_pw1			Variate piecewise of deltauepr3_r <sup>5</sup>	median(deltauepr3_r-(-200),0,(-20)-(-200))	0.0028	0.0003	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 138

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			(change in unemployment from 3 quarters prior)				
vdeltaUEpr3_csr_pw2			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-(-20),0,10-(-20))	0.0081	0.0005	0.0000
vdeltaUEpr3_csr_pw3			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-10,0,200-10)	0.0048	0.0001	0.0000
mseason_grp_CSR	L02		Categorical of season	season = "spring"	-0.0379	0.0098	0.0001
mseason_grp_CSR	L03		Categorical of season	season = "summer"	-0.1347	0.0101	0.0000
mseason_grp_CSR	Z0104		Categorical of season	base level: else			
vCCI_CSR_pw1			Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0097	0.0012	0.0000
vCCI_CSR_pw2			Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	-0.0155	0.0006	0.0000
vCCI_CSR_pw3			Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	0.0310	0.0018	0.0000
vSBOI_CSR_pw1			Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0189	0.0045	0.0000
vSBOI_CSR_pw2			Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	0.0430	0.0052	0.0000
vSBOI_CSR_pw3			Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	-0.1550	0.0035	0.0000

### Current Transition Model Parameters – ARM C\_CXS

The model parameters for the ARM current to self-cure transition are shown below.

Table 42: Current to Self-Cure Transition ARM Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-3.8635	0.1371	0.0000
mrnc_ind	2		Categorical of rnc_ind (refinanced loan indicator)	rnc_ind = "Y"	-0.1085	0.0137	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 139

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mrfnc_ind	3		Categorical of rfnrc_ind (refinanced loan indicator)	base level: else			
mdpa_rel	LRela		Categorical of dpa (down payment assistance)	dpa = "relative"	0.0634	0.0139	0.0000
mdpa_rel	Zothr		Categorical of dpa (down payment assistance)	base level: else			
mcalperiod_CCXS	L200104		Categorical of Calendar Period	period < 200604	-1.2431	0.0279	0.0000
mcalperiod_CCXS	L200604		Categorical of Calendar Period	period = 200604	1.0360	0.0318	0.0000
mcalperiod_CCXS	L200701		Categorical of Calendar Period	period = 200701	1.0535	0.0298	0.0000
mcalperiod_CCXS	L200702		Categorical of Calendar Period	period = 200702	0.3775	0.0356	0.0000
mcalperiod_CCXS	L200703		Categorical of Calendar Period	period = 200703	0.3095	0.0338	0.0000
mcalperiod_CCXS	Z201800		Categorical of Calendar Period	base level: else			
vpriordef_CCXS_pw1			Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	0.1159	0.0025	0.0000
mperiodnbr_CCXS	L02		Categorical of period_number	period_number = 2	-0.2307	0.0438	0.0000
mperiodnbr_CCXS	L03		Categorical of period_number	period_number = 3	0.0599	0.0382	0.1172
mperiodnbr_CCXS	L04		Categorical of period_number	period_number = 4	0.1643	0.0361	0.0000
mperiodnbr_CCXS	L05		Categorical of period_number	period_number = 5	0.1010	0.0364	0.0056
mperiodnbr_CCXS	L06		Categorical of period_number	period_number = 6	0.2024	0.0341	0.0000
mperiodnbr_CCXS	L07		Categorical of period_number	period_number = 7	0.1121	0.0343	0.0011
mperiodnbr_CCXS	Z08		Categorical of period_number	base level: else			
vperiodnbr_CCXS_pw1			Variate piecewise of period_number	median(0,period_number-8,36-8)	-0.0139	0.0008	0.0000
vperiodnbr_CCXS_pw2			Variate piecewise of period_number	median(0,period_number-36,53-36)	-0.0108	0.0012	0.0000
vperiodnbr_CCXS_pw3			Variate piecewise of period_number	median(0,period_number-53,76-53)	-0.0110	0.0011	0.0000
vperiodnbr_CCXS_pw4			Variate piecewise of period_number	median(0,period_number-76,108-76)	-0.0085	0.0016	0.0000
vcredit_CCXS_pw5			Variate piecewise of credit_score	median(0,credit_score-630,680-630)	-0.0034	0.0005	0.0000
vcredit_CCXS_pw6			Variate piecewise of credit_score	median(0,credit_score-680,720-680)	-0.0091	0.0011	0.0000
vcredit_CCXS_pw7			Variate piecewise of credit_score	median(0,credit_score-720,745-720)	-0.0062	0.0024	0.0102
vcredit_CCXS_pw8			Variate piecewise of credit_score	median(0,credit_score-745,800-745)	-0.0076	0.0017	0.0000
vdeltaUEinit_CCXS_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup>	median(0,deltaUEinit_r-0,62-0)	-0.0040	0.0013	0.0027

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 140

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			(change in unemployment rate from policy inception to current)				
vdeltaUEinit_CCXS_pw2			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-62,80-62)	0.0029	0.0010	0.0034
vdeltaUEinit_CCXS_pw6			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-126,200-126)	-0.0015	0.0003	0.0000
vdeltaUEinit_CCXS_pw7			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-200,300-200)	0.0006	0.0004	0.0858
mRatioTmpTei_CCXS	L00		Categorical of ratio_tmp_te1 (front-end ratio)	ratio_tmp_te1=0	0.2880	0.0441	0.0000
mRatioTmpTei_CCXS	Z01		Categorical of ratio_tmp_te1 (front-end ratio)	base level: else			
vratiotmpte1_CCXS_pw1			Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-0,19-0)	0.0162	0.0023	0.0000
vratiotmpte1_CCXS_pw4			Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-33,50-33)	0.0054	0.0016	0.0007
mpriordef_CCXS*mtimesinceD_CCXS	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	2.4771	0.0205	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	2.2226	0.0259	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	1.9216	0.0328	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	1.8957	0.0365	0.0000

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 141

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CCXS*mtimesinceD_CCXS	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	1.4662	0.0484	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	1.3759	0.0533	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 7	1.2653	0.0594	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 8	1.1741	0.0659	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 9	1.0841	0.0733	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L01	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; else	1.0626	0.0358	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	2.9266	0.0222	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	2.5963	0.0294	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	2.2955	0.0382	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	2.1649	0.0452	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	1.8578	0.0573	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L06	Interaction of categorical of prior_default_cnt	prior_default_cnt = 2; cx_time = 6	1.6258	0.0683	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 142

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
mpriordef_CCXS*mtimesinceD_CCXS	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 7	1.6710	0.0717	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 8	1.4967	0.0831	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 9	1.5256	0.0867	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L02	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; else	1.2762	0.0428	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	3.2530	0.0166	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	2.8586	0.0196	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	2.4989	0.0242	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	2.2953	0.0288	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	1.9378	0.0366	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	1.7329	0.0431	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 7	1.6324	0.0489	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 143

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CCXS*mtimesinceD_CCXS	L03	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 8	1.6005	0.0535	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 9	1.4285	0.0621	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	L03	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; else	1.1705	0.0361	0.0000
mpriordef_CCXS*mtimesinceD_CCXS	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vtimesincd_CCXS_pw1			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-10,24-10)	-0.0375	0.0039	0.0000
vtimesincd_CCXS_pw2			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-24,40-24)	-0.0263	0.0054	0.0000
vloanraw_CCXS_pw1			Variate piecewise of loansize_raw	median(0,loansize_raw-0,64000-0)	0.0000	0.0000	0.0000
vloanraw_CCXS_pw2			Variate piecewise of loansize_raw	median(0,loansize_raw-64000,157000-64000)	0.0000	0.0000	0.0000
vhpa2yb_CCXS_pw1			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-0,100-0)	-0.0037	0.0010	0.0002
vhpa2yb_CCXS_pw2			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-100,104-100)	-0.0432	0.0043	0.0000
vhpa2yb_CCXS_pw4			Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-113,115-113)	-0.0239	0.0059	0.0000
mseason_grp_CCXS	L02		Categorical of season	season = "spring"	-0.2965	0.0118	0.0000
mseason_grp_CCXS	L03		Categorical of season	season = "summer"	-0.0968	0.0111	0.0000
mseason_grp_CCXS	Z0104		Categorical of season	base level: else			
vCCI_CCXS_pw1			Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0089	0.0012	0.0000
vCCI_CCXS_pw2			Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0185	0.0008	0.0000
vCCI_CCXS_pw3			Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0069	0.0017	0.0000
vsBOI_CCXS_pw1			Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0617	0.0044	0.0000
vsBOI_CCXS_pw2			Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	-0.1054	0.0060	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 144

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vSBOI_CCXS_pw3			Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	0.0168	0.0050	0.0008

### Current Transition Model Parameters – ARM C\_D

The model parameters for the ARM current to default transition are shown below.

Table 43: Current to Default Transition ARM Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-3.4058	0.0695	0.0000
mjudicial	1		Categorical of judicial (judicial state)	judicial = 1 , judicial state	0.0410	0.0043	0.0000
mjudicial	2		Categorical of judicial (judicial state)	base level: else, non-judicial state			
mdpa_govt	LGovt		Categorical of dpa (down payment assistance)	dpa = "govt"	0.1224	0.0229	0.0000
mdpa_govt	Zothr		Categorical of dpa (down payment assistance)	base level: else			
mdpa_nprof	LNPro		Categorical of dpa (down payment assistance)	dpa= "nonprof"	0.2266	0.0108	0.0000
mdpa_nprof	Zothr		Categorical of dpa (down payment assistance)	base level: else			
mdpa_rel	LRela		Categorical of dpa (down payment assistance)	dpa = "relative"	0.0643	0.0068	0.0000
mdpa_rel	Zothr		Categorical of dpa (down payment assistance)	base level: else			
myslope_cd	L01		Categorical of Yield Curve Slope	1<=ycslope<=2	0.2748	0.0065	0.0000
myslope_cd	Z00		Categorical of Yield Curve Slope	base level: else			
mfrst_tm_by	1		Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.0394	0.0059	0.0000
mfrst_tm_by	2		Categorical of frst_tm_by (first-time buyer)	base level: else			
mrfnc_ind	2		Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind = "Y"	0.0539	0.0085	0.0000
mrfnc_ind	3		Categorical of rfnc_ind	base level: else			



**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 145

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			(refinanced loan indicator)				
mcalperiod_cd	L200104		Categorical of Calendar Period	period < 200604	-0.3404	0.0096	0.0000
mcalperiod_cd	L200604		Categorical of Calendar Period	period = 200604	1.5724	0.0141	0.0000
mcalperiod_cd	L200701		Categorical of Calendar Period	period = 200701	1.0794	0.0166	0.0000
mcalperiod_cd	L200702		Categorical of Calendar Period	period = 200702	0.9084	0.0173	0.0000
mcalperiod_cd	L200703		Categorical of Calendar Period	period = 200703	0.4739	0.0168	0.0000
mcalperiod_cd	Z201800		Categorical of Calendar Period	base level: else			
mperiodnbr_CD	L02		Categorical of period_number	period_number = 2	-0.6841	0.0186	0.0000
mperiodnbr_CD	L03		Categorical of period_number	period_number = 3	-0.2481	0.0155	0.0000
mperiodnbr_CD	L04		Categorical of period_number	period_number = 4	-0.0948	0.0146	0.0000
mperiodnbr_CD	L05		Categorical of period_number	period_number = 5	-0.0262	0.0141	0.0642
mperiodnbr_CD	L06		Categorical of period_number	period_number = 6	0.0236	0.0138	0.0869
mperiodnbr_CD	L07		Categorical of period_number	period_number = 7	-0.0083	0.0138	0.5474
mperiodnbr_CD	Z08		Categorical of period_number	base level: else			
vperiodnbr_cd_pw1			Variate piecewise of period_number	median(0,period_number-8,40-8)	-0.0196	0.0005	0.0000
vperiodnbr_cd_pw2			Variate piecewise of period_number	median(0,period_number-40,53-40)	-0.0231	0.0020	0.0000
vperiodnbr_cd_pw3			Variate piecewise of period_number	median(0,period_number-53,68-53)	-0.0181	0.0023	0.0000
vperiodnbr_cd_pw1*mdpa_nprof	LNPro		Interaction of variate piecewise of period_number and categorical of dpa	median(0,period_number-8,40-8); dpa= "nonprof"	-0.0089	0.0007	0.0000
vperiodnbr_cd_pw2*mdpa_nprof	LNPro		Interaction of variate piecewise of period_number and categorical of dpa	median(0,period_number-40,53-40); dpa= "nonprof"	0.0103	0.0022	0.0000
vperiodnbr_cd_pw*mdpa_nprof	Z0thr		Interaction of variate piecewise of period_number and categorical of dpa	mdpa_nprof base level: else;			
vcredit_cd_pw1			Variate piecewise of credit_score	0<credit_score<=450	-0.6980	0.1537	0.0000
vcredit_cd_pw3			Variate piecewise of credit_score	median(0,credit_score-500,600-500)	-0.0056	0.0004	0.0000
vcredit_cd_pw4			Variate piecewise of credit_score	median(0,credit_score-600,630-600)	-0.0056	0.0008	0.0000
vcredit_cd_pw5			Variate piecewise of credit_score	median(0,credit_score-630,680-630)	-0.0112	0.0005	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 146

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vcredit_cd_pw6			Variate piecewise of credit_score	median(0,credit_score-680,720-680)	-0.0122	0.0008	0.0000
vcredit_cd_pw7			Variate piecewise of credit_score	median(0,credit_score-720,745-720)	-0.0100	0.0017	0.0000
vcredit_cd_pw8			Variate piecewise of credit_score	median(0,credit_score-745,800-745)	-0.0110	0.0012	0.0000
icredit_grp0_CD	L000		Categorical of credit_score	credit_score=0	-0.9540	0.0332	0.0000
icredit_grp0_CD	Z999		Categorical of credit_score	base level: else			
vdeltaUEinit_cd_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-0,90-0)	0.0027	0.0002	0.0000
vdeltaUEinit_cd_pw4			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-100,110-100)	0.0029	0.0009	0.0010
vdeltaUEinit_cd_pw5			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-110,140-110)	0.0015	0.0003	0.0000
vdeltaUEinit_cd_pw7			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-175,200-175)	-0.0011	0.0004	0.0122
vdeltaUEinit_cd_pw8			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-200,300-200)	0.0009	0.0002	0.0000
mRatioTmpTei_CD	L00		Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.3711	0.0162	0.0000
mRatioTmpTei_CD	Z01		Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_cd_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	0.0161	0.0007	0.0000
vratiotmptei_cd_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	0.0063	0.0007	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 147

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vratiotmptei_cd_pw3			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-36,50-36)	0.0067	0.0012	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	1.5128	0.0415	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	1.3237	0.0421	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	1.1028	0.0428	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	0.7546	0.0441	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	0.5836	0.0453	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 6	0.4249	0.0466	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 7	0.3612	0.0477	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 8	0.2248	0.0495	0.0000
mpriordef_CD*mtimesinceD_CD	L01	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 9	0.1425	0.0513	0.0054
mpriordef_CD*mtimesinceD_CD	L01	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 10	0.0707	0.0529	0.1819
mpriordef_CD*mtimesinceD_CD	L01	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 11	0.0252	0.0545	0.6440

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 148

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CD*mtimesinceD_CD	L01	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time >= 12	-0.0882	0.0454	0.0520
mpriordef_CD*mtimesinceD_CD	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	1.9303	0.0420	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	1.6715	0.0429	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	1.4526	0.0440	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	1.1007	0.0460	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	0.9095	0.0480	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 6	0.7330	0.0503	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 7	0.6351	0.0526	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 8	0.5133	0.0555	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 9	0.3550	0.0592	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 10	0.4186	0.0602	0.0000
mpriordef_CD*mtimesinceD_CD	L02	L11	Interaction of categorical of prior_default_cnt	prior_default_cnt = 2; cx_time = 11	0.2638	0.0647	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 149

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
mpriordef_CD*mtimesinceD_CD	L02	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time >= 12	0.0429	0.0478	0.3690
mpriordef_CD*mtimesinceD_CD	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	2.2738	0.0417	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	1.9486	0.0421	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	1.7024	0.0425	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	1.3444	0.0434	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	1.1179	0.0445	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 6	0.9179	0.0457	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L07	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 7	0.7687	0.0472	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L08	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 8	0.5990	0.0492	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L09	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 9	0.4086	0.0518	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L10	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 10	0.3558	0.0536	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 150

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CD*mtimesinceD_CD	L03	L11	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 11	0.3436	0.0553	0.0000
mpriordef_CD*mtimesinceD_CD	L03	L12	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time >= 12	0.0431	0.0462	0.3512
mpriordef_CD*mtimesinceD_CD	Z00	Z00	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	base level prior_default_cnt = 0; base level prior_default_cnt = 0			
vpriordef_cd_pw1			Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	0.0890	0.0015	0.0000
vtimesinced_cd_pw1			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-12,24-12)	-0.0402	0.0025	0.0000
vtimesinced_cd_pw2			Variate piecewise of cx_time <sup>1</sup>	median(0,cx_time-24,40-24)	-0.0232	0.0028	0.0000
vsato_cd_pw1			Variate piecewise of sato (spread at origination)	min(0,sato-(-.1))	0.0519	0.0036	0.0000
vsato_cd_pw2			Variate piecewise of sato (spread at origination)	median(sato-(-.1),0,.7-(-.1))	0.0981	0.0300	0.0011
vperiodnbr_cd_pw1*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-8,40-8); prior_default_cnt ne 0	0.0073	0.0006	0.0000
vperiodnbr_cd_pw2*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-40,53-40); prior_default_cnt ne 0	0.0218	0.0021	0.0000
vperiodnbr_cd_pw3*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-53,68-53); prior_default_cnt ne 0	0.0126	0.0025	0.0000
vperiodnbr_cd_pw4*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-68,108-68); prior_default_cnt ne 0	0.0026	0.0009	0.0056
vperiodnbr_cd_pw*mpriordef_ind	Z00		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	base level: else; base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 151

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mltv_cd	L01		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r = .	-0.0710	0.0291	0.0146
mltv_cd	Z00		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_cd_pw1			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,70-0)	0.0057	0.0007	0.0000
vltv_cd_pw2			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-70,80-70)	0.0094	0.0011	0.0000
vltv_cd_pw3			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-80,94-80)	0.0056	0.0008	0.0000
vhpa2yb_cd_pw2			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-85,95-85)	-0.0105	0.0010	0.0000
vhpa2yb_cd_pw3			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-95,113-95)	-0.0105	0.0006	0.0000
vhpa2yb_cd_pw4			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-113,120-113)	-0.0040	0.0013	0.0021
vhpa2yb_cd_pw5			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-120,149-120)	-0.0097	0.0007	0.0000
vhpa2yb_cd_pw6			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-149,170-149)	-0.0172	0.0036	0.0000
vUEblend_cd_pw2			Variate piecewise of ue_bleded_r <sup>8</sup> (change in unemployment rate)	median(0,ue_bleded_r-420,820-420)	0.0001	0.0000	0.0000
vUEblend_cd_pw3			Variate piecewise of ue_bleded_r <sup>8</sup> (change in unemployment rate)	median(0,ue_bleded_r-820,1500-820)	0.0001	0.0000	0.0000
vdeltaUEpr3_cd_pw1			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-(-200),0,(-20)-(-200))	-0.0003	0.0001	0.0152
vdeltaUEpr3_cd_pw2			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-(-20),0,10-(-20))	0.0015	0.0002	0.0000
vdeltaUEpr3_cd_pw3			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-10,0,200-10)	0.0011	0.0001	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 152

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_ind*icredit_grp0_CD	L01	L000	Interaction of categorical of prior default indicator and categorical of credit_score	prior_default_cnt ne 0; credit_score=0	0.8931	0.0410	0.0000
mpriordef_ind*icredit_grp1_CD	L01	L450	Interaction of categorical of prior default indicator and categorical of credit_score	prior_default_cnt ne 0; credit_score<450	0.6916	0.1917	0.0003
mpriordef_ind*icredit_grp_CD	Z00	Z999	Interaction of categorical of prior default indicator and categorical of credit_score	base level: else; base level: else			
vcredit_cd_pw3*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-500,600-500); prior_default_cnt ne 0	0.0046	0.0005	0.0000
vcredit_cd_pw4*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-600,630-600); prior_default_cnt ne 0	0.0044	0.0010	0.0000
vcredit_cd_pw5*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-630,680-630); prior_default_cnt ne 0	0.0079	0.0006	0.0000
vcredit_cd_pw6*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-680,720-680); prior_default_cnt ne 0	0.0075	0.0011	0.0000
vcredit_cd_pw7*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-720,745-720); prior_default_cnt ne 0	0.0085	0.0024	0.0004
vcredit_cd_pw8*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-745,800-745); prior_default_cnt ne 0	0.0059	0.0018	0.0013
vcredit_cd_pw*mpriordef_ind	Z00		Interaction of variate piecewise of credit_score and categorical of	mpriordef_ind base level: else			



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 153

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			prior default indicator				
mseason_grp_CD	L02		Categorical of season	season = "spring"	-0.2680	0.0054	0.0000
mseason_grp_CD	L03		Categorical of season	season = "summer"	-0.0530	0.0051	0.0000
mseason_grp_CD	Z0104		Categorical of season	base level: else			
vCCI_CD_pw1			Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	-0.0016	0.0006	0.0039
vCCI_CD_pw2			Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	-0.0026	0.0003	0.0000
vCCI_CD_pw3			Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0032	0.0008	0.0000
vSBOI_CD_pw1			Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0039	0.0022	0.0800
vSBOI_CD_pw3			Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	-0.0258	0.0019	0.0000

### Current Transition Model Parameters – ARM C\_PRE

The model parameters for the ARM current to prepayment transition are shown below.

Table 44: Current to Prepayment Transition ARM Model Parameters

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept					-3.3836	0.1826	0.0000
mjudicial	1		Categorical of judicial (judicial state)	judicial = 1 , judicial state	-0.0666	0.0042	0.0000
mjudicial	2		Categorical of judicial (judicial state)	base level: else, non-judicial state			
mdpa_govt	LGovt		Categorical of dpa (down payment assistance)	dpa = "govt"	-0.3619	0.0336	0.0000
mdpa_govt	Zothr		Categorical of dpa (down payment assistance)	base level: else			
mdpa_nprof	LNPro		Categorical of dpa (down payment assistance)	dpa= "nonprof"	-0.2304	0.0107	0.0000
mdpa_nprof	Zothr		Categorical of dpa (down payment assistance)	base level: else			
myslope_CPFE	L01		Categorical of Yield Curve Slope	1<=ycslope<=2	0.1728	0.0054	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 154

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
myslope_CPPE	Z00		Categorical of Yield Curve Slope	base level: else			
mfrst_tm_by	1		Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.0596	0.0051	0.0000
mfrst_tm_by	2		Categorical of frst_tm_by (first-time buyer)	base level: else			
mrfnc_ind	2		Categorical of rfnrc_ind (refinanced loan indicator)	rfnc_ind = "Y"	-0.1337	0.0075	0.0000
mrfnc_ind	3		Categorical of rfnrc_ind (refinanced loan indicator)	base level: else			
mcalperiod_CPPE	L200104		Categorical of Calendar Period	period < 200604	0.6690	0.0121	0.0000
mcalperiod_CPPE	L200604		Categorical of Calendar Period	period = 200604	1.0317	0.0167	0.0000
mcalperiod_CPPE	L200701		Categorical of Calendar Period	period = 200701	1.0145	0.0176	0.0000
mcalperiod_CPPE	L200702		Categorical of Calendar Period	period = 200702	1.1490	0.0165	0.0000
mcalperiod_CPPE	L200703		Categorical of Calendar Period	period = 200703	0.8673	0.0184	0.0000
mcalperiod_CPPE	Z201800		Categorical of Calendar Period	base level: else			
mperiodnbr_CPPE	L02		Categorical of period_number	period_number = 2	-1.8055	0.0223	0.0000
mperiodnbr_CPPE	L03		Categorical of period_number	period_number = 3	-1.0299	0.0157	0.0000
mperiodnbr_CPPE	L04		Categorical of period_number	period_number = 4	-0.6242	0.0133	0.0000
mperiodnbr_CPPE	L05		Categorical of period_number	period_number = 5	-0.2815	0.0117	0.0000
mperiodnbr_CPPE	L06		Categorical of period_number	period_number = 6	-0.2095	0.0114	0.0000
mperiodnbr_CPPE	L07		Categorical of period_number	period_number = 7	-0.2022	0.0115	0.0000
mperiodnbr_CPPE	Z08		Categorical of period_number	base level: else			
vperiodnbr_CPPE_pw1			Variate piecewise of period_number	median(0,period_number-8,40-8)	-0.0081	0.0003	0.0000
vperiodnbr_CPPE_pw2			Variate piecewise of period_number	median(0,period_number-40,53-40)	-0.0337	0.0012	0.0000
vperiodnbr_CPPE_pw3			Variate piecewise of period_number	median(0,period_number-53,68-53)	0.0179	0.0018	0.0000
vperiodnbr_CPPE_pw4			Variate piecewise of period_number	median(0,period_number-68,108-68)	-0.0152	0.0014	0.0000
mperiodnbr_CPPE*mdpa_nprof	L02	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 2; dpa="nonprof"	-0.7542	0.1066	0.0000
mperiodnbr_CPPE*mdpa_nprof	L03	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 3; dpa="nonprof"	-0.8450	0.0738	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 155

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			period_number and Categorical of dpa				
mperiodnbr_CPRES*mdpa_nprof	L04	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 4; dpa="nonprof"	-0.5842	0.0542	0.0000
mperiodnbr_CPRES*mdpa_nprof	L05	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 5; dpa="nonprof"	-0.2858	0.0408	0.0000
mperiodnbr_CPRES*mdpa_nprof	L06	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 6; dpa="nonprof"	-0.1398	0.0378	0.0002
mperiodnbr_CPRES*mdpa_nprof	L07	LNPro	Interaction of Categorical of period_number and Categorical of dpa	period_number = 7; dpa="nonprof"	-0.1651	0.0389	0.0000
mperiodnbr_CPRES*mdpa_nprof	Z08	Zothr	Interaction of Categorical of period_number and Categorical of dpa	base level: else; base level: else			
vperiodnbr_CPRES_pw1*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-8,40-8); prior_default_cnt ne 0	0.0086	0.0008	0.0000
vperiodnbr_CPRES_pw2*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-40,53-40); prior_default_cnt ne 0	0.0281	0.0020	0.0000
vperiodnbr_CPRES_pw3*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-53,68-53); prior_default_cnt ne 0	-0.0366	0.0028	0.0000
vperiodnbr_CPRES_pw4*mpriordef_ind	L01		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	median(0,period_number-68,108-68); prior_default_cnt ne 0	0.0072	0.0017	0.0000
vperiodnbr_CPRES_pw*mpriordef_ind	Z00		Interaction of variate of piecewise of period_number and categorical of prior_default_cnt	base level: else; base level: else			

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 156

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vcredit_CPRE_pw1			Variate piecewise of credit_score	0<credit_score<=450	-0.6147	0.1695	0.0003
vcredit_CPRE_pw2			Variate piecewise of credit_score	median(0,credit_score-450,500-450)	-0.0091	0.0009	0.0000
vcredit_CPRE_pw3			Variate piecewise of credit_score	median(0,credit_score-500,600-500)	0.0021	0.0005	0.0000
vcredit_CPRE_pw5			Variate piecewise of credit_score	median(0,credit_score-630,680-630)	0.0047	0.0003	0.0000
vcredit_CPRE_pw6			Variate piecewise of credit_score	median(0,credit_score-680,720-680)	0.0041	0.0003	0.0000
vcredit_CPRE_pw8			Variate piecewise of credit_score	median(0,credit_score-745,800-745)	0.0026	0.0003	0.0000
vcredit_CPRE_pw2*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-450,500-450); prior_default_cnt ne 0	-0.0066	0.0007	0.0000
vcredit_CPRE_pw4*mpriordef_ind	L01		Interaction of variate piecewise of credit_score and categorical of prior default indicator	median(0,credit_score-600,630-600); prior_default_cnt ne 0	0.0054	0.0012	0.0000
vcredit_CPRE_pw*mpriordef_ind	Z00		Interaction of variate piecewise of credit_score and categorical of prior default indicator	mpriordef_ind base level: else			
vdeltaUEinit_CPRE_pw1			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-0,90-0)	-0.0007	0.0002	0.0011
vdeltaUEinit_CPRE_pw3			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-97,100-97)	-0.0236	0.0021	0.0000
vdeltaUEinit_CPRE_pw5			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-110,140-110)	0.0015	0.0003	0.0000
vdeltaUEinit_CPRE_pw7			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-175,200-175)	0.0019	0.0006	0.0015

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 157

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vdeltaUEinit_CPRES_pw8			Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-200,300-200)	-0.0009	0.0004	0.0147
mRatioTmpTei_CPRES	L00		Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	-0.1652	0.0137	0.0000
mRatioTmpTei_CPRES	Z01		Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_CPRES_pw1			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	-0.0068	0.0006	0.0000
vratiotmptei_CPRES_pw2			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	-0.0112	0.0007	0.0000
vratiotmptei_CPRES_pw3			Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-36,50-36)	-0.0056	0.0012	0.0000
mpriordef_CPRES*mtimesinceD_CPRES	L01	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time <= 1	-0.4024	0.0238	0.0000
mpriordef_CPRES*mtimesinceD_CPRES	L01	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 2	-0.5099	0.0275	0.0000
mpriordef_CPRES*mtimesinceD_CPRES	L01	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 3	-0.4833	0.0299	0.0000
mpriordef_CPRES*mtimesinceD_CPRES	L01	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 4	-0.3963	0.0308	0.0000
mpriordef_CPRES*mtimesinceD_CPRES	L01	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time = 5	-0.3089	0.0314	0.0000
mpriordef_CPRES*mtimesinceD_CPRES	L01	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 1; cx_time >= 6	-0.2876	0.0191	0.0000
mpriordef_CPRES*mtimesinceD_CPRES	L02	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time <= 1	-0.4520	0.0321	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 158

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_CPRE*mtimesinceD_CPRE	L02	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 2	-0.5889	0.0386	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L02	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 3	-0.5064	0.0416	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L02	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 4	-0.3552	0.0424	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L02	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time = 5	-0.3695	0.0459	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L02	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt = 2; cx_time >= 6	-0.3738	0.0235	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L03	L01	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time <= 1	-0.6444	0.0314	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L03	L02	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 2	-0.6970	0.0361	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L03	L03	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 3	-0.7164	0.0407	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L03	L04	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 4	-0.5193	0.0413	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L03	L05	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time = 5	-0.4832	0.0438	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	L03	L06	Interaction of categorical of prior_default_cnt and categorical of cx_time <sup>1</sup>	prior_default_cnt >= 3; cx_time >= 6	-0.4574	0.0251	0.0000
mpriordef_CPRE*mtimesinceD_CPRE	Z00	Z00	Interaction of categorical of prior_default_cnt	base level prior_default_cnt = 0; base level prior_default_cnt = 0			

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 159

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
			and categorical of cx_time <sup>1</sup>				
vpriordef_CPRE_pw1			Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	-0.0223	0.0047	0.0000
vsato_CPre_pw1			Variate piecewise of sato (spread at origination)	min(0,sato-(-.1))	0.0530	0.0034	0.0000
vsato_CPre_pw2			Variate piecewise of sato (spread at origination)	median(sato-(-.1),0,.7-(-.1))	0.1225	0.0299	0.0000
vloanraw_CPRE_pw1			Variate piecewise of loansize_raw	median(0,loansize_raw-0,64000-0)	0.0000	0.0000	0.0000
vloanraw_CPRE_pw2			Variate piecewise of loansize_raw	median(0,loansize_raw-64000,157000-64000)	0.0000	0.0000	0.0000
vloanraw_CPRE_pw3			Variate piecewise of loansize_raw	median(0,loansize_raw-157000,425000-157000)	0.0000	0.0000	0.0000
mltv_CPRE	L01		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r = .	0.2403	0.0313	0.0000
mltv_CPRE	Z00		Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_CPRE_pw1			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,70-0)	-0.0098	0.0008	0.0000
vltv_CPRE_pw2			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-70,80-70)	0.0175	0.0011	0.0000
vltv_CPRE_pw3			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-80,94-80)	-0.0208	0.0007	0.0000
vltv_CPRE_pw4			Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-94,100-94)	-0.1433	0.0042	0.0000
vhpa2yb_CPRE_pw1			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-0,85-0)	-0.0122	0.0020	0.0000
vhpa2yb_CPRE_pw2			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-85,95-85)	0.0147	0.0025	0.0000
vhpa2yb_CPRE_pw3			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-95,113-95)	0.0370	0.0007	0.0000
vhpa2yb_CPRE_pw4			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-113,120-113)	0.0178	0.0010	0.0000
vhpa2yb_CPRE_pw5			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-120,149-120)	0.0220	0.0004	0.0000
vhpa2yb_CPRE_pw6			Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-149,170-149)	0.0137	0.0012	0.0000
vUEblend_CPRE_pw1			Variate piecewise of ue_bleded_r <sup>8</sup> (change in unemployment rate)	median(0,ue_bleded_r-0,420-0)	-0.0013	0.0001	0.0000

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 160

Variable	ClassVal0	ClassVal1	Description	Description Detail	Estimate	StdErr	ProbChiSq
vUEblend_CPRES_pw2			Variate piecewise of ue_blen ded_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blen ded_r-420,820-420)	-0.0006	0.0000	0.0000
vUEblend_CPRES_pw3			Variate piecewise of ue_blen ded_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blen ded_r-820,1500-820)	-0.0009	0.0001	0.0000
vdeltaUEpr3_cpres_pw1			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r(-200),0,(-20)-(-200))	0.0020	0.0001	0.0000
vdeltaUEpr3_cpres_pw2			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r(-20),0,10-(-20))	0.0045	0.0002	0.0000
vdeltaUEpr3_cpres_pw3			Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-10,0,200-10)	0.0018	0.0001	0.0000
mseason_grp_CPRES	L02		Categorical of season	season = "spring"	0.1505	0.0048	0.0000
mseason_grp_CPRES	L03		Categorical of season	season = "summer"	0.1896	0.0048	0.0000
mseason_grp_CPRES	Z0104		Categorical of season	base level: else			
vCCI_CPRES_pw1			Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0078	0.0009	0.0000
vCCI_CPRES_pw2			Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	-0.0096	0.0003	0.0000
vCCI_CPRES_pw3			Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0023	0.0008	0.0032
vSBOI_CPRES_pw1			Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	0.0375	0.0032	0.0000
vSBOI_CPRES_pw2			Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	0.0145	0.0023	0.0000

Default Transition Model Parameters – FRM30NSR D\_CLM

The model parameters for the FRM30NSR default to claim transition are shown below.



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 161

Table 45: Default to Claim Transition FRM30NSR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-5.3679	0.0401	<.0001
mrnc_ind	2	Categorical of rnc_ind (refinanced loan indicator)	rnc_ind = "N"	0.2141	0.00443	<.0001
mrnc_ind	3	Categorical of rnc_ind (refinanced loan indicator)	base level: else			
mDeltaTm3_DCLM	L01	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	DeltaTm3Init_r <sup>12</sup> > 600	-0.3706	0.00594	<.0001
mDeltaTm3_DCLM	Z00	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	base level: else			
mseason	1	Categorical of season	season = "winter"	0.0182	0.00311	<.0001
mseason	2	Categorical of season	season = "spring"	0.0712	0.0031	<.0001
mseason	3	Categorical of season	season = "summer"	0.0758	0.00307	<.0001
mseason	4	Categorical of season	base level: season = "fall"			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.2017	0.00227	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	0.128	0.00707	<.0001
mdpa	2	Categorical of dpa (down payment assistance)	base level: else	0.4185	0.00345	<.0001
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "Relative"	-0.0176	0.00351	<.0001
mdpa_rel	ZOthr	Categorical of dpa (down payment assistance)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.1124	0.00313	<.0001
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 162

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mhpa2yb_DCLM	L085	Categorical of hpa2y_blended_r <sup>6</sup>	hpa2y_blended_r <= 80	0.1466	0.0104	<.0001
mhpa2yb_DCLM	Z000	Categorical of hpa2y_blended_r <sup>7</sup>	base level: else			
vhpa2yb_DCLM_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-80,98-80)	-0.0105	0.000505	<.0001
vhpa2yb_DCLM_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-98,108-98)	0.0437	0.000479	<.0001
vhpa2yb_DCLM_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-108,117-108)	-0.018	0.000457	<.0001
vhpa2yb_DCLM_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-117,180-117)	-0.0142	0.000377	<.0001
mperiodnbr_DCLM	L02	Categorical of period_number	period number <= 2	-1.2898	0.1435	<.0001
mperiodnbr_DCLM	L03	Categorical of period_number	period number = 3	-0.9782	0.043	<.0001
mperiodnbr_DCLM	L04	Categorical of period_number	period number = 4	-0.3877	0.0201	<.0001
mperiodnbr_DCLM	Z05	Categorical of period_number	base level: else			
vperiodnbr_DCLM_pw1		Variate piecewise of period_number	median(0,period_number-5,9-5)	0.0595	0.00221	<.0001
vperiodnbr_DCLM_pw2		Variate piecewise of period_number	median(0,period_number-9,17-9)	0.0211	0.000652	<.0001
vperiodnbr_DCLM_pw3		Variate piecewise of period_number	median(0,period_number-17,60-17)	0.00149	0.000203	<.0001
vperiodnbr_DCLM_pw4		Variate piecewise of period_number	median(0,period_number-60,86-60)	-0.00847	0.000705	<.0001
mcredit_DCLM	L01	Categorical of credit_score	credit_score = 0	0.0495	0.00549	<.0001
mcredit_DCLM	Z00	Categorical of credit_score	base level: else			
vcredit_DCLM_pw1		Variate piecewise of credit_score	median(0,credit_score-525,635-525)	0.000932	0.000056	<.0001
vcredit_DCLM_pw2		Variate piecewise of credit_score	median(0,credit_score-635,780-635)	0.0044	0.000049	<.0001
mdurdefepi_DCLM	Z01	Categorical of dur_def_episode (duration of default episode)	Base level: dur_def_episode <= 1			
mdurdefepi_DCLM	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	0.8523	0.00548	<.0001
mdurdefepi_DCLM	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	1.3863	0.00532	<.0001
mdurdefepi_DCLM	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	1.6283	0.00539	<.0001
mdurdefepi_DCLM	L05	Categorical of dur_def_episode	dur_def_episode = 5	1.722	0.00558	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 163

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
mdurdefepi_DCLM	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	1.7261	0.00586	<.0001
mdurdefepi_DCLM	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	1.7009	0.00618	<.0001
mdurdefepi_DCLM	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	1.6702	0.00654	<.0001
mdurdefepi_DCLM	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	1.6425	0.00694	<.0001
mdurdefepi_DCLM	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	1.6159	0.00735	<.0001
mdurdefepi_DCLM	L11	Categorical of dur_def_episode (duration of default episode)	else	1.5936	0.00607	<.0001
vdurdefepi_DCLM_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	-0.00868	0.000519	<.0001
vdurdefepi_DCLM_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-30,40-30)	-0.0576	0.00221	<.0001
vdeltaUEInit_DCLM_pw1		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-0,63-0)	-0.00576	0.000346	<.0001
vdeltaUEInit_DCLM_pw2		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-63,100-63)	0.00196	0.000147	<.0001
vdeltaUEInit_DCLM_pw3		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-100,116-100)	0.00325	0.000273	<.0001
vdeltaUEInit_DCLM_pw4		Variate piecewise of DeltaUEInit_r <sup>4</sup>	median(0,DeltaUEInit_r-116,218-116)	0.00136	0.000056	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 164

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(change in unemployment rate from policy inception to current)				
mRatioTmpTei_DCLM	L00	Categorical of ratio_tmp_te1 (front-end ratio)	ratio_tmp_te1=0	0.0629	0.0105	<.0001
mRatioTmpTei_DCLM	Z00	Categorical of ratio_tmp_te1 (front-end ratio)	base level: else			
vratiotmpte1_DCLM_pw1		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-0,24-0)	0.00438	0.00038	<.0001
vratiotmpte1_DCLM_pw2		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-24,36-24)	0.00421	0.000343	<.0001
vratiotmpte1_DCLM_pw3		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-36,50-36)	-0.00895	0.000717	<.0001
mpriordef_DCLM	Z00	Categorical of prior_default_cnt	base level: prior_default_cnt = 0			
mpriordef_DCLM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.2267	0.00297	<.0001
mpriordef_DCLM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.3896	0.00399	<.0001
mpriordef_DCLM	L03	Categorical of prior_default_cnt	prior_default_cnt = 3	-0.5096	0.00511	<.0001
mpriordef_DCLM	L04	Categorical of prior_default_cnt	prior_default_cnt = 4	-0.6159	0.00644	<.0001
mpriordef_DCLM	L05	Categorical of prior_default_cnt	prior_default_cnt = 5	-0.7231	0.00814	<.0001
mpriordef_DCLM	L06	Categorical of prior_default_cnt	prior_default_cnt = 6	-0.8446	0.0104	<.0001
mpriordef_DCLM	L07	Categorical of prior_default_cnt	prior_default_cnt = 7	-0.9356	0.0133	<.0001
mpriordef_DCLM	L08	Categorical of prior_default_cnt	prior_default_cnt = 8	-1.0252	0.0173	<.0001
mpriordef_DCLM	L09	Categorical of prior_default_cnt	prior_default_cnt = 9	-1.104	0.0226	<.0001
mpriordef_DCLM	L10	Categorical of prior_default_cnt	prior_default_cnt = 10	-1.1482	0.0296	<.0001
mpriordef_DCLM	L11	Categorical of prior_default_cnt	prior_default_cnt = 11	-1.2645	0.0403	<.0001
mpriordef_DCLM	L12	Categorical of prior_default_cnt	prior_default_cnt >= 12	-1.4973	0.0392	<.0001
vUEblend_DCLM_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r <sup>8</sup> -200,450-200)	0.00131	0.000035	<.0001
vUEblend_DCLM_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r <sup>8</sup> -450,850-450)	-0.00059	0.000012	<.0001
vUEblend_DCLM_pw3		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r <sup>8</sup> -850,1500-850)	-0.00012	0.000015	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 165

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vltv_DCLM_pw1		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-0,70-0)	0.00562	0.000467	<.0001
vltv_DCLM_pw2		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-70,81-70)	0.027	0.00062	<.0001
vltv_DCLM_pw3		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-81,91-81)	0.0132	0.000528	<.0001
vltv_DCLM_pw4		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-91,94-91)	0.0466	0.00151	<.0001
vltv_DCLM_pw5		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	max(0,ltv_i_r-94)	0.1003	0.00215	<.0001
vloanraw_DCLM_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-27000,65000-27000)	-1.28E-06	1.88E-07	<.0001
vloanraw_DCLM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-65000,120000-65000)	7.44E-07	6.87E-08	<.0001
vloanraw_DCLM_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-120000,500000-120000)	-1.42E-06	2.54E-08	<.0001
mDeltaTY10_DCLM	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (10 year treasury rate)	DeltaTy10Init_r <sup>2</sup> < 53	0.1223	0.0034	<.0001
mDeltaTY10_DCLM	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (10 year treasury rate)	DeltaTy10Init_r <sup>2</sup> > 130	-0.363	0.00972	<.0001
mDeltaTY10_DCLM	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (10 year treasury rate)	base level: else			
mprior3_ue_DCLM	L01	Categorical of prior3_ue_r <sup>11</sup> (state unemployment 3 prior quarters)	prior3_ue_r <sup>11</sup> < 1400	-0.4479	0.0163	<.0001
mprior3_ue_DCLM	Z00	Categorical of prior3_ue_r <sup>11</sup> (state unemployment 3 prior quarters)	base level: else			
mcalperiod_DCLM	L02	Categorical of Calendar Period	period < 199704	0.3487	0.00936	<.0001
mcalperiod_DCLM	z	Categorical of Calendar Period	base level: else			
mTY30_DCLM	L01	Categorical of treasury_yr_30 (30 year treasury rate)	treasury_yr_30 > 6	0.2393	0.0079	<.0001
mTY30_DCLM	Z00	Categorical of treasury_yr_30 (30 year treasury rate)	base level: else			

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 166

## Default Transition Model Parameters – FRM30NSR D\_CXM

The model parameters for the FRM30NSR default to modified cure transition are shown below.

Table 46: Default to Modified Cure Transition FRM30NSR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-6.2059	0.0489	<.0001
mcalperiod_DCXM	L01	Categorical of Calendar Period	period < 200604	-6.6094	0.0544	<.0001
mcalperiod_DCXM	z	Categorical of Calendar Period	base level: else			
mseason	1	Categorical of season	season = "winter"	-0.00645	0.0034	0.0581
mseason	2	Categorical of season	season = "spring"	0.1672	0.00328	<.0001
mseason	3	Categorical of season	season = "summer"	0.113	0.00332	<.0001
mseason	4	Categorical of season	base level: season = "fall"			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.0676	0.00244	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mdpa_govt	LGovt	Categorical of dpa (down payment assistance)	dpa = "govt"	-0.0675	0.00724	<.0001
mdpa_govt	ZOthr	Categorical of dpa (down payment assistance)	base level: else			
mdpa_rel	LRela	Categorical of dpa (down payment assistance)	dpa = "Relative"	-0.0456	0.00327	<.0001
mdpa_rel	ZOthr	Categorical of dpa (down payment assistance)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.061	0.00288	<.0001
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
myslope_DCXM	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=300	0.0696	0.00469	<.0001
myslope_DCXM	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=900	-0.1541	0.00396	<.0001
myslope_DCXM	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=1500	-0.1272	0.00387	<.0001
myslope_DCXM	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
mhpa2yb_DCXM	L085	Categorical of hpa2y_blended_r <sup>6</sup>	hpa2y_blended_r <sup>6</sup> <= 85	-0.0629	0.0057	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 167

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mhpa2yb_DCXM	Z000	Categorical of hpa2y_blended_r <sup>6</sup>	base level: else			
vhpa2yb_DCXM_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-106,111-106)	0.00468	0.00093	<.0001
vhpa2yb_DCXM_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-111,121-111)	0.0105	0.000649	<.0001
vhpa2yb_DCXM_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-121,180-121)	0.00541	0.000684	<.0001
mperiodnbr_DCXM	L02	Categorical of period_number	period_number <= 2	-0.8846	0.1113	<.0001
mperiodnbr_DCXM	L03	Categorical of period_number	eriod_number = 3 , else mperiodnbr_DCXM="Z04"	-0.2622	0.0337	<.0001
mperiodnbr_DCXM	Z04	Categorical of period_number	base level: else			
vperiodnbr_DCXM_pw1		Variate piecewise of period_number	median(0,period_number-4,9-4)	0.2144	0.00233	<.0001
vperiodnbr_DCXM_pw2		Variate piecewise of period_number	median(0,period_number-9,15-9)	-0.0402	0.00102	<.0001
vperiodnbr_DCXM_pw3		Variate piecewise of period_number	median(0,period_number-15,25-15)	0.00647	0.000545	<.0001
vperiodnbr_DCXM_pw4		Variate piecewise of period_number	median(0,period_number-25,59-25)	-0.00412	0.000257	<.0001
vperiodnbr_DCXM_pw5		Variate piecewise of period_number	median(0,period_number-59,90-59)	-0.00387	0.000566	<.0001
mcredit_DCXM	L01	Categorical of credit_score	credit_score = 0, else mcredit_DCXM = "Z00"	-0.0372	0.0052	<.0001
mcredit_DCXM	Z00	Categorical of credit_score	base level: else			
vcredit_DCXM_pw1		Variate piecewise of credit_score	median(0,credit_score-530,640-530)	-0.0021	0.000052	<.0001
vcredit_DCXM_pw2		Variate piecewise of credit_score	median(0,credit_score-640,680-640)	-0.00165	0.000128	<.0001
vcredit_DCXM_pw3		Variate piecewise of credit_score	median(0,credit_score-680,780-680)	-0.00194	0.000112	<.0001
mdurdefepi_DCXM	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <=1			
mdurdefepi_DCXM	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	0.5106	0.00375	<.0001
mdurdefepi_DCXM	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	0.6766	0.00395	<.0001
mdurdefepi_DCXM	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	0.6805	0.00431	<.0001
mdurdefepi_DCXM	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	0.611	0.00481	<.0001
mdurdefepi_DCXM	L06	Categorical of dur_def_episode	dur_def_episode = 6	0.5063	0.00544	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 168

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
mdurdefepi_DCXM	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	0.3743	0.00624	<.0001
mdurdefepi_DCXM	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	0.2596	0.00713	<.0001
mdurdefepi_DCXM	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	0.1321	0.0082	<.0001
mdurdefepi_DCXM	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 10	-0.1111	0.00672	<.0001
vdurdefepi_DCXM_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,23-10)	-0.0652	0.00114	<.0001
vdurdefepi_DCXM_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-23,40-23)	0.00973	0.00186	<.0001
vdeltaUEInit_DCXM_pw1		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-0,66-0)	0.00616	0.00027	<.0001
vdeltaUEInit_DCXM_pw2		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-66,95-66)	-0.00301	0.000168	<.0001
vdeltaUEInit_DCXM_pw3		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-95,230-95)	0.000556	0.000045	<.0001
vdeltaUEInit_DCXM_pw4		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-230,300-230)	-0.00048	0.000151	0.0014
mRatioTmpTei_DCXM	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0, else MRatioTmpTei_DCXM = "Z00"	0.8468	0.0335	<.0001



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 169

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mRatioTmpTei_DCXM	Z00	Categorical of ratio_tmp_te1 (front-end ratio)	base level: else			
vratiotmpte1_DCXM_pw1		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-0,14-0)	0.0408	0.00215	<.0001
vratiotmpte1_DCXM_pw2		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-14,26-14)	0.0223	0.000413	<.0001
vratiotmpte1_DCXM_pw3		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-26,44-26)	0.00484	0.000287	<.0001
vratiotmpte1_DCXM_pw4		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-44,52-44)	-0.0232	0.00239	<.0001
mpriordef_DCXM	Z00	Categorical of prior_default_cnt	base level: prior_default_cnt = 0			
mpriordef_DCXM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	0.1785	0.00341	<.0001
mpriordef_DCXM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	0.2364	0.00394	<.0001
mpriordef_DCXM	L03	Categorical of prior_default_cnt	prior_default_cnt = 3	0.2747	0.00458	<.0001
mpriordef_DCXM	L04	Categorical of prior_default_cnt	prior_default_cnt = 4	0.2881	0.00535	<.0001
mpriordef_DCXM	L05	Categorical of prior_default_cnt	prior_default_cnt = 5	0.2864	0.0063	<.0001
mpriordef_DCXM	L06	Categorical of prior_default_cnt	prior_default_cnt = 6	0.2621	0.0075	<.0001
mpriordef_DCXM	L07	Categorical of prior_default_cnt	prior_default_cnt = 7	0.2408	0.00905	<.0001
mpriordef_DCXM	L08	Categorical of prior_default_cnt	prior_default_cnt = 8	0.2103	0.0111	<.0001
mpriordef_DCXM	L09	Categorical of prior_default_cnt	prior_default_cnt = 9	0.1613	0.0139	<.0001
mpriordef_DCXM	L10	Categorical of prior_default_cnt	prior_default_cnt = >10	0.1542	0.015	<.0001
vpriordef_DCXM_pw1		Variate of prior_default_cnt	median(0,prior_default_cnt-10,16-10)	-0.0616	0.00718	<.0001
vsato_DCXM_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-(-.6))	0.2738	0.0103	<.0001
vsato_DCXM_pw2		Variate piecewise of sato (spread at origination)	median(sato-(-.6),0,9-(-.6))	0.0817	0.00319	<.0001
vsato_DCXM_pw3		Variate piecewise of sato (spread at origination)	median(sato-.9,0,1.82-.9)	-0.0995	0.0116	<.0001
vltv_DCXM_pw1		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-0,69-0)	0.00396	0.000478	<.0001
vltv_DCXM_pw2		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-69,80-69)	0.00218	0.000647	0.0007
vltv_DCXM_pw3		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-80,85-80)	0.00379	0.00117	0.0012

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 170

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vltv_DCXM_pw4		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-85,91-85)	0.00925	0.000927	<.0001
vltv_DCXM_pw5		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-91,94-91)	-0.0242	0.00199	<.0001
vltv_DCXM_pw6		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_r-94,99-94)	0.0928	0.00367	<.0001
vloanraw_DCXM_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,70000-0)	8.00E-06	2.65E-07	<.0001
vloanraw_DCXM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-70000,98000-70000)	5.73E-06	1.80E-07	<.0001
vloanraw_DCXM_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-98000,180000-98000)	1.60E-06	5.27E-08	<.0001
vloanraw_DCXM_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-180000,500000-180000)	1.47E-07	2.95E-08	<.0001
mDeltaTY10_DCXM	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	-0.214	0.00354	<.0001
mDeltaTY10_DCXM	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r > 108, else mDeltaTY10_DCXM = "Z00"	0.0573	0.00464	<.0001
mDeltaTY10_DCXM	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
vsBOI_DCXM_pw1		Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-85,100-85)	-0.00535	0.000543	<.0001
vsBOI_DCXM_pw2		Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-100,108-100)	-0.0438	0.000932	<.0001

### Default Transition Model Parameters – FRM30NSR D\_CXS

The model parameters for the FRM30NSR default to self-cure transition are shown below.

Table 47: Default to Self-Cure Transition FRM30NSR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				0.714	0.0161	<.0001
mseason	1	Categorical of season	season = "winter"	0.2213	0.00151	<.0001
mseason	2	Categorical of season	season = "spring"	0.2706	0.00153	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 171

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mseason	3	Categorical of season	season = "summer"	0.1007	0.0016	<.0001
mseason	4	Categorical of season	base level: season = "fall"			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.119	0.00111	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mdpa_rel	LRela	Categorical of dpa (down payment assistance)	dpa = "Relative"	0.0563	0.00146	<.0001
mdpa_rel	ZOthr	Categorical of dpa (down payment assistance)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.0405	0.0013	<.0001
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
myslope_DCXS	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=111	0.0129	0.00194	<.0001
myslope_DCXS	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=2000	0.0585	0.00193	<.0001
myslope_DCXS	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=875	0.0288	0.00237	<.0001
myslope_DCXS	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
mhpa2yb_DCXS	L080	Categorical of hpa2y_blended_r <sup>6</sup>	hpa2y_blended_r <= 80	-0.0494	0.00534	<.0001
mhpa2yb_DCXS	Z000	Categorical of hpa2y_blended_r <sup>6</sup>	base level: else			
vhpa2yb_DCXS_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-80,99-80)	0.0134	0.000228	<.0001
vhpa2yb_DCXS_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-99,105-99)	-0.0164	0.000425	<.0001
vhpa2yb_DCXS_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-105,115-105)	0.0073	0.000206	<.0001
vhpa2yb_DCXS_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-115,180-115)	0.00312	0.00016	<.0001
mperiodnbr_DCXS	L02	Categorical of period_number	period_number <= 2	1.2972	0.0115	<.0001
mperiodnbr_DCXS	L03	Categorical of period_number	period_number = 3	0.4684	0.00553	<.0001
mperiodnbr_DCXS	Z04	Categorical of period_number	base level: else			
vperiodnbr_DCXS_pw1		Variate piecewise of period_number	median(0,period_number-4,9-4)	-0.07	0.000703	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 172

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vperiodnbr_DCXS_pw2		Variate piecewise of period_number	median(0,period_number-9,17-9)	-0.00157	0.000336	<.0001
vperiodnbr_DCXS_pw3		Variate piecewise of period_number	median(0,period_number-17,30-17)	0.0159	0.000217	<.0001
vperiodnbr_DCXS_pw4		Variate piecewise of period_number	median(0,period_number-30,38-30)	0.00886	0.000356	<.0001
vperiodnbr_DCXS_pw5		Variate piecewise of period_number	median(0,period_number-38,57-38)	0.00907	0.000213	<.0001
vperiodnbr_DCXS_pw6		Variate piecewise of period_number	median(0,period_number-57,85-57)	0.00259	0.000223	<.0001
vperiodnbr_DCXS_pw7		Variate piecewise of period_number	median(0,period_number-85,105-85)	-0.0093	0.000704	<.0001
mcredit_DCXS	L01	Categorical of credit_score	credit_score = 0	0.1502	0.00354	<.0001
mcredit_DCXS	Z00	Categorical of credit_score	base level: else			
vcredit_DCXS_pw1		Variate piecewise of credit_score	median(0,credit_score-500,625-500)	0.00315	0.000032	<.0001
vcredit_DCXS_pw2		Variate piecewise of credit_score	median(0,credit_score-625,680-625)	0.00346	0.000042	<.0001
vcredit_DCXS_pw3		Variate piecewise of credit_score	median(0,credit_score-680,780-680)	0.000399	0.000044	<.0001
mdurdefepi_DCXS	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <=1			
mdurdefepi_DCXS	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.6065	0.0014	<.0001
mdurdefepi_DCXS	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-0.9723	0.00178	<.0001
mdurdefepi_DCXS	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-1.3375	0.00231	<.0001
mdurdefepi_DCXS	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	-1.5469	0.00282	<.0001
mdurdefepi_DCXS	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	-1.7624	0.00343	<.0001
mdurdefepi_DCXS	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	-1.9562	0.00414	<.0001
mdurdefepi_DCXS	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	-2.1354	0.00495	<.0001
mdurdefepi_DCXS	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	-2.2468	0.00566	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 173

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mdurdefepi_DCXS	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	-2.391	0.00652	<.0001
mdurdefepi_DCXS	L11	Categorical of dur_def_episode (duration of default episode)	else	-2.5275	0.00715	<.0001
vdurdefepi_DCXS_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,16-10)	-0.0171	0.00173	<.0001
vdurdefepi_DCXS_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-16,30-16)	-0.00889	0.00074	<.0001
vdeltaUEInit_DCXS_pw1		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-0,60-0)	0.00313	0.000154	<.0001
vdeltaUEInit_DCXS_pw2		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-60,100-60)	-0.00349	0.000066	<.0001
vdeltaUEInit_DCXS_pw3		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-100,116-100)	-0.00827	0.00014	<.0001
vdeltaUEInit_DCXS_pw4		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-116,218-116)	-0.00189	0.000032	<.0001
vdeltaUEInit_DCXS_pw5		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-218,330-218)	-0.00042	0.000063	<.0001
mRatioTmpTei_DCXS	L00	Categorical of ratio_tmp_teI (front-end ratio)	ratio_tmp_teI=0	-0.4107	0.00589	<.0001
mRatioTmpTei_DCXS	Z00	Categorical of ratio_tmp_teI (front-end ratio)	base level: else			

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 174

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vratiotmptei_DCXS_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	-0.0166	0.000172	<.0001
vratiotmptei_DCXS_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	-0.0115	0.000167	<.0001
vratiotmptei_DCXS_pw3		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-36,50-36)	-0.00542	0.000345	<.0001
mpriordef_DCXS	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.1197	0.00157	<.0001
mpriordef_DCXS	L02	Categorical of prior_default_cnt	prior_default_cnt > 1	-0.1664	0.0018	<.0001
mpriordef_DCXS	Z00	Categorical of prior_default_cnt	base: prior_default_cnt = 0			
vpriordef_DCXS_pw1		Variate of prior_default_cnt	median(0,prior_default_cnt-1,22-1)	0.00551	0.000374	<.0001
vdeltaUEpr3_DCXS_pw1		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(0,delta_ue_sa_st_r(-20),-30(-20))	0.00294	0.000176	<.0001
vdeltaUEpr3_DCXS_pw2		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(0,delta_ue_sa_st_r(-20),10(-20))	-0.00119	0.00007	<.0001
vUEblend_DCXS_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-200,480-200)	-0.00075	0.000013	<.0001
vUEblend_DCXS_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-480,800-480)	-0.00054	7.39E-06	<.0001
vltv_DCXS_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,71-0)	-0.00413	0.000167	<.0001
vltv_DCXS_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-71,81-71)	-0.00982	0.000213	<.0001
vltv_DCXS_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-81,85-81)	-0.00481	0.000355	<.0001
vltv_DCXS_pw4		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-85,92-85)	-0.05	0.000917	<.0001
vltv_DCXS_pw5		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-92,95-92)	-0.1622	0.00201	<.0001
vloanraw_DCXS_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-27000,70000-27000)	3.27E-07	8.86E-08	0.0002
vloanraw_DCXS_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-70000,98000-70000)	-1.13E-06	7.51E-08	<.0001
vloanraw_DCXS_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-98000,180000-98000)	-5.80E-07	2.57E-08	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 175

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vloanraw_DCXS_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-180000,500000-180000)	-3.56E-07	1.56E-08	<.0001
mDeltaTY10_DCXS	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r <sup>2</sup> < 53	-0.0485	0.00183	<.0001
mDeltaTY10_DCXS	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r <sup>2</sup> > 112	0.1535	0.00198	<.0001
mDeltaTY10_DCXS	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
mDeltaTm3_DCXS	L01	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	DeltaTm3Init_r <sup>12</sup> > 1000	0.129	0.0023	<.0001
mDeltaTm3_DCXS	Z00	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	base level: else			
mTY30_DCXS	L01	Categorical of treasury_yr_30	treasury_yr_30 > 6	-0.1476	0.0055	<.0001
mTY30_DCXS	Z00	Categorical of treasury_yr_31	base level: else			
mcalperiod_DCXS	L01	Categorical of Calendar Period	period < 200102	-0.6177	0.00416	<.0001
mcalperiod_DCXS	z	Categorical of Calendar Period	base level: else			
vSBOI_DCXS_pw1		Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-85,100-85)	-0.0338	0.000243	<.0001
vSBOI_DCXS_pw2		Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-100,108-100)	0.00997	0.000402	<.0001

Default Transition Model Parameters – FRM30NSR D\_END

The model parameters for the FRM30NSR default to end (prepayment or refinance) transition are shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 176

Table 48: Default to End Transition FRM30NSR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-1.3141	0.0591	<.0001
mseason	1	Categorical of season	season = "winter"	-0.1416	0.00502	<.0001
mseason	2	Categorical of season	season = "spring"	0.0783	0.0049	<.0001
mseason	3	Categorical of season	season = "summer"	0.1011	0.00493	<.0001
mseason	4	Categorical of season	base level: season = "fall"			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.1979	0.00364	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	-0.2333	0.0133	<.0001
mdpa	2	Categorical of dpa (down payment assistance)	dpa = "nonprof"	-0.3917	0.00794	<.0001
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	0.0621	0.00473	<.0001
mdpa	4	Categorical of dpa (down payment assistance)	base level: dpa = "na_other"			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.0761	0.0042	<.0001
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
myslope_DEND	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=111	0.1746	0.00576	<.0001
myslope_DEND	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=875	-0.6331	0.00798	<.0001
myslope_DEND	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=2000	-0.7775	0.0092	<.0001
myslope_DEND	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
mhpa2yb_DEND	L085	Categorical of hpa2y_blended_r <sup>6</sup>	hpa2y_blended_r <= 80	0.0724	0.0226	0.0014
mhpa2yb_DEND	Z00	Categorical of hpa2y_blended_r <sup>6</sup>	base level: else			
vhpa2yb_DEND_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-80,105-80)	0.0182	0.000705	<.0001
vhpa2yb_DEND_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-105,120-105)	0.0633	0.000408	<.0001



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 177

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vhpa2yb_DEND_pw3		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-120,180-120)	0.0399	0.000313	<.0001
mperiodnbr_DEND	L02	Categorical of period_number	period_number = 2	0.2213	0.0503	<.0001
mperiodnbr_DEND	L03	Categorical of period_number	period_number = 3	-0.0268	0.0222	0.2278
mperiodnbr_DEND	L04	Categorical of period_number	period_number = 4	-0.1572	0.0166	<.0001
mperiodnbr_DEND	L05	Categorical of period_number	period_number = 5	-0.1655	0.0143	<.0001
mperiodnbr_DEND	L06	Categorical of period_number	period_number = 6	-0.1749	0.013	<.0001
mperiodnbr_DEND	L07	Categorical of period_number	period_number = 7	-0.1979	0.0121	<.0001
mperiodnbr_DEND	L08	Categorical of period_number	period_number = 8	-0.1994	0.0117	<.0001
mperiodnbr_DEND	L09	Categorical of period_number	period_number = 9	-0.1063	0.011	<.0001
mperiodnbr_DEND	Z10	Categorical of period_number	base level: else			
vperiodnbr_DEND_pw1		Variate piecewise of period_number	median(0,period_number-10,65-10)	0.00847	0.000251	<.0001
vperiodnbr_DEND_pw2		Variate piecewise of period_number	median(0,period_number-65,90-65)	0.00561	0.000991	<.0001
vperiodnbr_DEND_pw3		Variate piecewise of period_number	median(0,period_number-90,114-90)	0.00906	0.00274	0.0009
mcredit_DEND	L01	Categorical of credit_score	credit_score = 0	0.4273	0.0244	<.0001
mcredit_DEND	Z00	Categorical of credit_score	base level: else			
vcredit_DEND_pw1		Variate piecewise of credit_score	median(0,credit_score-450,600-450)	0.000286	0.000178	0.1091
vcredit_DEND_pw2		Variate piecewise of credit_score	median(0,credit_score-600,680-600)	0.0047	0.000117	<.0001
vcredit_DEND_pw3		Variate piecewise of credit_score	median(0,credit_score-680,780-680)	0.00372	0.000137	<.0001
mdurdefepi_DEND	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <=1			
mdurdefepi_DEND	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.5016	0.00507	<.0001
mdurdefepi_DEND	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-0.7054	0.00617	<.0001
mdurdefepi_DEND	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-0.8659	0.00736	<.0001
mdurdefepi_DEND	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	-0.9734	0.00858	<.0001
mdurdefepi_DEND	L06	Categorical of dur_def_episode	dur_def_episode = 6	-1.0586	0.00974	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 178

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
mdurdefepi_DEND	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	-1.157	0.011	<.0001
mdurdefepi_DEND	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	-1.1948	0.0121	<.0001
mdurdefepi_DEND	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	-1.2571	0.0134	<.0001
mdurdefepi_DEND	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	-1.2472	0.0142	<.0001
mdurdefepi_DEND	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >10	-1.32	0.00942	<.0001
vdurdefepi_DEND_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	0.00432	0.000995	<.0001
vdurdefepi_DEND_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-30,40-30)	-0.0351	0.00326	<.0001
vdeltaUEInit_DEND_pw1		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-0,63-0)	-0.00712	0.000367	<.0001
vdeltaUEInit_DEND_pw2		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-63,100-63)	-0.00146	0.000215	<.0001
vdeltaUEInit_DEND_pw3		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-100,116-100)	0.006	0.000454	<.0001
vdeltaUEInit_DEND_pw4		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy	median(0,DeltaUEInit_r-116,200-116)	-0.0019	0.000126	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 179

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		inception to current)				
mRatioTmpTei_DEND	L00	Categorical of ratio_tmp_te_i (front-end ratio)	ratio_tmp_te_i=0	-0.5502	0.0278	<.0001
mRatioTmpTei_DEND	Z00	Categorical of ratio_tmp_te_i (front-end ratio)	base level: else			
vratiotmpte_i_DEND_pw1		Variate piecewise of ratio_tmp_te_i (front-end ratio)	median(0,ratio_tmp_te_i-0,15-0)	-0.0346	0.00184	<.0001
vratiotmpte_i_DEND_pw2		Variate piecewise of ratio_tmp_te_i (front-end ratio)	median(0,ratio_tmp_te_i-15,24-15)	-0.00955	0.000759	<.0001
vratiotmpte_i_DEND_pw3		Variate piecewise of ratio_tmp_te_i (front-end ratio)	median(0,ratio_tmp_te_i-24,50-24)	-0.00361	0.000376	<.0001
mpriordef_DEND	Z00	Categorical of prior_default_cnt	base level: prior_default_cnt = 0			
mpriordef_DEND	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.305	0.00473	<.0001
mpriordef_DEND	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.5175	0.0062	<.0001
mpriordef_DEND	L03	Categorical of prior_default_cnt	prior_default_cnt = 3	-0.6852	0.00779	<.0001
mpriordef_DEND	L04	Categorical of prior_default_cnt	prior_default_cnt = 4	-0.8266	0.00955	<.0001
mpriordef_DEND	L05	Categorical of prior_default_cnt	prior_default_cnt = 5	-0.9723	0.0117	<.0001
mpriordef_DEND	L06	Categorical of prior_default_cnt	prior_default_cnt = 6	-1.0592	0.0138	<.0001
mpriordef_DEND	L07	Categorical of prior_default_cnt	prior_default_cnt = 7	-1.1349	0.0164	<.0001
mpriordef_DEND	L08	Categorical of prior_default_cnt	prior_default_cnt = 8	-1.2071	0.0196	<.0001
mpriordef_DEND	L09	Categorical of prior_default_cnt	prior_default_cnt = 9	-1.3024	0.0239	<.0001
mpriordef_DEND	L10	Categorical of prior_default_cnt	prior_default_cnt >= 10	-1.4148	0.0186	<.0001
vsato_DEND_pw1		Variate piecewise of sato (spread at origination)	median(sato-(-.4),0,.95-(-.4))	0.038	0.00457	<.0001
vsato_DEND_pw2		Variate piecewise of sato (spread at origination)	median(sato-.95,0,1.82-.95)	0.1034	0.017	<.0001
vdeltaUEpr3_DEND_pw1		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(0,delta_ue_sa_st_r-(-20),-30-(-20))	0.000907	0.00057	0.1117
vdeltaUEpr3_DEND_pw2		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(0,delta_ue_sa_st_r-(-20),10-(-20))	0.00513	0.00022	<.0001
vUEblend_DEND_pw1		Variate piecewise of ue_blended_r <sup>8</sup>	median(0,ue_blended_r-0,450-0)	-0.00153	0.000045	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 180

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(unemployment rate)				
vUEblend_DEND_pw2		Variate piecewise of ue_bledned_r <sup>8</sup> (unemployment rate)	median(0,ue_bledned_r-450,850-450)	-0.00056	0.000022	<.0001
vUEblend_DEND_pw3		Variate piecewise of ue_bledned_r <sup>8</sup> (unemployment rate)	median(0,ue_bledned_r-850,1500-850)	-0.00034	0.00003	<.0001
vlv_DEND_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,55-0)	-0.00793	0.000735	<.0001
vlv_DEND_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-55,74-55)	-0.0247	0.000816	<.0001
vlv_DEND_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-74,84-74)	0.00415	0.000917	<.0001
vlv_DEND_pw4		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-84,90-84)	-0.0199	0.00124	<.0001
vlv_DEND_pw5		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-90,94-90)	-0.0565	0.0019	<.0001
vlv_DEND_pw6		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-94,99-94)	-0.1544	0.00441	<.0001
vloanraw_DEND_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-30000,70000-30000)	3.26E-06	2.85E-07	<.0001
vloanraw_DEND_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-70000,98000-70000)	5.20E-06	2.44E-07	<.0001
vloanraw_DEND_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-98000,180000-98000)	2.80E-06	8.57E-08	<.0001
vloanraw_DEND_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-180000,500000-180000)	8.07E-07	4.85E-08	<.0001
mDeltaTY10_DEND	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	-0.2375	0.00736	<.0001
mDeltaTY10_DEND	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
mprior3_ue_DEND	L01	Categorical of prior3_ue_r <sup>11</sup> (state unemployment 3 prior quarters)	prior3_ue_r <sup>11</sup> <1400	0.282	0.0304	<.0001
mprior3_ue_DEND	Z00	Categorical of prior3_ue_r <sup>11</sup> (state unemployment 3 prior quarters)	base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 181

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mcalperiod_DEND	L01	Categorical of Calendar Period	period < 200201	-0.3575	0.00931	<.0001
mcalperiod_DEND	z	Categorical of Calendar Period	base level: else			
vSBOI_DEND_pw1		Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-85,100-85)	0.00418	0.00118	0.0004
vSBOI_DEND_pw2		Variate piecewise of SBOI (small business optimism index)	median(0,mSBOI-100,108-100)	0.035	0.0014	<.0001
vCCI_DEND_pw1		Variate piecewise of SBOI (small business optimism index)	median(0,mCCI-25,100-25)	-0.00346	0.000275	<.0001
vCCI_DEND_pw2		Variate piecewise of SBOI (small business optimism index)	median(0,mCCI-100,142-100)	-0.0125	0.000307	<.0001

### Default Transition Model Parameters – FRM30SR D\_CLM

The model parameters for the FRM30SR default to claim transition are shown below.

Table 49: Default to Claim Transition FRM30SR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-3.4866	0.0767	<.0001
mseason_grp_DCLM	L02	Categorical of season	mseason = 2	0.0528	0.0063	<.0001
mseason_grp_DCLM	L03	Categorical of season	mseason = 3	0.0503	0.00637	<.0001
mseason_grp_DCLM	Z0104	Categorical of season	mseason in(1,4)			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.2493	0.00556	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mcalperiod_DCLM	L199704	Categorical of Calendar Period	period < 199704	1.1732	0.0187	<.0001
mcalperiod_DCLM	L200104	Categorical of Calendar Period	period < 200104	0.6824	0.0155	<.0001
mcalperiod_DCLM	L200604	Categorical of Calendar Period	period < 200604	0.1167	0.012	<.0001
mcalperiod_DCLM	Z	Categorical of Calendar Period	base level: else			
myslope_DCLM	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=141	-0.1641	0.00935	<.0001
myslope_DCLM	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 182

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vycslope_DCLM_pw1		Variate of ycslope_r <sup>9</sup> (yield curve slope)	median(0,ycslope_r-141,478-141)	-0.00012	0.000012	<.0001
vycslope_DCLM_pw2		Variate of ycslope_r <sup>9</sup> (yield curve slope)	median(0,ycslope_r-478,1270-478)	0.000145	0.000001	<.0001
vhpa2yb_DCLM_pw1		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-45,85-45)	-0.0137	0.0013	<.0001
vhpa2yb_DCLM_pw2		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-85,100-85)	0.0254	0.00097	<.0001
vhpa2yb_DCLM_pw3		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-100,138-100)	-0.00361	0.000426	<.0001
vhpa2yb_DCLM_pw4		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-138,160-138)	-0.0407	0.00322	<.0001
mperiodnbr_DCLM	L02	Categorical of period_number	period_number <= 2	-0.6751	0.1873	0.0003
mperiodnbr_DCLM	L03	Categorical of period_number	period_number = 3	-0.3753	0.0602	<.0001
mperiodnbr_DCLM	L04	Categorical of period_number	period_number = 4	-0.1258	0.0338	0.0002
mperiodnbr_DCLM	L05	Categorical of period_number	period_number = 5	0.0968	0.0232	<.0001
mperiodnbr_DCLM	L06	Categorical of period_number	period_number = 6	0.1157	0.0193	<.0001
mperiodnbr_DCLM	L07	Categorical of period_number	period_number = 7	0.1219	0.0173	<.0001
mperiodnbr_DCLM	L08	Categorical of period_number	period_number = 8	0.0936	0.0163	<.0001
mperiodnbr_DCLM	Z00	Categorical of period_number	base level: else			
vperiodnbr_DCLM_pw1		Variate piecewise of period_number	median(0,period_number-9,17-9)	0.0123	0.00145	<.0001
vperiodnbr_DCLM_pw2		Variate piecewise of period_number	median(0,period_number-17,59-17)	0.0033	0.00043	<.0001
vperiodnbr_DCLM_pw3		Variate piecewise of period_number	median(0,period_number-59,86-59)	-0.0126	0.00195	<.0001
vcredit_DCLM_pw1		Variate piecewise of credit_score	median(0,credit_score-550,635-550)	-0.00108	0.000175	<.0001
vcredit_DCLM_pw2		Variate piecewise of credit_score	median(0,credit_score-635,780-635)	0.00478	0.000239	<.0001
mdurdefepi_DCLM	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <= 1			
mdurdefepi_DCLM	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	0.6767	0.0115	<.0001
mdurdefepi_DCLM	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	1.1759	0.0112	<.0001
mdurdefepi_DCLM	L04	Categorical of dur_def_episode	dur_def_episode = 4	1.4151	0.0115	<.0001

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 183

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
mdurdefepi_DCLM	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	1.5096	0.012	<.0001
mdurdefepi_DCLM	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	1.4941	0.0129	<.0001
mdurdefepi_DCLM	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	1.4874	0.0137	<.0001
mdurdefepi_DCLM	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	1.4251	0.0148	<.0001
mdurdefepi_DCLM	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	1.4233	0.0157	<.0001
mdurdefepi_DCLM	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	1.403	0.0168	<.0001
mdurdefepi_DCLM	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 11	1.3681	0.0181	<.0001
mdurdefepi_DCLM	L12	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 12	1.3254	0.0195	<.0001
mdurdefepi_DCLM	L13	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 13	1.3649	0.0205	<.0001
mdurdefepi_DCLM	L14	Categorical of dur_def_episode (duration of default episode)	else	1.3017	0.0157	<.0001
vdurdefepi_DCLM_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-13,40-13)	-0.0104	0.00157	<.0001
vdurdefepi_DCLM_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-40,50-40)	-0.1791	0.0195	<.0001
vdeltaUEinit_DCLM_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-0,53-0)	-0.0153	0.00106	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 184

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vdeltaUEinit_DCLM_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-53,98-53)	-0.011	0.000247	<.0001
vdeltaUEinit_DCLM_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-98,330-98)	0.00104	0.000106	<.0001
vratiotmptei_DCLM_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	0.00406	0.00035	<.0001
mpriordef_DCLM	Z00	Categorical of prior_default_cnt	base level: prior_default_cnt = 0			
mpriordef_DCLM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.3952	0.00703	<.0001
mpriordef_DCLM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.5871	0.00953	<.0001
mpriordef_DCLM	L03	Categorical of prior_default_cnt	prior_default_cnt = 3	-0.7458	0.0124	<.0001
mpriordef_DCLM	L04	Categorical of prior_default_cnt	prior_default_cnt = 4	-0.8891	0.0159	<.0001
mpriordef_DCLM	L05	Categorical of prior_default_cnt	prior_default_cnt = 5	-0.99	0.0203	<.0001
mpriordef_DCLM	L06	Categorical of prior_default_cnt	prior_default_cnt = 6	-1.1624	0.0273	<.0001
mpriordef_DCLM	L07	Categorical of prior_default_cnt	prior_default_cnt = 7	-1.2482	0.036	<.0001
mpriordef_DCLM	L08	Categorical of prior_default_cnt	prior_default_cnt = 8	-1.3963	0.0483	<.0001
mpriordef_DCLM	L09	Categorical of prior_default_cnt	else	-1.2198	0.0781	<.0001
vpriordef_DCLM_pw1		Variate of prior_default_cnt	median(0,prior_default_cnt-8,15-8)	-0.141	0.0324	<.0001
vdeltaUEpr3_DCLM_pw1		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(0,delta_ue_sa_st_r-(-20),-30-(-20))	-0.00273	0.000834	0.001
vdeltaUEpr3_DCLM_pw2		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(0,delta_ue_sa_st_r-(-20),10-(-20))	-0.00468	0.00035	<.0001
vUEblend_DCLM_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-200,550-200)	0.00255	0.000053	<.0001
vUEblend_DCLM_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-550,850-550)	-0.00047	0.000037	<.0001



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 185

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vUEblend_DCLM_pw3		Variate piecewise of ue_bledned_r <sup>8</sup> (unemployment rate)	median(0,ue_bledned_r-850,1500-850)	0.000293	0.000033	<.0001
vlvtv_DCLM_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-40,70-40)	0.00226	0.000543	<.0001
vlvtv_DCLM_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-70,81-70)	0.0246	0.00132	<.0001
vlvtv_DCLM_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-81,92-81)	0.00728	0.00097	<.0001
vlvtv_DCLM_pw4		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-92,100-92)	0.0367	0.00294	<.0001
vloanraw_DCLM_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-60000,100000-60000)	6.12E-06	2.64E-07	<.0001
vloanraw_DCLM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-100000,200000-100000)	-7.54E-07	9.65E-08	<.0001
vloanraw_DCLM_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,500000-200000)	-1.52E-06	7.45E-08	<.0001
mTY30_DCLM	L07	Categorical of treasury_yr_30	treasury_yr_30 > 7	0.4774	0.0343	<.0001
mTY30_DCLM	Z00	Categorical of treasury_yr_30	base level: else			

## Default Transition Model Parameters – FRM30SR D\_CXM

The model parameters for the FRM30SR default to modified cure transition are shown below.

Table 50: Default to Modified Cure Transition FRM30SR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-6.398	0.0955	<.0001
mcalperiod_DCXM	L200604	Categorical of Calendar Period	period < 200604	-6.1491	0.1385	<.0001
mcalperiod_DCXM	Z	Categorical of Calendar Period	base level: else			
mseason	1	Categorical of season	season = "winter"	-0.03	0.0079	0.0001
mseason	2	Categorical of season	season = "spring"	0.117	0.00771	<.0001
mseason	3	Categorical of season	season = "summer"	0.086	0.0078	<.0001
mseason	4	Categorical of season	base level: season = "fall"			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.0824	0.00598	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
vhpa2yb_DCXM_pw1		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-65,83-65)	0.016	0.00194	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 186

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vhpa2yb_DCXM_pw2		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-83,94-83)	-0.00832	0.00145	<.0001
vhpa2yb_DCXM_pw3		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-94,115-94)	0.00689	0.000629	<.0001
vhpa2yb_DCXM_pw4		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-115,140-115)	0.0078	0.00101	<.0001
mperiodnbr_DCXM	L02	Categorical of period_number	period_number <= 2	-1.038	0.2383	<.0001
mperiodnbr_DCXM	L03	Categorical of period_number	period_number = 3	-0.5827	0.0864	<.0001
mperiodnbr_DCXM	L04	Categorical of period_number	period_number = 4	-0.3524	0.0569	<.0001
mperiodnbr_DCXM	Z00	Categorical of period_number	base level: else			
vperiodnbr_DCXM_pw1		Variate piecewise of period_number	median(0,period_number-4,8-4)	0.233	0.00859	<.0001
vperiodnbr_DCXM_pw2		Variate piecewise of period_number	median(0,period_number-8,12-8)	-0.0625	0.00372	<.0001
vperiodnbr_DCXM_pw3		Variate piecewise of period_number	median(0,period_number-12,21-12)	0.026	0.00132	<.0001
vperiodnbr_DCXM_pw4		Variate piecewise of period_number	median(0,period_number-21,59-21)	-0.00427	0.000473	<.0001
mdurdefepi_DCXM	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <=1			
mdurdefepi_DCXM	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	0.4806	0.00862	<.0001
mdurdefepi_DCXM	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	0.5689	0.00923	<.0001
mdurdefepi_DCXM	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	0.5301	0.0102	<.0001
mdurdefepi_DCXM	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	0.4268	0.0115	<.0001
mdurdefepi_DCXM	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	0.3425	0.013	<.0001
mdurdefepi_DCXM	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	0.2034	0.015	<.0001
mdurdefepi_DCXM	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	0.0729	0.014	<.0001
vdurdefepi_DCXM_pw1		Variate piecewise of	median(0,dur_def_episode-7,23-7)	-0.079	0.00215	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 187

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		dur_def_episode (duration of default episode)				
vdurdefepi_DCXM_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-23,40-23)	0.0258	0.00519	<.0001
vdeltaUEinit_DCXM_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-0,66-0)	0.00702	0.00057	<.0001
vdeltaUEinit_DCXM_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-66,90-66)			
vdeltaUEinit_DCXM_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-90,131-90)	0.00541	0.000277	<.0001
vdeltaUEinit_DCXM_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-131,200-131)	0.00256	0.000196	<.0001
mRatioTmpTei_DCXM	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.482	0.0444	<.0001
mRatioTmpTei_DCXM	Z01	Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_DCXM_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	0.0232	0.0022	<.0001
vratiotmptei_DCXM_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	0.0108	0.00199	<.0001
vratiotmptei_DCXM_pw3		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-36,100-36)	-0.00468	0.000919	<.0001
mpriordef_DCXM	Z00	Categorical of prior_default_cnt	base level: prior_default_cnt = 0			
mpriordef_DCXM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	0.197	0.00786	<.0001
mpriordef_DCXM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	0.2583	0.00915	<.0001
mpriordef_DCXM	L03	Categorical of prior_default_cnt	prior_default_cnt = 3	0.278	0.0107	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 188

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_DCXM	L04	Categorical of prior_default_cnt	prior_default_cnt = 4	0.2847	0.0125	<.0001
mpriordef_DCXM	L05	Categorical of prior_default_cnt	prior_default_cnt >= 5	0.2608	0.0136	<.0001
vpriordef_DCXM_pw1		Variate pf prior_default_cnt	median(0,prior_default_cnt-5,9-5)	-0.024	0.0063	0.0001
vpriordef_DCXM_pw2		Variate pf prior_default_cnt	median(0,prior_default_cnt-9,14-9)	-0.0803	0.0131	<.0001
vsato_DCXM_pw1		Variate piecewise of sato (spread at origination)	median(sato-(-1.4),0,-6-(-1.4))	0.0219	0.00821	0.0076
vsato_DCXM_pw2		Variate piecewise of sato (spread at origination)	max(sato-.6,0)	0.1031	0.0281	0.0002
vUEblend_DCXM_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_r-200,420-200)	0.000877	0.000122	<.0001
vUEblend_DCXM_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_r-420,940-420)	-0.00062	0.000025	<.0001
vUEblend_DCXM_pw3		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_r-940,1500-940)	-0.00011	0.000042	0.0099
vltv_DCXM_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-48,82-48)	0.00295	0.000498	<.0001
vltv_DCXM_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-82,91-82)	0.0116	0.00103	<.0001
vloanraw_DCXM_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,70000-0)	0.00001	8.92E-07	<.0001
vloanraw_DCXM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-70000,120000-70000)	4.23E-06	2.18E-07	<.0001
vloanraw_DCXM_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-120000,400000-120000)	5.81E-07	4.74E-08	<.0001
mDeltaTy10_DCXM	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	-0.2023	0.00848	<.0001
mDeltaTy10_DCXM	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
mDeltaTM3_DCXM	L01	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy)	DeltaTM3Init_r < 3	-0.109	0.0101	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 189

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		inception to current)				
mDeltaTM3_DCXM	L02	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	DeltaTM3Init_r > 550	-0.2632	0.011	<.0001
mDeltaTM3_DCXM	Z00	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	base level: else			

### Default Transition Model Parameters – FRM30SR D\_CXS

The model parameters for the FRM30SR default to self-cure transition are shown below.

Table 51: Default to Self-Cure Transition FRM30SR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				0.3559	0.0254	<.0001
mcalperiod_DCXS	L200104	Categorical of Calendar Period	period < 200104	-1.2054	0.00848	<.0001
mcalperiod_DCXS	L200604	Categorical of Calendar Period	period < 200604	-0.7326	0.00636	<.0001
mcalperiod_DCXS	Z201800	Categorical of Calendar Period	base level: else			
mseason	1	Categorical of season	season = "winter"	0.1813	0.00362	<.0001
mseason	2	Categorical of season	season = "spring"	0.2532	0.00368	<.0001
mseason	3	Categorical of season	season = "summer"	0.1014	0.00379	<.0001
mseason	4	Categorical of season	base level: season = "fall"			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.1124	0.0028	<.0001
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mhpa2yb_DCXS	L085	Categorical of hpa2y_bleded_r <sup>6</sup>	hpa2y_bleded_r <= 80	0.0511	0.0126	<.0001
mhpa2yb_DCXS	Z000	Categorical of hpa2y_bleded_r <sup>6</sup>	base level: else			
vhpa2yb_DCXS_pw1		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-80,99-80)	0.00901	0.000535	<.0001
vhpa2yb_DCXS_pw2		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_r-99,105-99)	-0.00418	0.000962	<.0001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 190

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vhpa2yb_DCXS_pw3		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-105,116-105)	0.00959	0.000464	<.0001
vhpa2yb_DCXS_pw4		Variate piecewise of hpa2y_bledned_r <sup>6</sup>	median(0,hpa2y_bledned_r-116,180-116)	0.00858	0.000392	<.0001
mperiodnbr_DCXS	L02	Categorical of period_number	period_number <= 2	1.4079	0.0237	<.0001
mperiodnbr_DCXS	L03	Categorical of period_number	period_number = 3	0.6352	0.0121	<.0001
mperiodnbr_DCXS	L04	Categorical of period_number	period_number = 4	0.2595	0.01	<.0001
mperiodnbr_DCXS	L05	Categorical of period_number	period_number = 5	0.0274	0.00929	0.0032
mperiodnbr_DCXS	Z06	Categorical of period_number	base level: else			
vperiodnbr_DCXS_pw1		Variate piecewise of period_number	median(0,period_number-5,15-5)	-0.0219	0.000726	<.0001
vperiodnbr_DCXS_pw2		Variate piecewise of period_number	median(0,period_number-15,25-15)	0.0115	0.000563	<.0001
vperiodnbr_DCXS_pw3		Variate piecewise of period_number	median(0,period_number-25,57-25)	-0.001	0.000245	<.0001
vperiodnbr_DCXS_pw4		Variate piecewise of period_number	median(0,period_number-57,85-57)	0.00592	0.000585	<.0001
vperiodnbr_DCXS_pw5		Variate piecewise of period_number	median(0,period_number-85,105-85)	-0.00778	0.00223	0.0005
vcredit_DCXS_pw1		Variate piecewise of credit_score	median(0,credit_score-480,675-480)	0.000057	0.00003	0.0573
mdurdefepi_DCXS	Z01	Categorical of dur_def_episode (duration of default episode)	base level:dur_def_episode <=1			
mdurdefepi_DCXS	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.6663	0.00341	<.0001
mdurdefepi_DCXS	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-1.0509	0.00439	<.0001
mdurdefepi_DCXS	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-1.4123	0.00569	<.0001
mdurdefepi_DCXS	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	-1.6016	0.00693	<.0001
mdurdefepi_DCXS	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	-1.8105	0.00846	<.0001
mdurdefepi_DCXS	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	-2.0337	0.0104	<.0001
mdurdefepi_DCXS	L08	Categorical of dur_def_episode	dur_def_episode = 8	-2.1738	0.0123	<.0001

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 191

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
mdurdefepi_DCXS	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	-2.2996	0.0142	<.0001
mdurdefepi_DCXS	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	-2.4124	0.0162	<.0001
mdurdefepi_DCXS	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >10	-2.4481	0.0219	<.0001
vdurdefepi_DCXS_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,14-10)	-0.0546	0.00714	<.0001
vdurdefepi_DCXS_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-14,35-14)	-0.00405	0.00153	0.0081
vdeltaUEinit_DCXS_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-0,59-0)	0.00297	0.00035	<.0001
vdeltaUEinit_DCXS_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-95,104-95)	-0.0081	0.000501	<.0001
vdeltaUEinit_DCXS_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_r-104,200-104)	-0.00092	0.000077	<.0001
mRatioTmpTei_DCXS	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	-0.1949	0.00904	<.0001
mRatioTmpTei_DCXS	Z01	Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_DCXS_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-10,24-10)	-0.0125	0.000872	<.0001
vratiotmptei_DCXS_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,46-24)	-0.00592	0.000611	<.0001
mpriordef_DCXS	Z00	Categorical of prior_default_cnt	base level: prior_default_cnt = 0			

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 192

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_DCXS	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.0388	0.00376	<.0001
mpriordef_DCXS	L02	Categorical of prior_default_cnt	else	-0.0684	0.00374	<.0001
vsato_DCXS_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-0)	-0.067	0.00712	<.0001
vsato_DCXS_pw2		Variate piecewise of sato (spread at origination)	median(sato-0,0,.6-0)	-0.0929	0.00718	<.0001
vsato_DCXS_pw3		Variate piecewise of sato (spread at origination)	median(sato-.6,0,1.82-.6)	-0.0861	0.0118	<.0001
vdeltaUEpr3_DCXS_pw1		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	min(0,delta_ue_sa_st_r(-20))	0.00096	0.000063	<.0001
vdeltaUEpr3_DCXS_pw2		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(delta_ue_sa_st_r(-20),0,10-(-20))	0.00183	0.000142	<.0001
vdeltaUEpr3_DCXS_pw3		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	max(delta_ue_sa_st_r-10,0)	-0.00053	0.000036	<.0001
vUEblend_DCXS_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-200,473-200)	-0.00081	0.000034	<.0001
vUEblend_DCXS_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-473,750-473)	-0.00064	0.000019	<.0001
vUEblend_DCXS_pw3		Variate piecewise of ue_blended_r <sup>8</sup> (unemployment rate)	median(0,ue_blended_r-750,1500-750)	-0.00033	0.000014	<.0001
vltv_DCXS_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-69,85-69)	-0.00599	0.000333	<.0001
vltv_DCXS_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-85,94-85)	-0.0189	0.000602	<.0001
vltv_DCXS_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-94,99-94)	-0.0426	0.00247	<.0001
vloanraw_DCXS_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-27000,158000-27000)	-2.51E-06	4.73E-08	<.0001
vloanraw_DCXS_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-158000,520000-158000)	-4.62E-07	2.73E-08	<.0001
mDeltaTY10_DCXS	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year	DeltaTy10Init_r > 127	0.1953	0.00523	<.0001



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 193

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		Treasury rate from policy inception to current)				
mDeltaTY10_DCXS	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
mDeltaTm3_DCXS	L01	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	DeltaTm3Init_r > 1000	0.1421	0.00508	<.0001
mDeltaTm3_DCXS	Z00	Categorical of DeltaTm3Init_r <sup>12</sup> (change in 3 month treasury from policy inception to current)	base level: else			

### Default Transition Model Parameters – FRM30SR D\_END

The model parameters for the FRM30SR default to end (prepayment or refinance) transition are shown below.

Table 52: Default to End Transition FRM30SR Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	WaldChiSq
Intercept				-3.0706	0.0912	1132.572
mseason_grp_DEND	L02	Categorical of season	mseason = 2	0.1694	0.0101	278.925
mseason_grp_DEND	L03	Categorical of season	mseason = 3	0.1933	0.0104	344.9985
mseason_grp_DEND	Z0104	Categorical of season	base level: mseason in(1,4)			
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 (yes)	-0.224	0.00927	584.4139
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
myslope_DEND	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=125	0.0973	0.0106	83.7665
myslope_DEND	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=470	-0.5094	0.0154	1096.716
myslope_DEND	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=2200	-0.9095	0.0233	1526.287
myslope_DEND	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 194

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	WaldChiSq
vhpa2yb_DEND_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-85,102-85)	0.0155	0.00192	65.3363
vhpa2yb_DEND_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-102,109-102)	0.0631	0.00294	460.0102
vhpa2yb_DEND_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-109,120-109)	0.0667	0.00137	2361.993
vhpa2yb_DEND_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-120,180-120)	0.0365	0.000717	2582.692
mperiodnbr_DEND	L02	Categorical of period_number	period_number = 2	0.4886	0.0951	26.4138
mperiodnbr_DEND	L03	Categorical of period_number	period_number = 3	0.3113	0.0431	52.0632
mperiodnbr_DEND	Z00	Categorical of period_number	base level: else			
vperiodnbr_DEND_pw1		Variate piecewise of period_number	median(0,period_number-3,14-3)	0.0347	0.00208	279.4752
vperiodnbr_DEND_pw2		Variate piecewise of period_number	median(0,period_number-14,32-14)	0.0131	0.000967	184.4227
vperiodnbr_DEND_pw3		Variate piecewise of period_number	median(0,period_number-32,57-32)	0.00528	0.000991	28.4333
vperiodnbr_DEND_pw4		Variate piecewise of period_number	median(0,period_number-57,110-57)	0.023	0.0013	310.5232
mcredit_score_DEND	L00	Categorical of credit_score	credit_score = 0	0.1337	0.0218	37.599
mcredit_score_DEND	Z00	Categorical of credit_score	base level: else			
vcredit_DEND_pw1		Variate piecewise of credit_score	median(0,credit_score-642,780-642)	0.00326	0.000458	50.7145
mdurdefepi_DEND	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <= 1			
mdurdefepi_DEND	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.5292	0.0119	1982.786
mdurdefepi_DEND	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-0.7665	0.0147	2711.437
mdurdefepi_DEND	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-0.9376	0.0178	2761.8
mdurdefepi_DEND	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	-1.0234	0.0208	2414.956
mdurdefepi_DEND	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	-1.1447	0.0242	2231.499
mdurdefepi_DEND	L09	Categorical of dur_def_episode	dur_def_episode <= 9	-1.3288	0.0189	4926.293

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 195

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	WaldChiSq
		(duration of default episode)				
mdurdefepi_DEND	L20	Categorical of dur_def_episode (duration of default episode)	dur_def_episode <= 20	-1.4717	0.0174	7148.197
mdurdefepi_DEND	L34	Categorical of dur_def_episode (duration of default episode)	dur_def_episode <= 34	-1.4921	0.031	2314.729
mdurdefepi_DEND	L60	Categorical of dur_def_episode (duration of default episode)	dur_def_episode <= 60	-2.0274	0.084	582.6866
mdurdefepi_DEND	L61	Categorical of dur_def_episode (duration of default episode)	else	-2.0213	0.2955	46.7915
vdeltaUEinit_DEND_pw1		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-50,98-50)	0.0076	0.000326	542.1933
mpriordef_DEND	Z00	Categorical of prior_default_cnt	base level: prior_default_cnt = 0			
mpriordef_DEND	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.334	0.0114	850.8756
mpriordef_DEND	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.5683	0.0153	1371.071
mpriordef_DEND	L03	Categorical of prior_default_cnt	prior_default_cnt = 3	-0.8023	0.0198	1637.028
mpriordef_DEND	L04	Categorical of prior_default_cnt	prior_default_cnt = 4	-0.976	0.0244	1603.311
mpriordef_DEND	L05	Categorical of prior_default_cnt	prior_default_cnt = 5	-1.0828	0.0285	1440.825
mpriordef_DEND	L07	Categorical of prior_default_cnt	prior_default_cnt <= 7	-1.3019	0.0279	2183.654
mpriordef_DEND	L10	Categorical of prior_default_cnt	prior_default_cnt <= 10	-1.5663	0.0358	1914.039
mpriordef_DEND	L11	Categorical of prior_default_cnt	prior_default_cnt > 10	-1.7289	0.0559	957.4073
vdeltaUEpr3_DEND_pw1		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(delta_ue_sa_st_r-(-20),0,10-(-20))	0.00362	0.000396	83.5122
vdeltaUEpr3_DEND_pw2		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	max(delta_ue_sa_st_r-10,0)	0.00304	0.000115	695.8715
vUEblend_DEND_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (change in	median(0,ue_blended_r-200,700-200)	-0.00131	0.000051	668.3666

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 196

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	WaldChiSq
		unemployment rate)				
vUEblend_DEND_pw2		Variate piecewise of ue_bledned_r <sup>8</sup> (change in unemployment rate)	median(0,ue_bledned_r-700,900-700)	-0.00193	0.000107	324.6006
mltv_DEND	L00	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r=.	-0.571	0.0794	51.6863
mltv_DEND	Z01	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_DEND_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-20,55-20)	-0.0154	0.00244	39.5308
vltv_DEND_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-55,83-55)	-0.0115	0.000973	140.2214
vltv_DEND_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-83,96-83)	-0.02	0.0014	204.9156
vloanraw_DEND_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-98000,180000-98000)	1.40E-06	1.69E-07	67.9208
vloanraw_DEND_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-180000,500000-180000)	1.48E-06	1.04E-07	201.9164
mDeltaTY10_DEND	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	-0.1666	0.0178	87.8078
mDeltaTY10_DEND	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
mcalperiod_DEND	L200202	Categorical of Calendar Period	period < 200202	-0.5866	0.0185	1008.1
mcalperiod_DEND	Z	Categorical of Calendar Period	base level: else			

Default Transition Model Parameters – FRM15 D\_CLM

The model parameters for the FRM15 default to claim transition are shown below.

Table 53: Default to Claim Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-6.5020	0.2009	0.0000
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	0.3222	0.1372	0.0188

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 197

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mdpa	2	Categorical of dpa (down payment assistance)	dpa= "nonprof"	0.3077	0.0357	0.0000
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	-0.1287	0.0498	0.0097
mdpa	4	Categorical of dpa (down payment assistance)	base level: else			
mperiodnbr_DCLM	L04	Categorical of period number	period_number <= 4	-0.2892	0.1501	0.0540
mperiodnbr_DCLM	L08	Categorical of period number	period_number <= 8	0.1473	0.0542	0.0066
mperiodnbr_DCLM	Z09	Categorical of period number	base level: else			
vperiodnbr_DCLM_pw1		Variate piecewise of period_number	median(0,period_number-8,18-8)	0.0223	0.0063	0.0004
vperiodnbr_DCLM_pw2		Variate piecewise of period_number	median(0,period_number-18,39-18)	0.0071	0.0028	0.0109
vcredit_DCLM_pw3		Variate piecewise of credit_score	median(0,credit_score-645,800-645)	0.0064	0.0004	0.0000
mdurdefepi_DCLM	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	1.1203	0.0550	0.0000
mdurdefepi_DCLM	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	1.6169	0.0544	0.0000
mdurdefepi_DCLM	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	2.0312	0.0540	0.0000
mdurdefepi_DCLM	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	2.2209	0.0553	0.0000
mdurdefepi_DCLM	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	2.2562	0.0579	0.0000
mdurdefepi_DCLM	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode <= 17	2.3457	0.0498	0.0000
mdurdefepi_DCLM	L18	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 18	2.2687	0.0630	0.0000
mdurdefepi_DCLM	Z01	Categorical of dur_def_episode (duration of default episode)	base level: else			
vloanraw_DCLM_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,48000-0)	0.0000	0.0000	0.0000
vloanraw_DCLM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-48000,200000-48000)	0.0000	0.0000	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 198

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vloanraw_DCLM_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,425000-200000)	0.0000	0.0000	0.0013
vdeltaUEinit_DCLM_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-0,80-0)	-0.0107	0.0014	0.0000
vratiotmptei_DCLM_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,20-0)	0.0124	0.0017	0.0000
vratiotmptei_DCLM_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-20,36-20)	0.0073	0.0024	0.0027
vratiotmptei_DCLM_pw3		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-36,50-36)	-0.0163	0.0078	0.0372
mpriordef_DCLM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.1673	0.0264	0.0000
mpriordef_DCLM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.3136	0.0348	0.0000
mpriordef_DCLM	L03	Categorical of prior_default_cnt	prior_default_cnt >= 3	-0.4171	0.0398	0.0000
mpriordef_DCLM	Z00	Categorical of prior_default_cnt	base level: else			
vpriordef_DCLM_pw1		Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,15-3)	-0.1047	0.0173	0.0000
vsato_DCLM_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-(.4))	0.0940	0.0247	0.0001
mltv_DCLM	Miss	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i = .	0.4660	0.0970	0.0000
mltv_DCLM	Z00	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_DCLM_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-0,65-0)	0.0252	0.0014	0.0000
vltv_DCLM_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-65,76-65)	0.0270	0.0037	0.0000
vltv_DCLM_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-76,93-76)	0.0583	0.0043	0.0000
mhpa2yb_DCLM	L085	Categorical of hpa2y_blended_r <sup>6</sup>	0 < hpa2y_blended_r <= 85	0.3967	0.0801	0.0000
mhpa2yb_DCLM	Z000	Categorical of hpa2y_blended_r <sup>6</sup>	base level: else			
vhpa2yb_DCLM_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-85,104-85)	0.0344	0.0036	0.0000
vhpa2yb_DCLM_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-104,140-104)	-0.0077	0.0020	0.0002

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 199

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vDeltaTY1_DCLM_pw1		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-0,87-0)	-0.0061	0.0006	0.0000
vDeltaTY1_DCLM_pw2		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-87,150-87)	-0.0019	0.0007	0.0067
Mperiod_DCLM	L01	Categorical of period (calendar period)	period < 200603	-0.1411	0.0373	0.0002
Mperiod_DCLM	Z01	Categorical of period (calendar period)	base level: else			
mseason_grp_DCLM	L02	Categorical of season	season = "spring"	0.0654	0.0248	0.0084
mseason_grp_DCLM	L03	Categorical of season	season = "summer"	0.0937	0.0247	0.0001
mseason_grp_DCLM	Z0104	Categorical of season	base level: else			
vCCI_DCLM_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0253	0.0027	0.0000
vCCI_DCLM_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0136	0.0016	0.0000
vCCI_DCLM_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0051	0.0026	0.0444
vSBOI_DCLM_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0532	0.0100	0.0000

## Default Transition Model Parameters – FRM15 D\_CXM

The model parameters for the FRM15 default to modified cure transition are shown below.

Table 54: Default to Modified Cure Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-4.3009	0.1297	0.0000
mdpa_comb13_DCXM	2	Categorical of dpa (down payment assistance)	dpa = "nonprof"	0.1829	0.0314	0.0000
mdpa_comb13_DCXM	3	Categorical of dpa (down payment assistance)	dpa = "govt" or dpa = "relative"	0.0685	0.0391	0.0797
mdpa_comb13_DCXM	4	Categorical of dpa (down payment assistance)	base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 200

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mperiodnbr_DCXM	L03	Categorical of period number	period_number <= 3	-1.3321	0.1975	0.0000
mperiodnbr_DCXM	L04	Categorical of period number	period_number = 4	-1.0580	0.1370	0.0000
mperiodnbr_DCXM	L05	Categorical of period number	period_number = 5	-0.8546	0.1031	0.0000
mperiodnbr_DCXM	L06	Categorical of period number	period_number = 6	-0.5365	0.0796	0.0000
mperiodnbr_DCXM	L07	Categorical of period number	period_number = 7	-0.2129	0.0657	0.0012
mperiodnbr_DCXM	Z08	Categorical of period number	base level: else			
vperiodnbr_DCXM_pw1		Variate piecewise of period_number	median(0,period_number-7,14-7)	-0.0206	0.0064	0.0013
vperiodnbr_DCXM_pw3		Variate piecewise of period_number	median(0,period_number-31,48-31)	-0.0061	0.0028	0.0299
vperiodnbr_DCXM_pw4		Variate piecewise of period_number	median(0,period_number-48,60-48)	-0.0171	0.0066	0.0094
mcredit_score_DCXM	L00	Categorical of credit_score	credit_score = 0	-0.3456	0.0746	0.0000
mcredit_score_DCXM	Z00	Categorical of credit_score	base level: else			
vcredit_DCXM_pw1		Variate piecewise of credit_score	median(0,credit_score-450,545-450)	-0.0037	0.0008	0.0000
vcredit_DCXM_pw2		Variate piecewise of credit_score	median(0,credit_score-545,800-545)	-0.0015	0.0002	0.0000
mdurdefepi_DCXM	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	0.4220	0.0241	0.0000
mdurdefepi_DCXM	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	0.5937	0.0259	0.0000
mdurdefepi_DCXM	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	0.5790	0.0288	0.0000
mdurdefepi_DCXM	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	0.4769	0.0330	0.0000
mdurdefepi_DCXM	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	0.3995	0.0376	0.0000
mdurdefepi_DCXM	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	0.1903	0.0450	0.0000
mdurdefepi_DCXM	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 8	-0.0083	0.0399	0.8354
mdurdefepi_DCXM	Z01	Categorical of dur_def_episode (duration of default episode)	base level: else			



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 201

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vdurdefepi_DCXM_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-7,29-7)	-0.0540	0.0053	0.0000
vloanraw_DCXM_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,62000-0)	0.0000	0.0000	0.0000
vloanraw_DCXM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-62000,97000-62000)	0.0000	0.0000	0.0036
vloanraw_DCXM_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-97000,200000-97000)	0.0000	0.0000	0.0000
vloanraw_DCXM_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,425000-200000)	0.0000	0.0000	0.0336
vDeltaUEinit_DCXM_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-95,184-95)	0.0024	0.0004	0.0000
mRatioTmpTei_DCXM	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.5812	0.0594	0.0000
mRatioTmpTei_DCXM	Z00	Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_DCXM_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	0.0275	0.0028	0.0000
vratiotmptei_DCXM_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,50-24)	0.0069	0.0019	0.0003
mpriordef_DCXM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	0.2280	0.0229	0.0000
mpriordef_DCXM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	0.2822	0.0262	0.0000
mpriordef_DCXM	L07	Categorical of prior_default_cnt	prior_default_cnt >= 7	0.1962	0.0455	0.0000
mpriordef_DCXM	PW1	Categorical of prior_default_cnt	3 <= prior_default_cnt <= 6	0.2894	0.0251	0.0000
mpriordef_DCXM	Z00	Categorical of prior_default_cnt	base level: else			
vsato_DCXM_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-(-.56))	0.1492	0.0516	0.0038
vsato_DCXM_pw4		Variate piecewise of sato (spread at origination)	max(sato,-2,0)	-0.1463	0.0398	0.0002
vltv_DCXM_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-20,92-20)	0.0076	0.0008	0.0000
vltv_DCXM_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-92,100-92)	0.2387	0.0407	0.0000
mhpa2yb_DCXM	L084	Categorical of hpa2y_blended_r <sup>6</sup>	hpa2y_blended_R <=84	-0.2181	0.0482	0.0000
mhpa2yb_DCXM	Z00	Categorical of hpa2y_blended_r <sup>6</sup>	base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 202

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vhpa2yb_DCXM_pw2		Variate piecewise of hpa2y_bleded_r <sup>6</sup>	median(0,hpa2y_bleded_R-100,116-100)	0.0074	0.0021	0.0004
muest_DCXM	L42	Categorical of ue_sa_st_r <sup>10</sup> (seasonally adjusted state unemployment)	ue_sa_st_r<=420	-0.0182	0.0322	0.5710
muest_DCXM	L79	Categorical of ue_sa_st_r <sup>10</sup> (seasonally adjusted state unemployment)	ue_sa_st_r>790	-0.0925	0.0224	0.0000
muest_DCXM	Z00	Categorical of ue_sa_st_r <sup>10</sup> (seasonally adjusted state unemployment)	base level: else			
mseason_grp_DCXM	L02	Categorical of season	season = "spring"	0.1281	0.0194	0.0000
mseason_grp_DCXM	L03	Categorical of season	season = "summer"	0.0881	0.0195	0.0000
mseason_grp_DCXM	Z0104	Categorical of season	base level: else			
vCCI_DCXM_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	-0.0071	0.0011	0.0000
vCCI_DCXM_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0086	0.0010	0.0000
vCCI_DCXM_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0172	0.0021	0.0000

### Default Transition Model Parameters – FRM15 D\_CXS

The model parameters for the FRM15 default to self-cure transition are shown below.

Table 55: Default to Self-Cure Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				0.3080	0.0906	0.0007
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1	-0.0924	0.0062	0.0000
mjudicial	2	Categorical of judicial (judicial state)	base level: else			
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	-0.1941	0.0639	0.0024
mdpa	2	Categorical of dpa (down payment assistance)	dpa= "nonprof"	-0.3588	0.0195	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 203

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	-0.0213	0.0182	0.2422
mdpa	4	Categorical of dpa (down payment assistance)	base level: else			
mrfnc_ind	1	Categorical of rfnc_ind (refinanced loan indicator)	refinanced, non-streamlined	-0.0202	0.0108	0.0620
mrfnc_ind	2	Categorical of rfnc_ind (refinanced loan indicator)	streamlined refinanced	0.1136	0.0149	0.0000
mrfnc_ind	3	Categorical of rfnc_ind (refinanced loan indicator)	base level: else			
mperiodnbr_DCXS	L02	Categorical of period number	period_number = 2	1.3359	0.0659	0.0000
mperiodnbr_DCXS	L03	Categorical of period number	period_number = 3	0.6374	0.0352	0.0000
mperiodnbr_DCXS	L04	Categorical of period number	period_number = 4	0.3465	0.0287	0.0000
mperiodnbr_DCXS	L05	Categorical of period number	period_number = 5	0.2359	0.0253	0.0000
mperiodnbr_DCXS	L06	Categorical of period number	period_number = 6	0.1882	0.0231	0.0000
mperiodnbr_DCXS	L07	Categorical of period number	period_number = 7	0.1617	0.0218	0.0000
mperiodnbr_DCXS	L08	Categorical of period number	period_number = 8	0.1218	0.0211	0.0000
mperiodnbr_DCXS	Z09	Categorical of period number	base level: else			
vperiodnbr_DCXS_pw1		Variate piecewise of period_number	median(0,period_number-8,31-8)	0.0034	0.0007	0.0000
vperiodnbr_DCXS_pw2		Variate piecewise of period_number	median(0,period_number-31,52-31)	-0.0027	0.0008	0.0010
mcredit_score_DCXS	L00	Categorical of credit_score	credit_score = 0	0.3895	0.0216	0.0000
mcredit_score_DCXS	Z00	Categorical of credit_score	base level: else			
vcredit_DCXS_pw1		Variate piecewise of credit_score	median(0,credit_score-465,643-465)	0.0036	0.0001	0.0000
vcredit_DCXS_pw2		Variate piecewise of credit_score	median(0,credit_score-643,800-643)	0.0013	0.0001	0.0000
mdurdefepi_DCXS	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.6432	0.0079	0.0000
mdurdefepi_DCXS	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-0.9850	0.0101	0.0000
mdurdefepi_DCXS	L04	Categorical of dur_def_episode	dur_def_episode = 4	-1.3624	0.0132	0.0000

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 204

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
mdurdefepi_DCXS	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	-1.5180	0.0160	0.0000
mdurdefepi_DCXS	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	-1.7083	0.0194	0.0000
mdurdefepi_DCXS	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode <= 7	-2.0404	0.0181	0.0000
mdurdefepi_DCXS	Z01	Categorical of dur_def_episode (duration of default episode)	base level: else			
vdurdefepi_DCXS_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-6,20-6)	-0.0548	0.0025	0.0000
vloanraw_DCXS_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-0,37000-0)	0.0000	0.0000	0.0346
vloanraw_DCXS_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-37000,130000-37000)	0.0000	0.0000	0.0018
vloanraw_DCXS_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-130000,200000-130000)	0.0000	0.0000	0.0000
vdeltaUEinit_DCXS_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-0,78-0)	0.0014	0.0005	0.0019
vdeltaUEinit_DCXS_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-78,107-78)	-0.0034	0.0005	0.0000
vdeltaUEinit_DCXS_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-107,125-107)	-0.0037	0.0008	0.0000
vdeltaUEinit_DCXS_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEinit_R-125,200-125)	-0.0018	0.0002	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 205

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mRatioTmpTei_DCXS	L00	Categorical of ratio_tmp_teI (front-end ratio)	ratio_tmp_teI=0	-0.3188	0.0574	0.0000
mRatioTmpTei_DCXS	Z00	Categorical of ratio_tmp_teI (front-end ratio)	base level: else			
vratiotmpteI_DCXS_pw1		Variate piecewise of ratio_tmp_teI (front-end ratio)	median(0,ratio_tmp_teI-0,12-0)	-0.0156	0.0049	0.0016
vratiotmpteI_DCXS_pw2		Variate piecewise of ratio_tmp_teI (front-end ratio)	median(0,ratio_tmp_teI-12,28-12)	-0.0156	0.0008	0.0000
vratiotmpteI_DCXS_pw3		Variate piecewise of ratio_tmp_teI (front-end ratio)	median(0,ratio_tmp_teI-28,50-28)	-0.0065	0.0011	0.0000
mpriordef_DCXS	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.1602	0.0087	0.0000
mpriordef_DCXS	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.2013	0.0102	0.0000
mpriordef_DCXS	L07	Categorical of prior_default_cnt	prior_default_cnt >= 7	-0.1556	0.0315	0.0000
mpriordef_DCXS	PW1	Categorical of prior_default_cnt	3 <= prior_default_cnt <= 6	-0.1932	0.0148	0.0000
mpriordef_DCXS	Z00	Categorical of prior_default_cnt	base level: else			
vpriordef_DCXS_pw1		Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-2,7-2)	-0.0130	0.0058	0.0237
vsato_DCXS_pw2		Variate piecewise of sato (spread at origination)	median(sato-(-.4),0,.14-(-.4))	-0.0669	0.0158	0.0000
vsato_DCXS_pw3		Variate piecewise of sato (spread at origination)	max(sato-.14,0)	-0.0661	0.0157	0.0000
vlvtv_DCXS_pw1		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-0,19-0)	0.0147	0.0010	0.0000
vlvtv_DCXS_pw2		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-19,83-19)	-0.0075	0.0003	0.0000
vlvtv_DCXS_pw3		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-83,88-83)	-0.0285	0.0046	0.0000
vlvtv_DCXS_pw4		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-88,91-88)	-0.0353	0.0122	0.0038
vlvtv_DCXS_pw5		Variate piecewise of ltv_i_r <sup>2</sup> (loan-to-value)	median(0,ltv_i_R-91,100-91)	-0.0270	0.0118	0.0226
vUEblend_DCXS_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_R-0,525-0)	-0.0003	0.0001	0.0000
vUEblend_DCXS_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (change in	median(0,ue_blended_R-525,800-525)	-0.0002	0.0000	0.0000

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 206

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		unemployment rate)				
vUEblend_DCXS_pw3		Variate piecewise of ue_bledned_r <sup>8</sup> (change in unemployment rate)	median(0,ue_bledned_R-800,1500-800)	-0.0003	0.0000	0.0000
vDeltaTY1_DCXS_pw1		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-0,22-0)	-0.0071	0.0007	0.0000
vDeltaTY1_DCXS_pw2		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-22,80-22)	0.0015	0.0002	0.0000
mseason_grp_DCXS	L02	Categorical of season	season = "spring"	0.1265	0.0074	0.0000
mseason_grp_DCXS	L03	Categorical of season	season = "summer"	-0.0227	0.0076	0.0029
mseason_grp_DCXS	Z0104	Categorical of season	base level: else			
vCCI_DCXS_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	-0.0017	0.0007	0.0229
vCCI_DCXS_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0034	0.0006	0.0000
vCCI_DCXS_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	0.0190	0.0008	0.0000
vSBOI_DCXS_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0105	0.0029	0.0003
vSBOI_DCXS_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	-0.0974	0.0031	0.0000

Default Transition Model Parameters – FRM15 D\_END

The model parameters for the fixed rate 15-year mortgage default to end transition are shown below.

Table 56: Default to End Transition FRM15 Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-2.0396	0.1190	0.0000
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	-0.3812	0.2407	0.1133

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 207

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mdpa	2	Categorical of dpa (down payment assistance)	dpa = "nonprof"	-0.3520	0.0678	0.0000
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	0.0766	0.0537	0.1536
mdpa	4	Categorical of dpa (down payment assistance)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.0903	0.0287	0.0017
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
vhpa2yb_DEND_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_R-104,140-104)	0.0273	0.0014	0.0000
vperiodnbr_DEND_pw1		Variate piecewise of period_number	median(0,period_number-10,30-10)	0.0082	0.0021	0.0000
vperiodnbr_DEND_pw2		Variate piecewise of period_number	median(0,period_number-30,52-30)	0.0073	0.0023	0.0013
vperiodnbr_DEND_pw3		Variate piecewise of period_number	median(0,period_number-52,60-52)	0.1780	0.0065	0.0000
mcredit_score_DEND	L00	Categorical of credit_score	credit_score = 0	0.7737	0.0502	0.0000
mcredit_score_DEND	Z00	Categorical of credit_score	base level: else			
vcredit_DEND_pw1		Variate piecewise of credit_score	median(0,credit_score-470,800-470)	0.0044	0.0002	0.0000
vdurdefepi_DEND_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode,12)	-0.1813	0.0035	0.0000
vdurdefepi_DEND_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-12,54-12)	0.0095	0.0035	0.0059
vloanraw_DEND_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-55000,120000-55000)	0.0000	0.0000	0.0000
vloanraw_DEND_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-120000,200000-120000)	0.0000	0.0000	0.0000
vloanraw_DEND_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,425000-200000)	0.0000	0.0000	0.0570
vdeltaUEinit_DEND_pw1		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_R-0,175-0)	0.0020	0.0004	0.0000
mpriordef_DEND	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.3884	0.0237	0.0000
mpriordef_DEND	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.5694	0.0292	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 208

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_DEND	L03	Categorical of prior_default_cnt	prior_default_cnt >= 3	-0.8273	0.0296	0.0000
mpriordef_DEND	Z00	Categorical of prior_default_cnt	base level: else			
vpriordef_DEND_pw1		Variate piecewise of prior_default_cnt	median(0,prior_default_cnt-3,14-3)	-0.0662	0.0078	0.0000
vUEblend_DEND_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_R-0,800-0)	-0.0012	0.0001	0.0000
vUEblend_DEND_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_R-800,1500-800)	-0.0011	0.0001	0.0000
mltv_DEND	Miss	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i = .	-0.5091	0.0473	0.0000
mltv_DEND	Z00	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_DEND_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-0,63-0)	-0.0174	0.0010	0.0000
vltv_DEND_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_R-63,100-63)	-0.0168	0.0018	0.0000
vDeltaTY1_DEND_pw2		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-6,200-6)	0.0011	0.0002	0.0000
Mperiod_DEND	L01	Categorical of period (calendar period)	period < 200603	0.2798	0.0409	0.0000
Mperiod_DEND	Z01	Categorical of period (calendar period)	base level: else			
mseason_grp_DEND	L02	Categorical of season	season = "spring"	0.0682	0.0211	0.0012
mseason_grp_DEND	L03	Categorical of season	season = "summer"	0.1317	0.0210	0.0000
mseason_grp_DEND	Z0104	Categorical of season	base level: else			
vCCI_DEND_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0092	0.0023	0.0000
vSBOI_DEND_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0244	0.0050	0.0000
vSBOI_DEND_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	0.0254	0.0085	0.0028



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 209

## Default Transition Model Parameters – ARM D\_CLM

The model parameters for the ARM default to claim transition are shown below.

Table 57: Default to Claim Transition ARM Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-5.8513	0.2772	0.0000
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 , judicial state	-0.1659	0.0103	0.0000
mjudicial	2	Categorical of judicial (judicial state)	base level: else, non-judicial state			
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	0.3891	0.0444	0.0000
mdpa	2	Categorical of dpa (down payment assistance)	dpa= "nonprof"	0.4671	0.0158	0.0000
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	0.0272	0.0167	0.1024
mdpa	4	Categorical of dpa (down payment assistance)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.2049	0.0125	0.0000
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
myslope_DCLM	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=111	-0.2315	0.0205	0.0000
myslope_DCLM	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=875	-0.3236	0.0237	0.0000
myslope_DCLM	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=2000	0.0356	0.0263	0.1762
myslope_DCLM	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
mperiodnbr_DCLM	L02	Categorical of period_number	period_number <= 2	-0.5289	0.3617	0.1436
mperiodnbr_DCLM	L03	Categorical of period_number	period_number = 3	-0.8909	0.1366	0.0000
mperiodnbr_DCLM	L04	Categorical of period_number	period_number = 4	-0.7761	0.0826	0.0000
mperiodnbr_DCLM	Z05	Categorical of period_number	base level: else			
vperiodnbr_DCLM_pw2		Variate piecewise of period_number	median(0,period_number-10,18-10)	0.0412	0.0024	0.0000
vperiodnbr_DCLM_pw3		Variate piecewise of period_number	median(0,period_number-18,64-18)	-0.0166	0.0009	0.0000
vperiodnbr_DCLM_pw4		Variate piecewise of period_number	median(0,period_number-64,108-64)	0.0120	0.0033	0.0003

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 210

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mcredit_DCLM	L01	Categorical of credit_score	credit_score = 0	0.4015	0.0628	0.0000
mcredit_DCLM	Z00	Categorical of credit_score	base level: else			
vcredit_DCLM_pw1		Variate piecewise of credit_score	median(0,credit_score-300,720-300)	0.0009	0.0002	0.0000
vcredit_DCLM_pw2		Variate piecewise of credit_score	median(0,credit_score-720,800-720)	0.0067	0.0009	0.0000
vdurdefepi_DCLM_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	-0.0061	0.0015	0.0000
vdurdefepi_DCLM_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-30,40-30)	-0.0517	0.0076	0.0000
vdeltaUEinit_dclm_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-0,63-0)	0.0039	0.0019	0.0424
vdeltaUEinit_dclm_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-63,100-63)	-0.0028	0.0007	0.0001
vdeltaUEinit_dclm_pw3		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-100,116-100)	0.0069	0.0012	0.0000
vdeltaUEinit_dclm_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-116,218-116)	0.0008	0.0003	0.0025
vdeltaUEinit_dclm_pw5		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-218,330-218)	0.0012	0.0004	0.0046
mRatioTmpTei_DCLM	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.1139	0.0165	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 211

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mRatioTmpTei_DCLM	Z00	Categorical of ratio_tmp_te_i (front-end ratio)	base level: else			
vratiotmpte_i_DCLM_pw2		Variate piecewise of ratio_tmp_te_i (front-end ratio)	median(0,ratio_tmp_te_i-24,36-24)	0.0059	0.0014	0.0000
vratiotmpte_i_DCLM_pw3		Variate piecewise of ratio_tmp_te_i (front-end ratio)	median(0,ratio_tmp_te_i-36,50-36)	-0.0131	0.0030	0.0000
mpriordef_DCLM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.3613	0.0128	0.0000
mpriordef_DCLM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.5620	0.0171	0.0000
mpriordef_DCLM	L03	Categorical of prior_default_cnt	3 <= prior_default_cnt <= 8	-0.8538	0.0177	0.0000
mpriordef_DCLM	L04	Categorical of prior_default_cnt	9 <= prior_default_cnt <= 13	-1.5255	0.0643	0.0000
mpriordef_DCLM	L05	Categorical of prior_default_cnt	prior_default_cnt >= 14	-2.5301	0.2912	0.0000
mpriordef_DCLM	Z00	Categorical of prior_default_cnt	base level: 0			
vloanraw_DCLM_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-30000,109000-30000)	0.0000	0.0000	0.0000
vloanraw_DCLM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-109000,143000-109000)	0.0000	0.0000	0.0000
vloanraw_DCLM_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-143000,200000-143000)	0.0000	0.0000	0.0000
vloanraw_DCLM_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,425000-200000)	0.0000	0.0000	0.0000
mltv_DCLM	L01	Categorical of ltv_i_r^2 (loan-to-value)	ltv_i_r = .	0.2048	0.1134	0.0709
mltv_DCLM	Z00	Categorical of ltv_i_r^2 (loan-to-value)	base level: else			
vltv_DCLM_pw1		Variate piecewise of ltv_i_r^2 (loan-to-value)	median(0,ltv_i_r-0,70-0)	0.0211	0.0031	0.0000
vltv_DCLM_pw2		Variate piecewise of ltv_i_r^2 (loan-to-value)	median(0,ltv_i_r-70,81-70)	0.0080	0.0025	0.0013
vltv_DCLM_pw3		Variate piecewise of ltv_i_r^2 (loan-to-value)	median(0,ltv_i_r-81,94-81)	0.0220	0.0018	0.0000
mhpa2yb_DCLM	L085	Categorical of hpa2y_blended_r^6	hpa2y_blended_r <= 85	0.2113	0.0316	0.0000
mhpa2yb_DCLM	Z000	Categorical of hpa2y_blended_r^6	base level: else			
vhpa2yb_DCLM_pw1		Variate piecewise of hpa2y_blended_r^6	median(0,hpa2y_blended_r-85,98-85)	0.0063	0.0027	0.0181
vhpa2yb_DCLM_pw2		Variate piecewise of hpa2y_blended_r^6	median(0,hpa2y_blended_r-98,108-98)	0.0102	0.0024	0.0000
vhpa2yb_DCLM_pw3		Variate piecewise of hpa2y_blended_r^6	median(0,hpa2y_blended_r-108,130-108)	-0.0175	0.0011	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 212

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vhpa2yb_DCLM_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-130,180-130)	-0.0573	0.0041	0.0000
vUEblend_DCLM_pw1		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(200,ue_blended_r,450)	0.0012	0.0003	0.0000
vUEblend_DCLM_pw2		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_r-450,850-450)	-0.0005	0.0001	0.0000
vUEblend_DCLM_pw3		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blended_r-850,1500-850)	0.0003	0.0001	0.0000
vdeltaUEpr3_DCLM_pw1		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-(-200),0,(-20)-(-200))	-0.0016	0.0003	0.0000
vdeltaUEpr3_DCLM_pw3		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-10,0,200-10)	-0.0011	0.0002	0.0000
vprior3uest_DCLM_pw1		Variate piecewise of prior3_ue_sa_st (change in prior-3 seasonally adjusted unemployment rate)	median(2.4,prior3_ue_sa_st,5)	0.1713	0.0197	0.0000
vprior3uest_DCLM_pw2		Variate piecewise of prior3_ue_sa_st (change in prior-3 seasonally adjusted unemployment rate)	median(0,prior3_ue_sa_st-5,12.3-5)	0.0548	0.0084	0.0000
mDeltaTY10_DCLM	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	0.2622	0.0178	0.0000
mDeltaTY10_DCLM	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 213

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mseason_grp_DCLM	L02	Categorical of season	season = "spring"	0.0460	0.0119	0.0001
mseason_grp_DCLM	L03	Categorical of season	season = "summer"	0.0463	0.0120	0.0001
mseason_grp_DCLM	Z0104	Categorical of season	base level: else			
vCCI_DCLM_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0102	0.0014	0.0000
vCCI_DCLM_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0028	0.0008	0.0005
vCCI_DCLM_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	0.0281	0.0022	0.0000
vSBOI_DCLM_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0350	0.0053	0.0000
vSBOI_DCLM_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	-0.0133	0.0053	0.0113
vSBOI_DCLM_pw3		Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	-0.0345	0.0050	0.0000

**Default Transition Model Parameters – ARM D\_CXM**

The model parameters for the ARM default to modified cure transition are shown below.

*Table 58: Default to Modified Cure Transition ARM Model Parameters*

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-4.1901	0.2129	0.0000
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	0.1402	0.0535	0.0088
mdpa	2	Categorical of dpa (down payment assistance)	dpa= "nonprof"	0.1650	0.0181	0.0000
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	0.0564	0.0190	0.0029
mdpa	4	Categorical of dpa (down payment assistance)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.0419	0.0172	0.0149
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
mrfnc_ind	2	Categorical of rfnrc_ind	rfnc_ind <> "N"	0.0570	0.0242	0.0185

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 214

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(refinanced loan indicator)				
mrfnc_ind	3	Categorical of rfn_ind (refinanced loan indicator)	base level: else			
myslope_DCXM	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=111	0.0041	0.0298	0.8916
myslope_DCXM	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=875	0.2425	0.0261	0.0000
myslope_DCXM	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=2000	0.4355	0.0285	0.0000
myslope_DCXM	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
mperiodnbr_DCXM	L02	Categorical of period_number	period_number <= 2	-1.8680	1.0041	0.0628
mperiodnbr_DCXM	L03	Categorical of period_number	period_number = 3	-0.6562	0.2261	0.0037
mperiodnbr_DCXM	L04	Categorical of period_number	period_number = 4	-0.5630	0.1504	0.0002
mperiodnbr_DCXM	Z05	Categorical of period_number	base level: else			
vperiodnbr_DCXM_pw1		Variate piecewise of period_number	median(0,period_number-5,9-5)	0.1661	0.0148	0.0000
vperiodnbr_DCXM_pw2		Variate piecewise of period_number	median(0,period_number-9,18-9)	-0.0123	0.0031	0.0000
vperiodnbr_DCXM_pw3		Variate piecewise of period_number	median(0,period_number-18,36-18)	-0.0147	0.0018	0.0000
vperiodnbr_DCXM_pw4		Variate piecewise of period_number	median(0,period_number-36,50-36)	0.0160	0.0022	0.0000
vperiodnbr_DCXM_pw5		Variate piecewise of period_number	median(0,period_number-50,108-50)	-0.0068	0.0016	0.0000
mcredit_DCXM	L01	Categorical of credit_score	credit_score = 0	-0.2209	0.0311	0.0000
mcredit_DCXM	L02	Categorical of credit_score	credit_score<525	-0.0524	0.0529	0.3217
mcredit_DCXM	Z00	Categorical of credit_score	base level: else			
vcredit_DCXM_pw1		Variate piecewise of credit_score	median(0,credit_score-525,645-525)	-0.0017	0.0003	0.0000
vcredit_DCXM_pw2		Variate piecewise of credit_score	median(0,credit_score-645,800-645)	-0.0024	0.0004	0.0000
vdurdefepi_DCXM_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-5,7-5)	-0.0883	0.0086	0.0000
vdurdefepi_DCXM_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-7,40-7)	-0.0577	0.0023	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 215

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vdeltaUEinit_DCXM_pw1		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-0,63-0)	0.0046	0.0018	0.0096
vdeltaUEinit_DCXM_pw2		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-63,100-63)	-0.0052	0.0007	0.0000
vdeltaUEinit_DCXM_pw4		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-116,218-116)	0.0016	0.0003	0.0000
vdeltaUEinit_DCXM_pw5		Variate piecewise of DeltaUEinit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,deltaUEinit_r-218,330-218)	0.0011	0.0004	0.0026
mRatioTmpTei_DCXM	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.4322	0.0538	0.0000
mRatioTmpTei_DCXM	Z00	Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_DCXM_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	0.0165	0.0024	0.0000
vratiotmptei_DCXM_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	0.0051	0.0017	0.0019
mpriordef_DCXM	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	0.3361	0.0173	0.0000
mpriordef_DCXM	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	0.4558	0.0195	0.0000
mpriordef_DCXM	L03	Categorical of prior_default_cnt	3 <= prior_default_cnt <= 8	0.6137	0.0193	0.0000
mpriordef_DCXM	L04	Categorical of prior_default_cnt	9 <= prior_default_cnt <= 13	0.5149	0.0401	0.0000
mpriordef_DCXM	L05	Categorical of prior_default_cnt	prior_default_cnt >= 14	0.3774	0.1075	0.0004
mpriordef_DCXM	Z00	Categorical of prior_default_cnt	base level: 0			
vsato_DCXM_pw1		Variate piecewise of sato (spread at origination)	min(0,sato-(-.1))	-0.0294	0.0098	0.0027
vloanraw_DCXM_pw1		Variate piecewise of loansize_raw	median(30000,loansize_raw,109000)	0.0000	0.0000	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 216

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vloanraw_DCXM_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-109000,143000-109000)	0.0000	0.0000	0.0000
vloanraw_DCXM_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,425000-200000)	0.0000	0.0000	0.0328
vlvtv_DCXM_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,68-0)	0.0059	0.0018	0.0011
vlvtv_DCXM_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-68,81-68)	0.0094	0.0023	0.0000
vlvtv_DCXM_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-81,91-81)	-0.0066	0.0026	0.0112
vhpa2yb_DCXM_pw2		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-98,108-98)	-0.0312	0.0024	0.0000
vhpa2yb_DCXM_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-117,180-117)	-0.0156	0.0022	0.0000
vdeltaUEpr3_DCXM_pw1		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-(-200),0,(-20)-(-200))	-0.0009	0.0003	0.0049
vdeltaUEpr3_DCXM_pw2		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-(-20),0,10-(-20))	0.0029	0.0007	0.0000
vdeltaUEpr3_DCXM_pw3		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-10,0,200-10)	-0.0017	0.0002	0.0000
vprior3uest_DCXM_pw1		Variate piecewise of prior3_ue_sa_st (change in prior-3 seasonally adjusted unemployment rate)	median(2.4,prior3_ue_sa_st,5)	-0.0356	0.0170	0.0359
vprior3uest_DCXM_pw2		Variate piecewise of prior3_ue_sa_st (change in prior-3 seasonally adjusted unemployment rate)	median(0,prior3_ue_sa_st-5,12.3-5)	-0.0531	0.0057	0.0000
mDeltaTY10_DCXM	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from	DeltaTy10Init_r < 53	-0.2716	0.0174	0.0000



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 217

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		policy inception to current)				
mDeltaTY10_DCXM	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
mseason_grp_DCXM	L02	Categorical of season	season = "spring"	0.1351	0.0138	0.0000
mseason_grp_DCXM	L03	Categorical of season	season = "summer"	-0.0203	0.0141	0.1513
mseason_grp_DCXM	Z0104	Categorical of season	base level: else			
vCCI_DCXM_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	-0.0145	0.0015	0.0000
vCCI_DCXM_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0496	0.0013	0.0000
vCCI_DCXM_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	0.0836	0.0030	0.0000
vSBOI_DCXM_pw1		Variate piecewise of small business optimism index	median(0,SBOI_r-83,95-83)	-0.0351	0.0058	0.0000
vSBOI_DCXM_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	-0.4316	0.0083	0.0000
vSBOI_DCXM_pw3		Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	-0.1329	0.0110	0.0000

## Default Transition Model Parameters – ARM D\_CXS

The model parameters for the ARM default to self-cure transition are shown below.

Table 59: Default to Self-Cure Transition ARM Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				0.6976	0.0627	0.0000
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 , judicial state	-0.1410	0.0055	0.0000
mjudicial	2	Categorical of judicial (judicial state)	base level: else, non-judicial state			
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	-0.2256	0.0297	0.0000
mdpa	2	Categorical of dpa (down payment assistance)	dpa = "nonprof"	-0.2412	0.0096	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 218

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	-0.0018	0.0086	0.8349
mdpa	4	Categorical of dpa (down payment assistance)	base level: else			
mrfnc_ind	2	Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind <> "N"	-0.1312	0.0094	0.0000
mrfnc_ind	3	Categorical of rfnc_ind (refinanced loan indicator)	base level: else			
myslope_DCXS	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=111	-0.2148	0.0110	0.0000
myslope_DCXS	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=875	0.1113	0.0119	0.0000
myslope_DCXS	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=2000	0.0660	0.0132	0.0000
myslope_DCXS	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
mperiodnbr_DCXS	L02	Categorical of period_number	period_number <= 2	1.6388	0.0844	0.0000
mperiodnbr_DCXS	L03	Categorical of period_number	period_number = 3	0.6355	0.0379	0.0000
mperiodnbr_DCXS	L04	Categorical of period_number	period_number = 4	0.1908	0.0307	0.0000
mperiodnbr_DCXS	Z05	Categorical of period_number	base level: else			
vperiodnbr_DCXS_pw1		Variate piecewise of period_number	median(0,period_number-5,9-5)	-0.0578	0.0053	0.0000
vperiodnbr_DCXS_pw2		Variate piecewise of period_number	median(0,period_number-9,18-9)	0.0080	0.0017	0.0000
vperiodnbr_DCXS_pw3		Variate piecewise of period_number	median(0,period_number-18,36-18)	0.0143	0.0008	0.0000
vperiodnbr_DCXS_pw4		Variate piecewise of period_number	median(0,period_number-36,50-36)	0.0040	0.0010	0.0000
mcredit_DCXS	L01	Categorical of credit_score	credit_score = 0	0.0945	0.0185	0.0000
mcredit_DCXS	L02	Categorical of credit_score	credit_score<525	-0.0356	0.0355	0.3149
mcredit_DCXS	Z00	Categorical of credit_score	base level: else			
vcredit_DCXS_pw1		Variate piecewise of credit_score	median(0,credit_score-525,645-525)	0.0026	0.0002	0.0000
vcredit_DCXS_pw2		Variate piecewise of credit_score	median(0,credit_score-645,800-645)	0.0009	0.0002	0.0000
mdurdefepi_DCXS	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.6019	0.0069	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 219

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mdurdefepi_DCXS	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-0.9461	0.0086	0.0000
mdurdefepi_DCXS	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-1.2845	0.0108	0.0000
mdurdefepi_DCXS	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 4	-1.4205	0.0119	0.0000
mdurdefepi_DCXS	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <=1			
vdurdefepi_DCXS_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-5,7-5)	-0.3167	0.0078	0.0000
vdurdefepi_DCXS_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-7,40-7)	-0.0264	0.0010	0.0000
vdeltaUEinit_DCXS_pw3		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-100,116-100)	-0.0033	0.0005	0.0000
vdeltaUEinit_DCXS_pw4		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-116,218-116)	-0.0007	0.0001	0.0000
mRatioTmpTei_DCXS	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	-0.2495	0.0208	0.0000
mRatioTmpTei_DCXS	Z00	Categorical of ratio_tmp_tei (front-end ratio)	base level: else			
vratiotmptei_DCXS_pw1		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-0,24-0)	-0.0122	0.0009	0.0000
vratiotmptei_DCXS_pw2		Variate piecewise of ratio_tmp_tei (front-end ratio)	median(0,ratio_tmp_tei-24,36-24)	-0.0074	0.0008	0.0000
mpriordef_DCXS	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.0647	0.0077	0.0000
mpriordef_DCXS	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.1240	0.0091	0.0000
mpriordef_DCXS	L03	Categorical of prior_default_cnt	3 <= prior_default_cnt <= 8	-0.1902	0.0085	0.0000

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 220

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
mpriordef_DCXS	L04	Categorical of prior_default_cnt	9 <= prior_default_cnt <= 13	-0.1972	0.0151	0.0000
mpriordef_DCXS	L05	Categorical of prior_default_cnt	prior_default_cnt >= 14	-0.1524	0.0313	0.0000
mpriordef_DCXS	Z00	Categorical of prior_default_cnt	base level: 0			
vsato_DCXS_pw2		Variate piecewise of sato (spread at origination)	median(sato-(-.1),0,.7-(-.1))	-0.0635	0.0347	0.0671
vloanraw_DCXS_pw1		Variate piecewise of loansize_raw	median(30000,loansize_raw,143000)	0.0000	0.0000	0.0000
vloanraw_DCXS_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-143000,200000-143000)	0.0000	0.0000	0.0000
vloanraw_DCXS_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,425000-200000)	0.0000	0.0000	0.0049
vdeltaUEpr3_DCXS_pw3		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-10,0,200-10)	-0.0011	0.0002	0.0000
vdeltaUEBlended_DCXS_pw3		Variate piecewise of ue_blended_r <sup>8</sup> (change in unemployment rate)	delta_ue_blended - .1	-0.0385	0.0127	0.0024
mltv_DCXS	L01	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r = .	0.2799	0.0336	0.0000
mltv_DCXS	Z00	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_DCXS_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,68-0)	-0.0037	0.0006	0.0000
vltv_DCXS_pw2		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-68,81-68)	-0.0106	0.0010	0.0000
vltv_DCXS_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-81,91-81)	-0.0090	0.0013	0.0000
vltv_DCXS_pw4		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-91,100-91)	-0.0409	0.0035	0.0000
vhpa2yb_DCXS_pw1		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-85,98-85)	0.0075	0.0010	0.0000
vhpa2yb_DCXS_pw3		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-108,117-108)	0.0103	0.0011	0.0000
vhpa2yb_DCXS_pw4		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-117,130-117)	0.0072	0.0012	0.0000
vhpa2yb_DCXS_pw5		Variate piecewise of hpa2y_blended_r <sup>6</sup>	median(0,hpa2y_blended_r-130,180-130)	0.0108	0.0012	0.0000
vprior3uest_DCXS_pw1		Variate piecewise of	median(2.5,prior3_ue_sa_st,5)	-0.0291	0.0070	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 221

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		prior3_ue_sa_st (change in prior-3 seasonally adjusted unemployment rate)				
vprior3uest_DCXS_pw2		Variate piecewise of prior3_ue_sa_st (change in prior-3 seasonally adjusted unemployment rate)	median(0,prior3_ue_sa_st-5,12.1-5)	-0.0312	0.0027	0.0000
mDeltaTY10_DCXS	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	-0.0139	0.0085	0.0997
mDeltaTY10_DCXS	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
vDeltaTY1_DCXS_pw2		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-22,80-22)	0.0010	0.0002	0.0000
vDeltaTY1_DCXS_pw3		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-80,150-80)	0.0010	0.0002	0.0000
mseason_grp_DCXS	L02	Categorical of season	season = "spring"	0.1581	0.0061	0.0000
mseason_grp_DCXS	L03	Categorical of season	season = "summer"	-0.0033	0.0065	0.6100
mseason_grp_DCXS	Z0104	Categorical of season	base level: else			
vCCI_DCXS_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0125	0.0005	0.0000
vCCI_DCXS_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	0.0206	0.0010	0.0000
vSBOI_DCXS_pw1		Variate piecewise of small business optimism index	median(0,CCI_r-110,134-110)	-0.0281	0.0019	0.0000
vSBOI_DCXS_pw2		Variate piecewise of small business optimism index	median(0,SBOI_r-95,100-95)	-0.0764	0.0028	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 222

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vSBOI_DCXS_pw3		Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	-0.0345	0.0029	0.0000

### Default Transition Model Parameters – ARM D\_END

The model parameters for the ARM default to end transition are shown below.

Table 60: Default to End Transition ARM Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				-3.3900	0.2295	0.0000
mjudicial	1	Categorical of judicial (judicial state)	judicial = 1 , judicial state	-0.1731	0.0141	0.0000
mjudicial	2	Categorical of judicial (judicial state)	base level: else, non-judicial state			
mdpa	1	Categorical of dpa (down payment assistance)	dpa = "govt"	-0.4795	0.0978	0.0000
mdpa	2	Categorical of dpa (down payment assistance)	dpa= "nonprof"	-0.4808	0.0319	0.0000
mdpa	3	Categorical of dpa (down payment assistance)	dpa = "relative"	0.0594	0.0209	0.0046
mdpa	4	Categorical of dpa (down payment assistance)	base level: else			
mfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	-0.0304	0.0163	0.0627
mfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else			
myslope_DEND	L01	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r<=111	0.2621	0.0241	0.0000
myslope_DEND	L02	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=875	-0.7216	0.0381	0.0000
myslope_DEND	L03	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	ycslope_r>=2000	-0.7899	0.0454	0.0000
myslope_DEND	Z00	Categorical of ycslope_r <sup>9</sup> (yield curve slope)	base level: else			
vperiodnbr_DEND_pw2		Variate piecewise of period_number	median(0,period_number-9,18-9)	0.0192	0.0039	0.0000
vperiodnbr_DEND_pw3		Variate piecewise of period_number	median(0,period_number-18,36-18)	0.0166	0.0019	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 223

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vperiodnbr_DEND_pw4		Variate piecewise of period_number	median(0,period_number-36,50-36)	0.0073	0.0024	0.0023
vperiodnbr_DEND_pw5		Variate piecewise of period_number	median(0,period_number-50,70-50)	0.0196	0.0028	0.0000
mcredit_DEND	L01	Categorical of credit_score	credit_score = 0	0.3355	0.0678	0.0000
mcredit_DEND	L02	Categorical of credit_score	credit_score<525	0.0678	0.1288	0.5989
mcredit_DEND	Z00	Categorical of credit_score	base level: else			
vcredit_DEND_pw1		Variate piecewise of credit_score	median(0,credit_score-525,645-525)	0.0027	0.0007	0.0000
vcredit_DEND_pw2		Variate piecewise of credit_score	median(0,credit_score-645,800-645)	0.0038	0.0005	0.0000
mdurdefepi_DEND	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.3630	0.0199	0.0000
mdurdefepi_DEND	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-0.5837	0.0239	0.0000
mdurdefepi_DEND	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-0.6907	0.0275	0.0000
mdurdefepi_DEND	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 4	-0.7964	0.0293	0.0000
mdurdefepi_DEND	Z01	Categorical of dur_def_episode (duration of default episode)	base level: dur_def_episode <=1			
vdurdefepi_DEND_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-5,7-5)	-0.1005	0.0175	0.0000
vdurdefepi_DEND_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-7,24-7)	-0.0161	0.0025	0.0000
vdurdefepi_DEND_pw3		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-24,40-24)	-0.0229	0.0050	0.0000
vdeltaUEinit_DEND_pw1		Variate piecewise of DeltaUEInit_r <sup>4</sup> (change in unemployment rate from policy inception to current)	median(0,DeltaUEInit_r-0,63-0)	0.0039	0.0020	0.0506
vdeltaUEinit_DEND_pw2		Variate piecewise of DeltaUEInit_r <sup>4</sup>	median(0,DeltaUEInit_r-63,100-63)	0.0054	0.0007	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 224

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(change in unemployment rate from policy inception to current)				
mRatioTmpTei_DEND	L00	Categorical of ratio_tmp_te1 (front-end ratio)	ratio_tmp_te1=0	-0.3578	0.0504	0.0000
mRatioTmpTei_DEND	Z00	Categorical of ratio_tmp_te1 (front-end ratio)	base level: else			
vratiotmp1ei_DEND_pw1		Variate piecewise of ratio_tmp_te1 (front-end ratio)	median(0,ratio_tmp_te1-0,24-0)	-0.0092	0.0021	0.0000
mpriordef_DEND	L01	Categorical of prior_default_cnt	prior_default_cnt = 1	-0.1777	0.0171	0.0000
mpriordef_DEND	L02	Categorical of prior_default_cnt	prior_default_cnt = 2	-0.3106	0.0223	0.0000
mpriordef_DEND	L03	Categorical of prior_default_cnt	3 <= prior_default_cnt <= 8	-0.6791	0.0237	0.0000
mpriordef_DEND	L04	Categorical of prior_default_cnt	9 <= prior_default_cnt <= 13	-1.3108	0.0581	0.0000
mpriordef_DEND	L05	Categorical of prior_default_cnt	prior_default_cnt >= 14	-1.3221	0.1227	0.0000
mpriordef_DEND	Z00	Categorical of prior_default_cnt	base level: 0			
vloanraw_DEND_pw1		Variate piecewise of loansize_raw	median(30000,loansize_raw,143000)	0.0000	0.0000	0.0000
vloanraw_DEND_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-200000,425000-200000)	0.0000	0.0000	0.0000
mltv_DEND	L01	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	ltv_i_r = .	0.2698	0.0866	0.0018
mltv_DEND	Z00	Categorical of ltv_i_r <sup>7</sup> (loan-to-value)	base level: else			
vltv_DEND_pw1		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-0,68-0)	-0.0182	0.0019	0.0000
vltv_DEND_pw3		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-81,91-81)	-0.0160	0.0028	0.0000
vltv_DEND_pw4		Variate piecewise of ltv_i_r <sup>7</sup> (loan-to-value)	median(0,ltv_i_r-91,100-91)	-0.1033	0.0088	0.0000
vhpa2yb_DEND_pw1		Variate piecewise of hpa2y_b1ended_r <sup>6</sup>	median(0,hpa2y_b1ended_r-85,98-85)	0.0252	0.0044	0.0000
vhpa2yb_DEND_pw2		Variate piecewise of hpa2y_b1ended_r <sup>6</sup>	median(0,hpa2y_b1ended_r-98,108-98)	0.0299	0.0039	0.0000
vhpa2yb_DEND_pw3		Variate piecewise of hpa2y_b1ended_r <sup>6</sup>	median(0,hpa2y_b1ended_r-108,117-108)	0.0701	0.0025	0.0000
vhpa2yb_DEND_pw4		Variate piecewise of hpa2y_b1ended_r <sup>6</sup>	median(0,hpa2y_b1ended_r-117,180-117)	0.0307	0.0009	0.0000



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 225

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vUEblend_DEND_pw1		Variate piecewise of ue_blen ded_r <sup>8</sup> (change in unemployment rate)	median(200,ue_blen ded_r,450)	-0.0018	0.0002	0.0000
vUEblend_DEND_pw3		Variate piecewise of ue_blen ded_r <sup>8</sup> (change in unemployment rate)	median(0,ue_blen ded_r-850,1500-850)	-0.0007	0.0002	0.0000
vdeltaUEpr3_DEND_pw2		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-(-20),0,10-(-20))	0.0042	0.0006	0.0000
vdeltaUEpr3_DEND_pw3		Variate piecewise of deltauepr3_r <sup>5</sup> (change in unemployment from 3 quarters prior)	median(deltauepr3_r-10,0,200-10)	-0.0008	0.0003	0.0024
mDeltaTY10_DEND	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	-0.2515	0.0323	0.0000
mDeltaTY10_DEND	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else			
vDeltaTY1_DEND_pw1		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-0,22-0)	0.0244	0.0026	0.0000
vDeltaTY1_DEND_pw2		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-22,80-22)	0.0028	0.0005	0.0000
vDeltaTY1_DEND_pw3		Variate piecewise of DeltaTy1Init_r <sup>3</sup> (change in 1-year Treasury rate from policy inception to current)	median(0,DeltaTy1Init_R-80,150-80)	0.0030	0.0004	0.0000
mseason_grp_DEND	L02	Categorical of season	season = "spring"	0.1355	0.0159	0.0000
mseason_grp_DEND	L03	Categorical of season	season = "summer"	0.1260	0.0161	0.0000
mseason_grp_DEND	Z0104	Categorical of season	base level: else			

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 226

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
vCCI_DEND_pw1		Variate piecewise of consumer confidence index	median(0,CCI_r-30,75-30)	0.0058	0.0017	0.0007
vCCI_DEND_pw2		Variate piecewise of consumer confidence index	median(0,CCI_r-75,110-75)	-0.0066	0.0011	0.0000
vCCI_DEND_pw3		Variate piecewise of consumer confidence index	median(0,CCI_r-110,134-110)	-0.0360	0.0024	0.0000
vSBOI_DEND_pw3		Variate piecewise of small business optimism index	median(0,SBOI_r-100,108-100)	0.0587	0.0051	0.0000

### Section 3: Model Validation

Model validation was accomplished in part by applying the model structure developed using the training set to the validation dataset. The application of the model to the validation data produces the probability of each type of transition. The actual target variable is then compared to the predicted target variable to ensure the model fits the transition process without over-fitting the actual data.

Specifically, for the final condition transition state, we calculate the actual transition rate and the predicted transition rate. The actual transition is 1 for the final transition state of the record and 0 for all other transition states. The probability of each final transition state for each record in the validation dataset is derived from the model parameters. The sum of all predicted final condition transition states' probabilities is 1 for each record.

Simple quantile plots are then created for each final condition transition state. All records are sorted, or ranked, in increasing order by the predicted probability. Ten equal sized decile groups are created with 10% of the records in each group. The sum of the actual probability and the sum of the predicted probability for each ending condition within each decile is calculated. The total number of actual and predicted transitions are compared for consistency. The objective of a model is to have a significant spread in predicted values while maintaining a close relationship between the resulting actual and predicted values.

The validation charts shown below show that the spread in prediction is consistent between the actual and predicted experience, and also the actual vs. predicted ratio for each decile are consistent as well.

#### Current FRM30NSR Transition Models

The validation charts by ending condition for the FRM30NSR models are shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 227

Figure 16: Current FRM30NSR Transition Model Validation - Ending Condition Streamlined Refinance

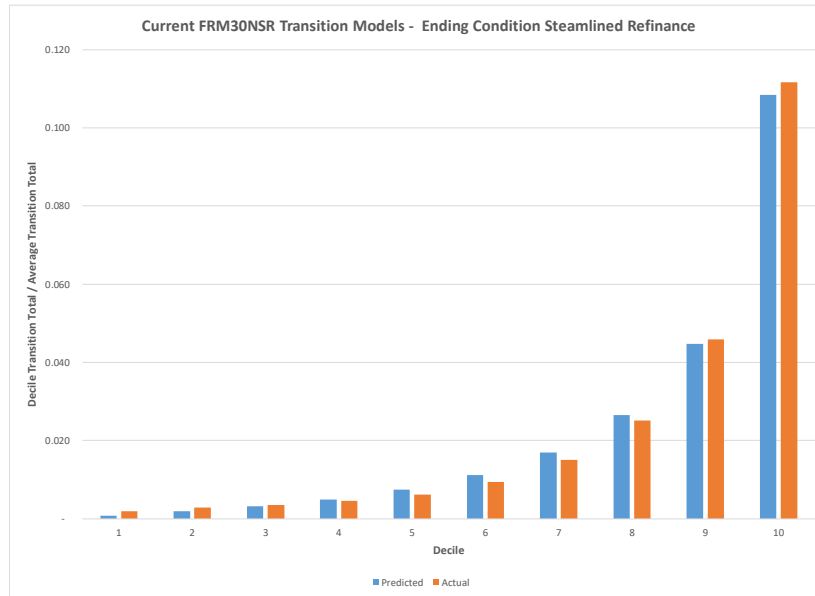
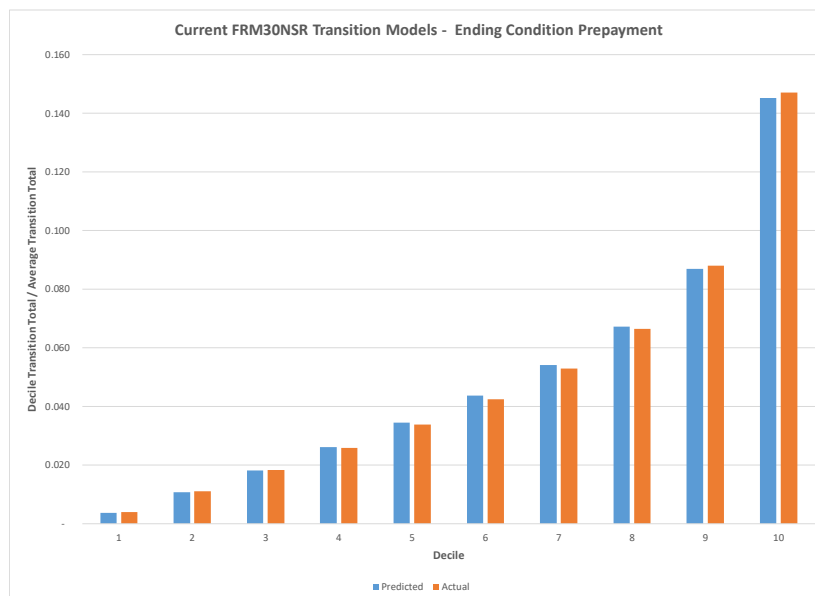


Figure 17: Current FRM30NSR Transition Model Validation - Ending Condition Prepayment



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 228

Figure 18: Current FRM30NSR Transition Model Validation - Ending Condition Self-Cure

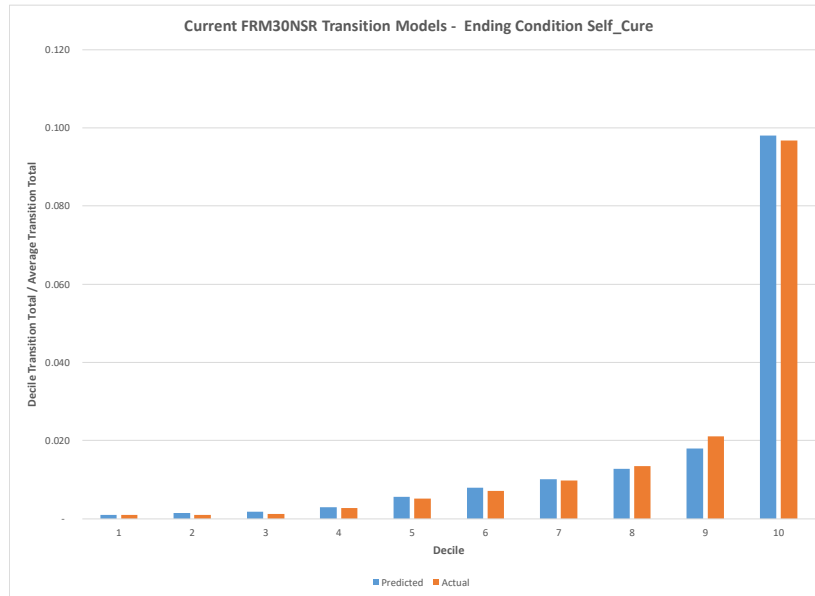
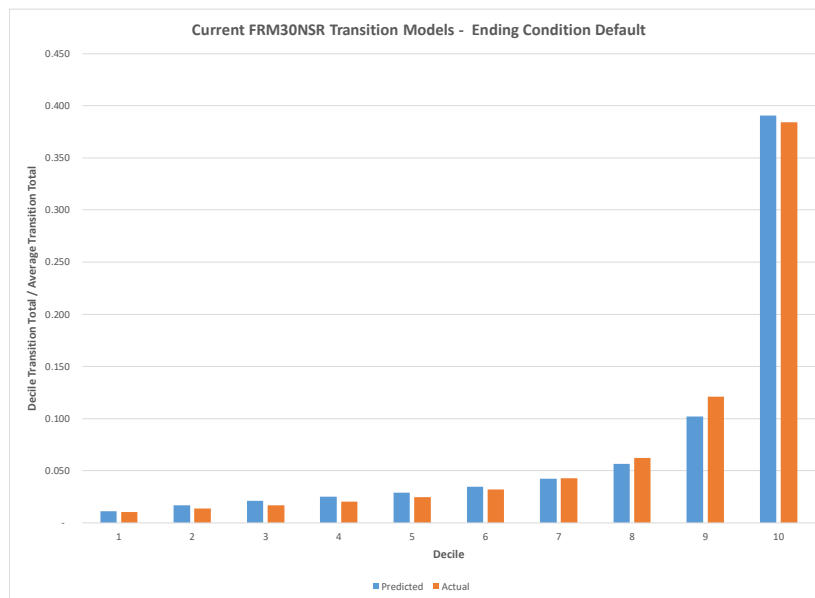


Figure 19: Current FRM30NSR Transition Model Validation - Ending Condition Default



## Current FRM30SR Transition Models

The validation charts by ending condition for the FRM30SR models are shown below.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 229

Figure 20: Current FRM30SR Transition Model Validation - Ending Condition Self-Cure

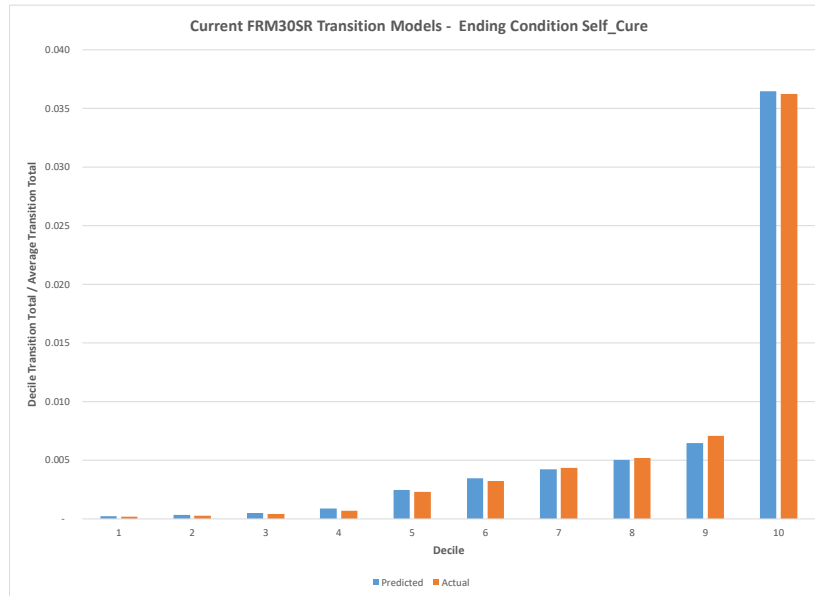
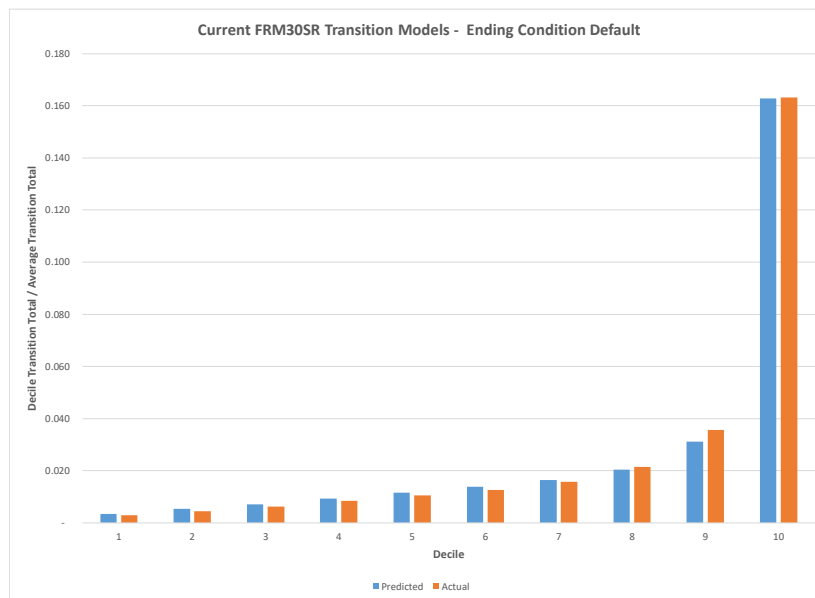


Figure 21: Current FRM30SR Transition Model Validation - Ending Condition Default

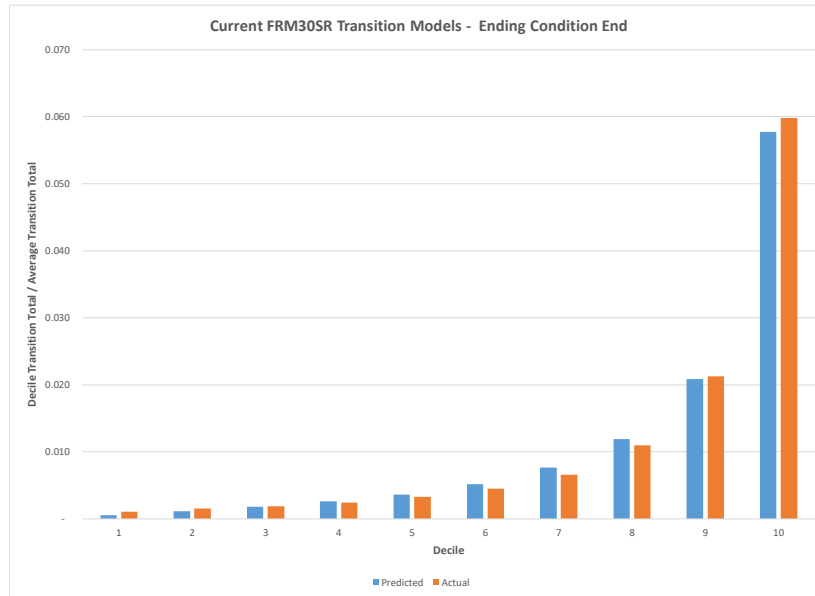


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 230

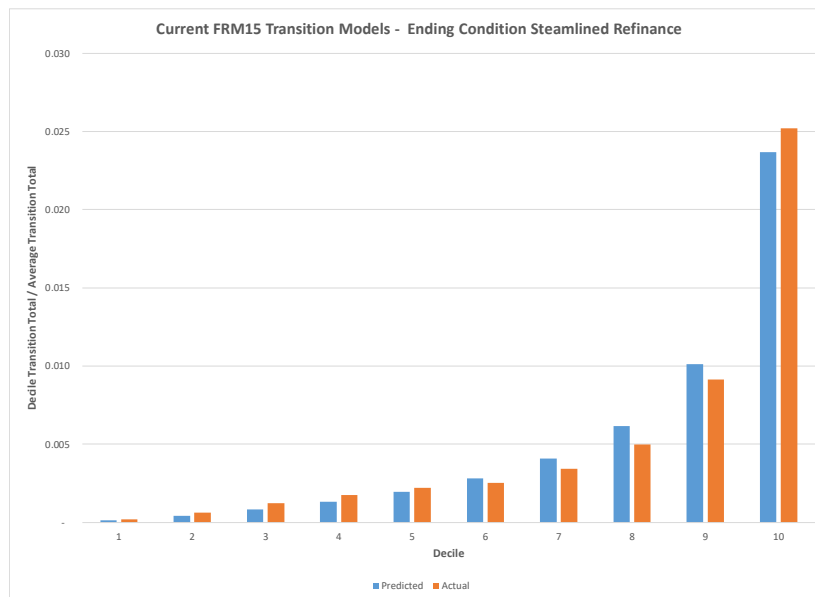
Figure 22: Current FRM30SR Transition Model Validation - Ending Condition End



## Current FRM15 Transition Models

The validation charts by ending condition for the FRM15 models are shown below.

Figure 23: Current FRM15 Transition Model Validation - Ending Condition Streamlined Refinance



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

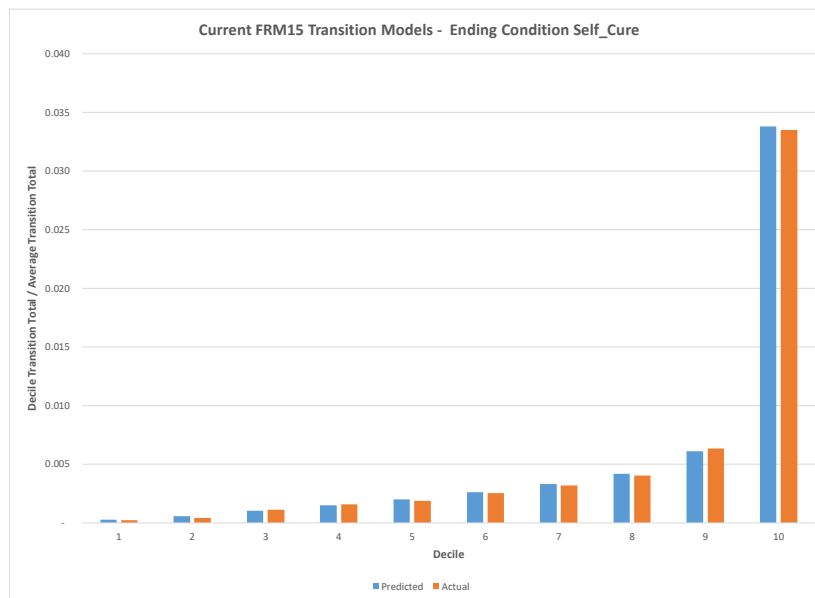
November 12, 2020

Page 231

Figure 24: Current FRM15 Transition Model Validation - Ending Condition Default



Figure 25: Current FRM15 Transition Model Validation - Ending Condition Self-Cure

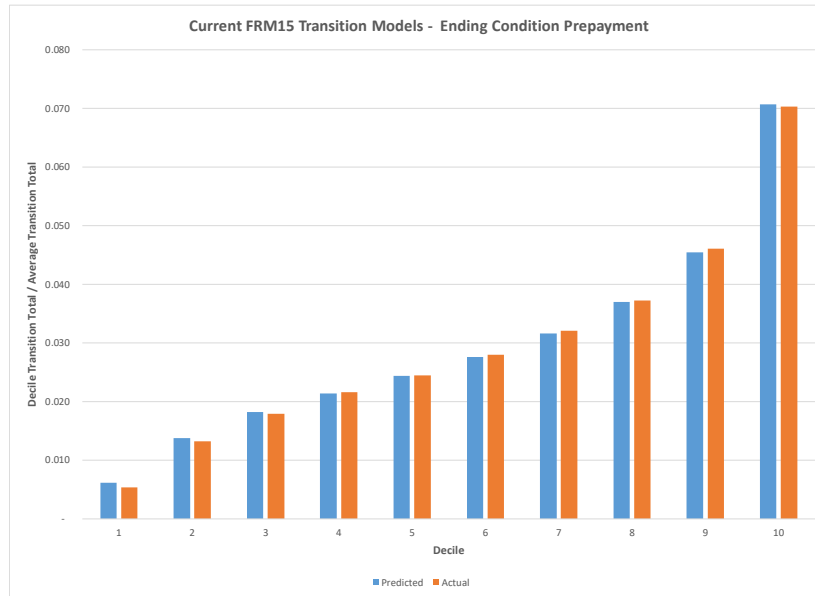


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 232

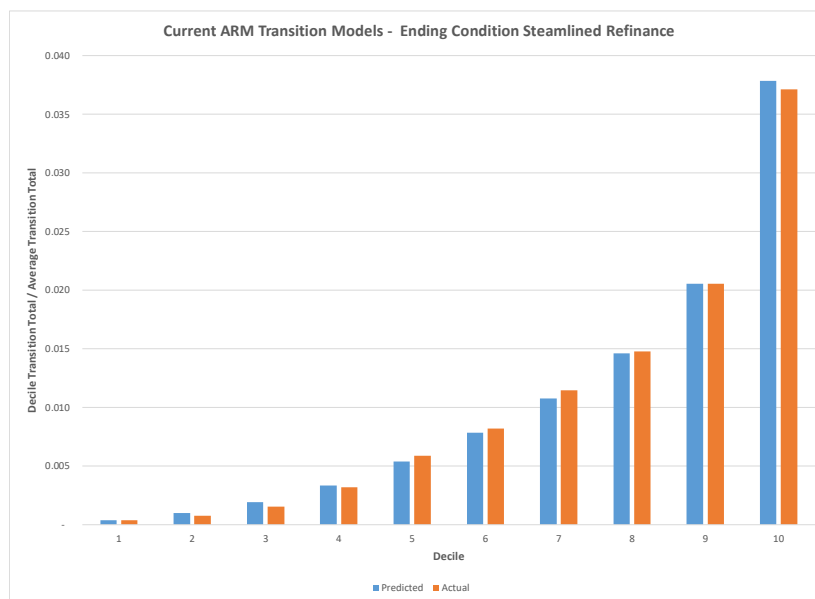
Figure 26: Current FRM15 Transition Model Validation - Ending Condition Prepayment



## Current ARM Transition Models

The validation charts by ending condition for the ARM model are shown below.

Figure 27: Current ARM Transition Model Validation - Ending Condition Streamlined Refinance





# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 233

Figure 28: Current ARM Transition Model Validation - Ending Condition Default

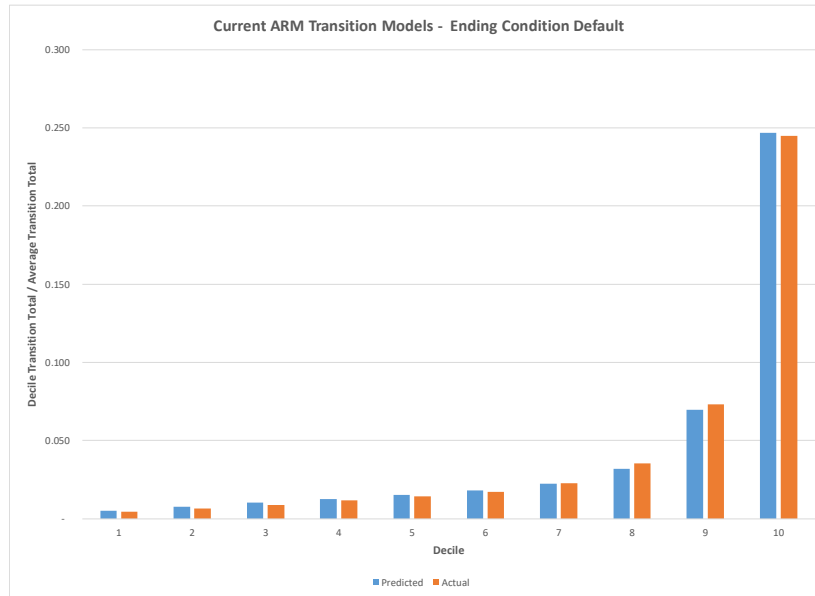
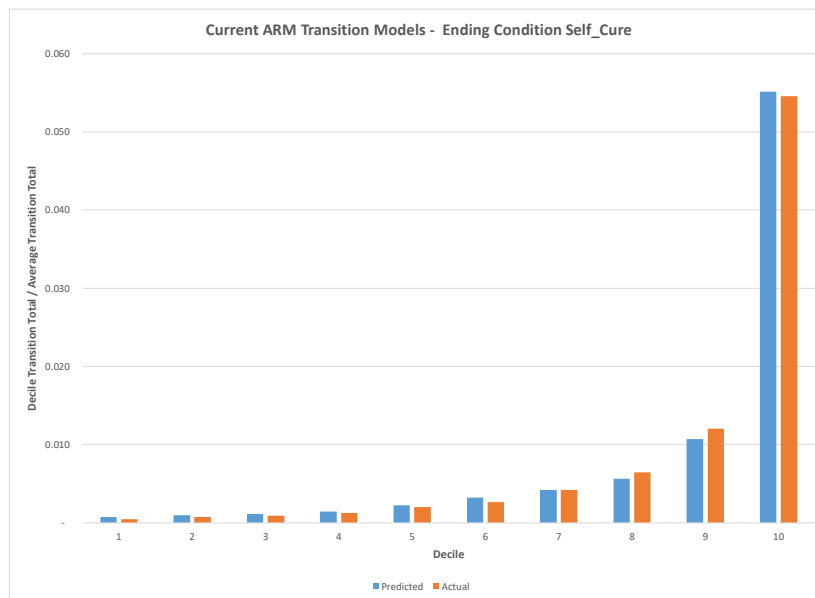


Figure 29: Current ARM Transition Model Validation - Ending Condition Self-Cure

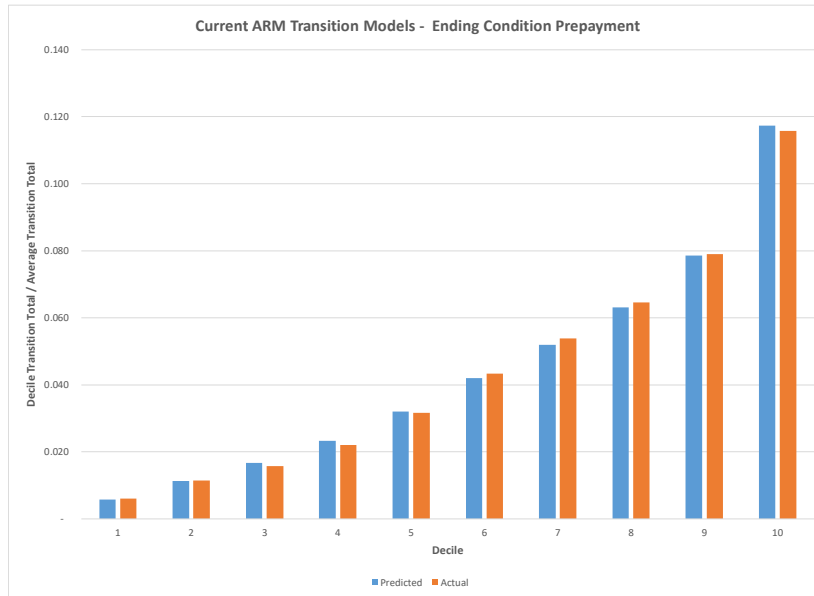


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 234

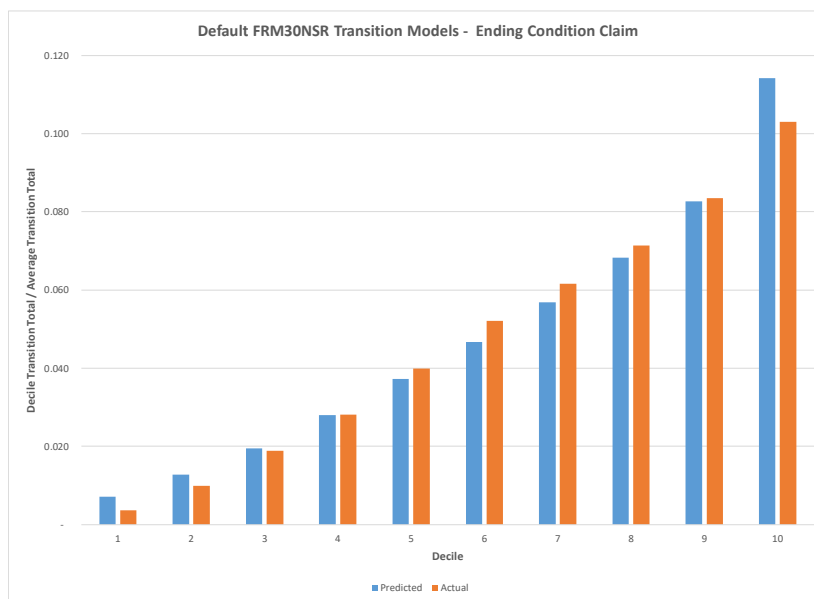
Figure 30: Current ARM Transition Model Validation - Ending Condition Prepayment



## Default FRM30NSR Transition Models

The validation charts by ending condition for the FRM30NSR models are shown below.

Figure 31: Default FRM30 Transition Model Validation - Ending Condition Claim



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 235

Figure 32: Default FRM30 Transition Model Validation - Ending Condition Cure with Modification

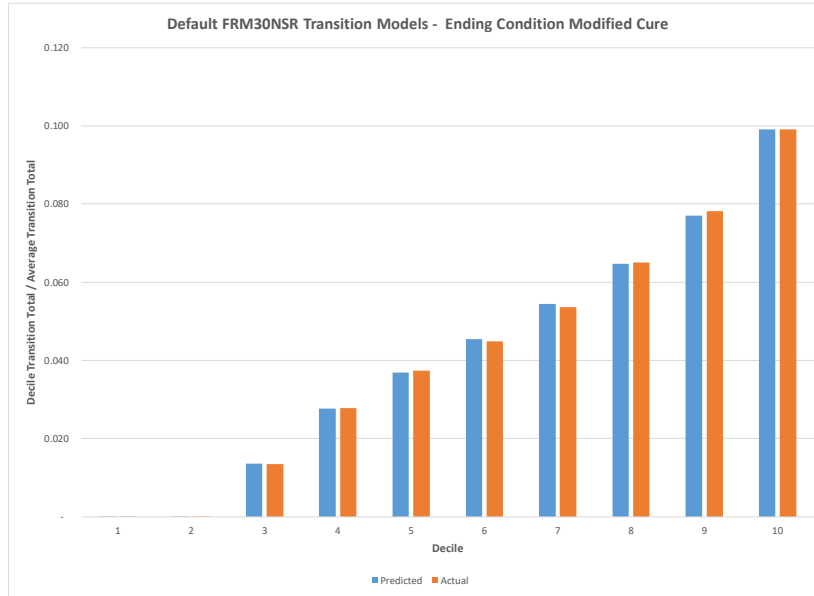
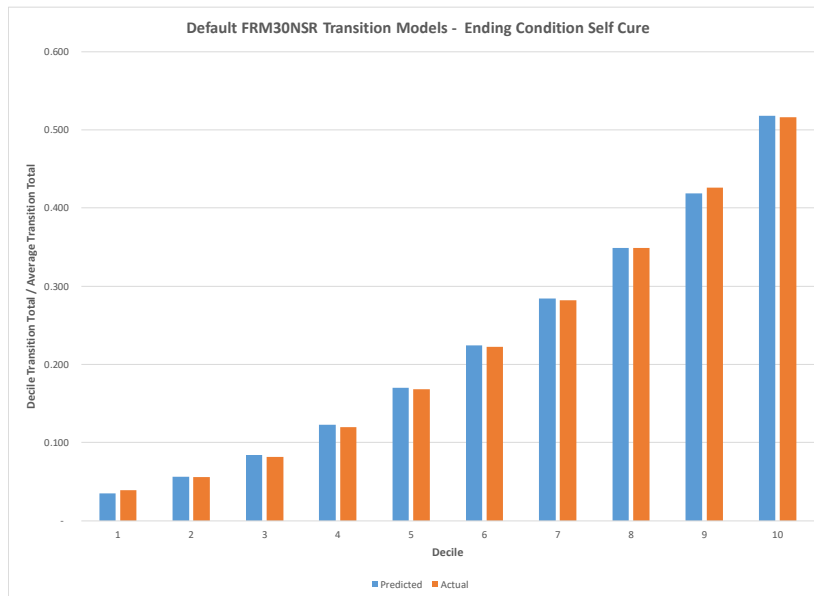


Figure 33: Default FRM30 Transition Model Validation - Ending Condition Self-Cure

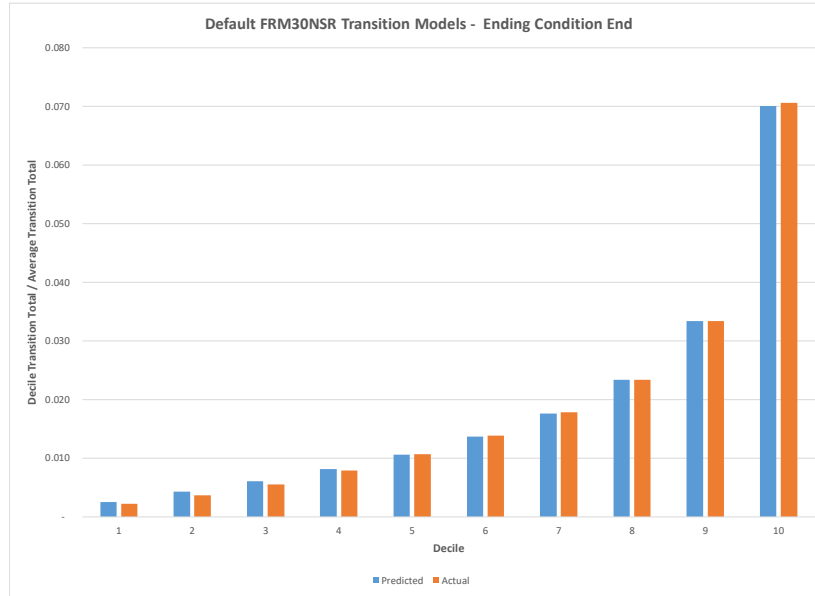


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 236

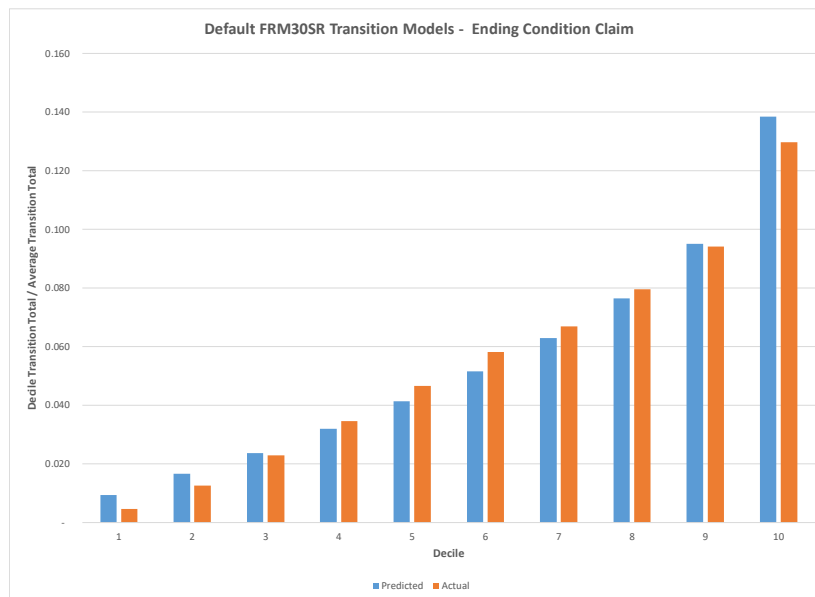
Figure 34: Default FRM30 Transition Model Validation - Ending Condition End



## Default FRM30SR Transition Models

The validation charts by ending condition for the FRM30SR models are shown below.

Figure 35: Default FRM30 Transition Model Validation - Ending Condition Claim



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 237

Figure 36: Default FRM30 Transition Model Validation - Ending Condition Cure with Modification

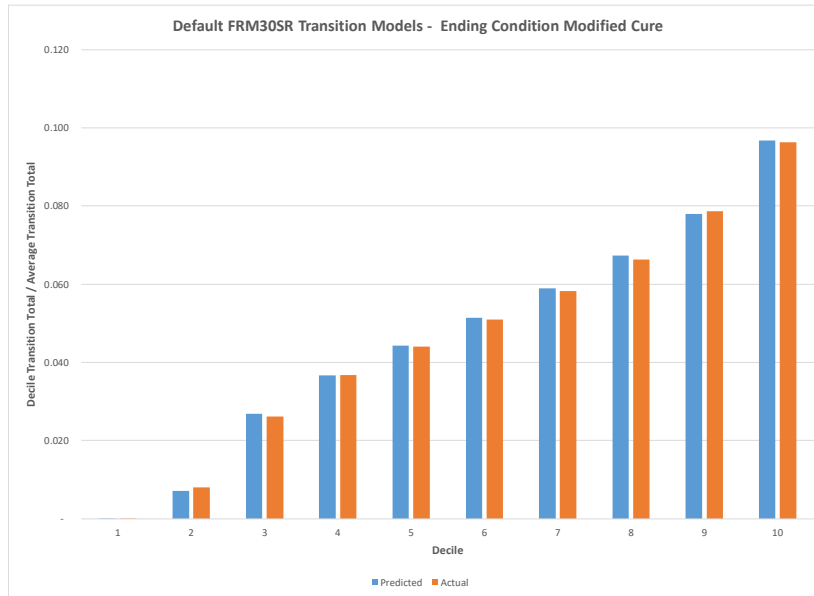
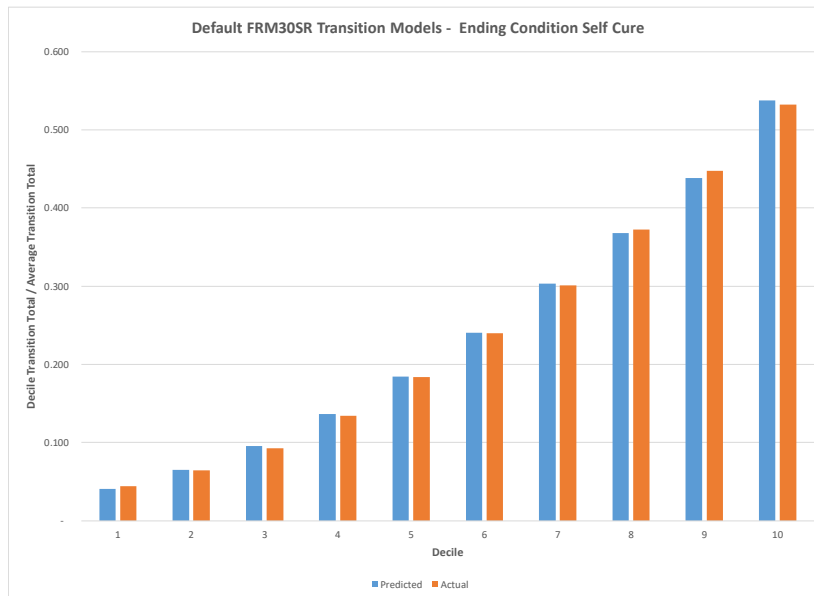


Figure 37: Default FRM30 Transition Model Validation - Ending Condition Self-Cure

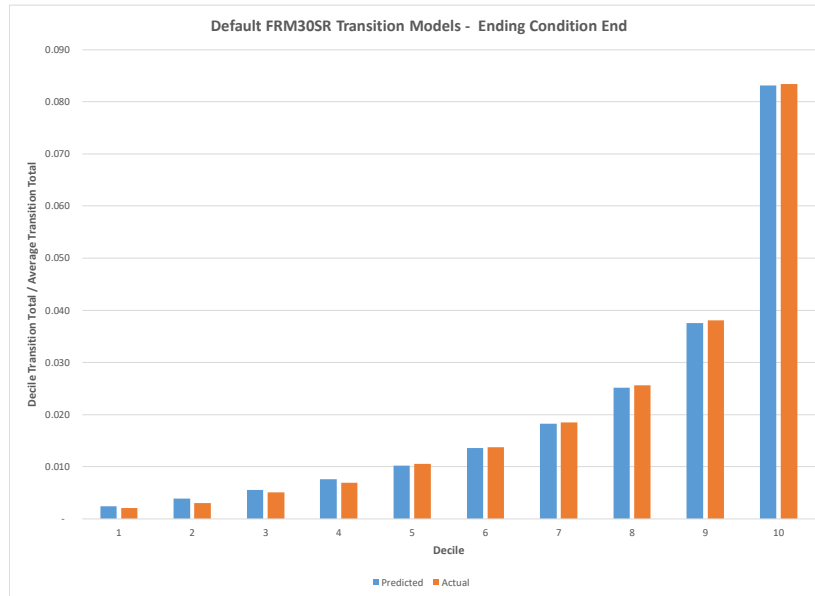


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 238

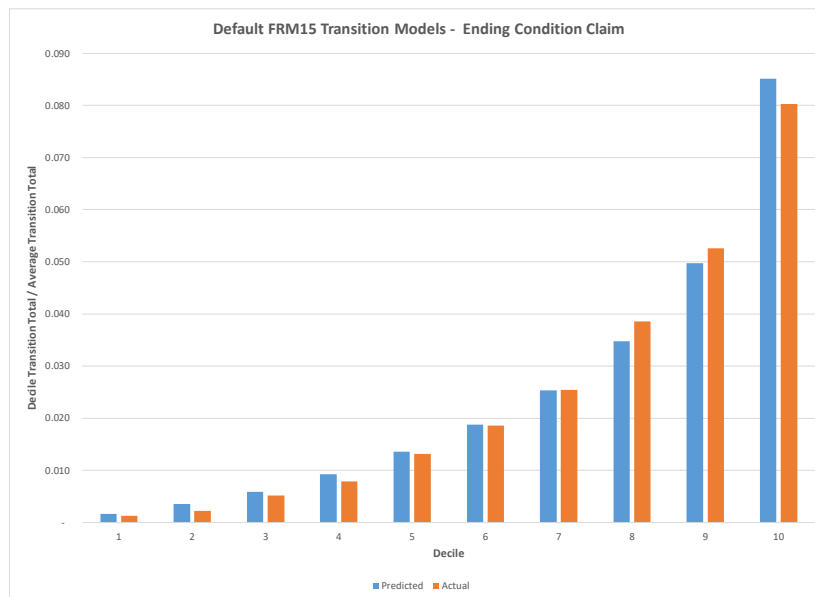
Figure 38: Default FRM30 Transition Model Validation - Ending Condition End



## Default FRM15 Transition Models

The validation charts by ending condition for the FRM15 model are shown below.

Figure 39: Default FRM15 Transition Model Validation - Ending Condition Claim



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 239

Figure 40: Default FRM15 Transition Model Validation - Ending Condition Cure with Modification

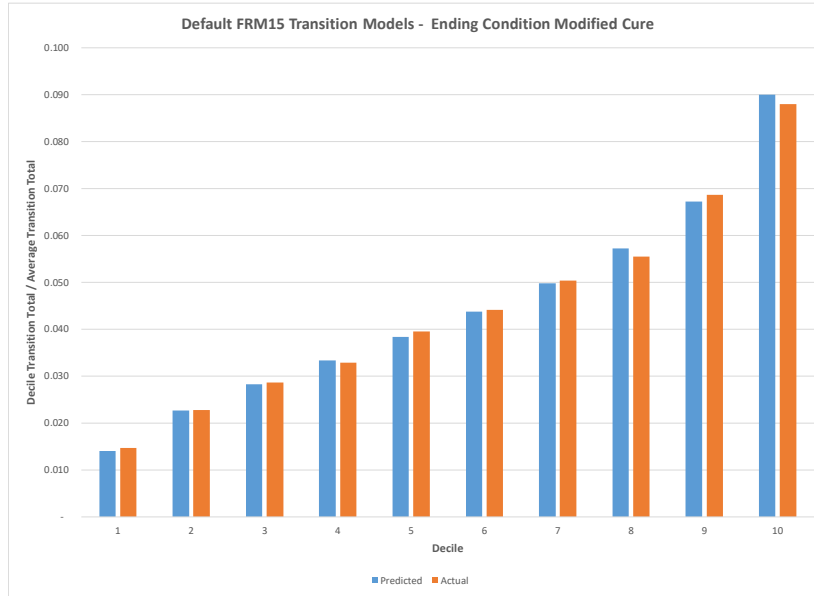
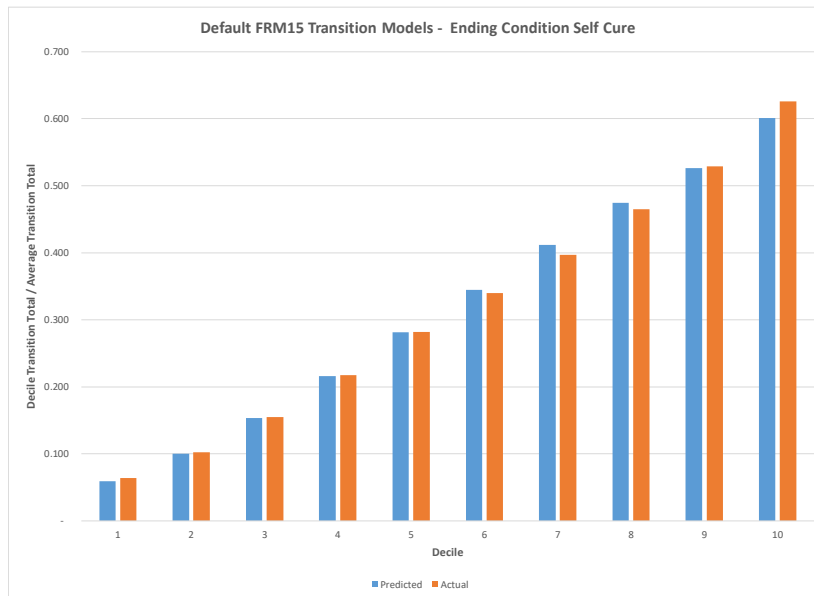


Figure 41: Default FRM15 Transition Model Validation - Ending Condition Self-Cure

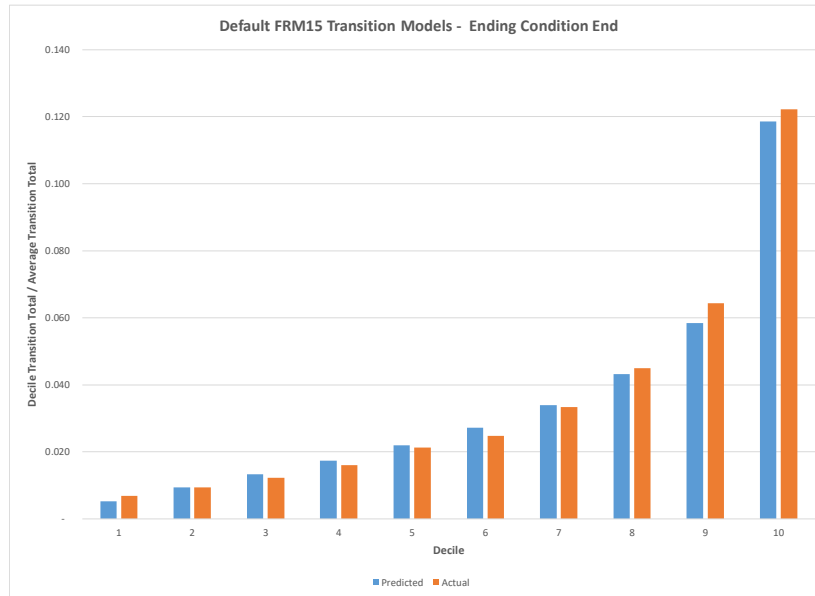


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 240

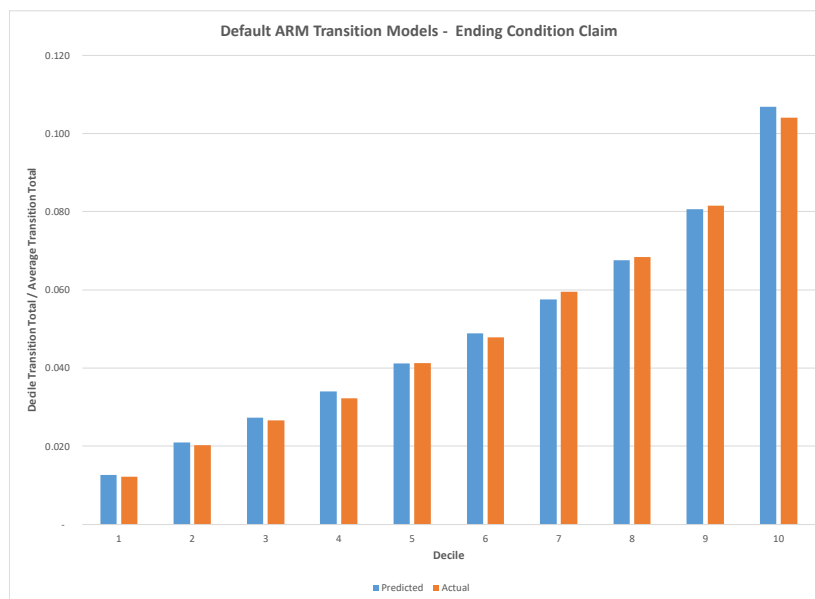
Figure 42: Default FRM15 Transition Model Validation - Ending Condition End



## Default ARM Transition Models

The validation charts by ending condition for the ARM models are shown below.

Figure 43: Default ARM Transition Model Validation - Ending Condition Claim





# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 241

Figure 44: Default ARM Transition Model Validation - Ending Condition Cure with Modification

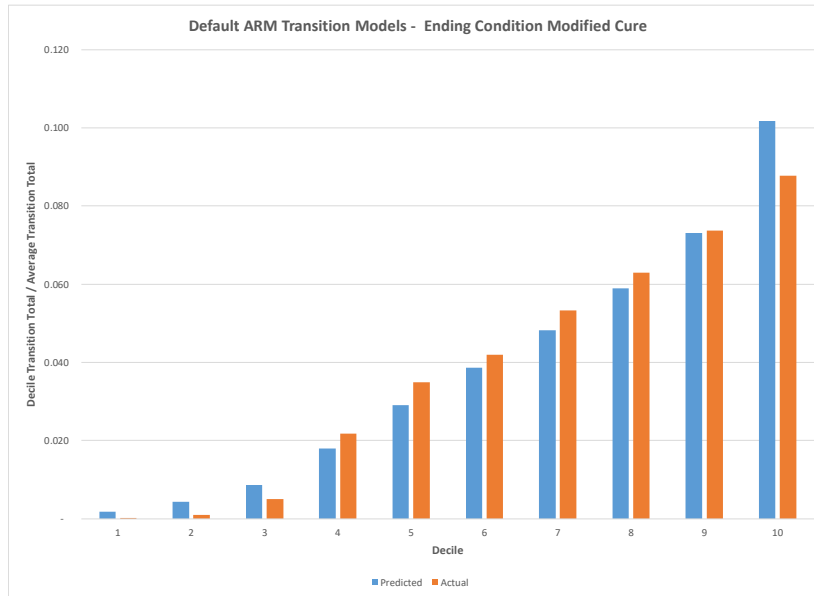
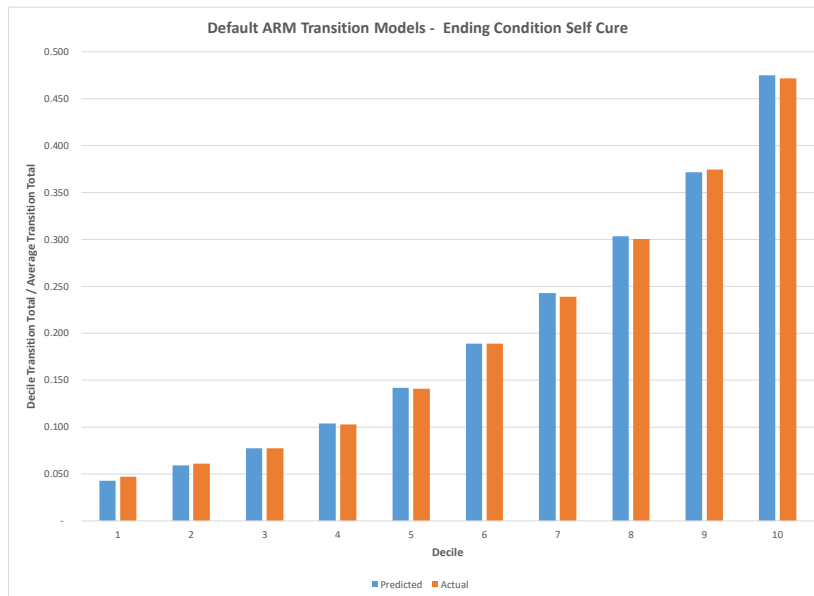


Figure 45: Default ARM Transition Model Validation - Ending Condition Self-Cure

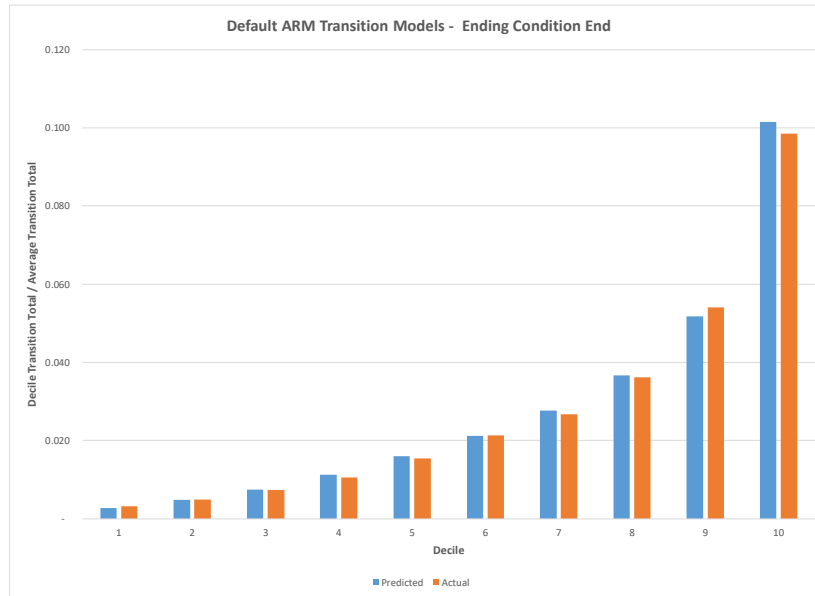


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 242

Figure 46: Default ARM Transition Model Validation - Ending Condition End



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 243

### Appendix C: Loss Severity Models

---

This appendix describes the loss severity models used in this Actuarial Review. One of the primary sources of variation in the MMI performance has been the loss severity experienced on mortgages that terminate as claims. In the case of a single mortgage, net loss is defined as the difference between the acquisition cost to HUD (acq\_cost\_to\_HUD) from the IDB table and the recoveries realized by FHA on properties owned. We predict the net loss by modeling the probability of the type of claim that develops, then modeling separately the loss for each type of claim and the recovery for real estate owned (REO) claims.

In this appendix, we also summarize the model specifications, describe the explanatory variables used, provide the model parameters and provide validation exhibits for the final models.

#### Model Specifications

Typically, when an FHA-endorsed mortgage terminates as a claim, the property is conveyed to FHA, and FHA makes a payment to the lender to settle the claim and acquire the underlying property. That is, the underlying house becomes REO. The claim payment FHA makes to the servicer, known as the acquisition cost, consists of three components:

1. the outstanding unpaid principal balance on the mortgage;
2. the foregone interest advanced by the servicer as a result of the mortgage default; and
3. legal and administrative costs paid by the servicer associated with foreclosure, including any expenses associated with the cost of repairing or maintaining the property prior to conveyance.

The formula for acquisition cost is:

$$\text{Acquisition Cost} = \text{Unpaid Principal Balance} + \text{Foregone Interest} + \text{Foreclosure Expense}$$

Following acquisition, FHA attempts to sell the property, sometimes at a reduced price in order to assist low-income prospective homebuyers in achieving homeownership. During the period when the property is held by FHA, but not yet sold, FHA incurs various holding costs associated with maintenance, repairs, tax payments and expenses incurred in preparing the property for sale. Upon sale of the collateral property, FHA receives the sale price less any sales expenses. In sum, the net loss amount is the net amount that FHA cannot recoup from this process:

$$\text{Net Loss} = \text{Acquisition Cost} + \text{Holding Cost} - \text{Sale Price} + \text{Sale Expense}$$

Table 61 shows the distribution of different types of FHA claim terminations. Conveyance refers to the foreclosure procedure discussed above, wherein the property is conveyed to FHA after foreclosure is completed. This is the most common type of claim.

FHA permits pre-foreclosure sales (PFS) as an alternative to the foreclosure process. In the case of a PFS, the property is sold by the borrower without the foreclosure process being completed, or even started in some cases. Instead of acquiring the foreclosed house, FHA directly pays the loss amount claimed by the lender. The

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 244

loss amount of a PFS case is reported as an acquisition cost to FHA. By 2012, the percentage of PFS was just under 24%. Since then, the percentage of PFS has decreased to 7.34%.

There were a significant volume of note (non-performing mortgage) sales from claim Fiscal Year 2003 through claim Fiscal Year 2006. From claim Fiscal Year 2007 to claim Fiscal Year 2012, there were significantly fewer note sales. By 2014, however, the percentage of note sales rose above 27%. In these cases, the expenses of foreclosure procedures and subsequent house sales are avoided by FHA. Note sales are discretionary and highly unpredictable. We do not model note sales as a continuing program.

FHA changed its servicing guide in 2013 to allow foreclosure without conveyance. This consists of a Third Party Sale (TPS) during the foreclosure auction. A third party, instead of FHA, acquires the property directly from the foreclosure auction. This process allows FHA to avoid the process and expenses of property disposition after conveyance including any associated holding costs. TPS' have increased significantly since 2012, accounting for nearly 61% of claims in 2019 and 48% of claims in 2020.

Table 61: Percentage of Claim Termination Types by Fiscal Claim Year

Claim Year	Conveyance (REO)	Note Sales	Third Party Sales (TPS)	Pre Foreclosure Sale (PFS)
1999	94.86%	0.11%	0.00%	5.02%
2000	95.06%	0.09%	0.00%	4.85%
2001	95.03%	0.01%	0.00%	4.97%
2002	94.33%	0.00%	0.00%	5.66%
2003	86.74%	8.34%	0.00%	4.92%
2004	85.57%	8.41%	0.00%	6.02%
2005	83.29%	9.79%	0.00%	6.91%
2006	89.37%	2.83%	0.00%	7.80%
2007	92.80%	0.00%	0.00%	7.20%
2008	93.06%	0.00%	0.10%	6.84%
2009	90.06%	0.00%	0.01%	9.93%
2010	84.46%	0.31%	0.00%	15.22%
2011	76.29%	1.17%	0.02%	22.51%
2012	71.24%	1.32%	3.59%	23.86%
2013	56.72%	17.66%	6.87%	18.74%
2014	42.68%	27.29%	15.40%	14.63%
2015	54.26%	16.27%	18.25%	11.22%
2016	49.54%	11.51%	29.28%	9.66%
2017	38.14%	6.24%	46.96%	8.66%
2018	34.42%	0.11%	56.30%	9.17%
2019	30.92%	0.13%	60.84%	8.10%
2020	44.36%	0.00%	48.30%	7.34%

Table 62 shows the average net loss for the combined foreclosure (REO and TPS) and PFS claims by claim Fiscal Year for 1991 to 2020. The average net loss increased from 1991 to 2012, reaching a high of almost \$129,000 in Fiscal Year 2013. Since 2011, the average net loss had been decreasing through 2019, but has increased slightly in 2020.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 245

Table 62: Historical Average Net Loss

Claim Year	Average Net Loss
1991	61,095
1992	62,389
1993	65,614
1994	68,850
1995	71,118
1996	73,864
1997	77,434
1998	81,185
1999	84,226
2000	85,883
2001	87,069
2002	88,206
2003	91,208
2004	93,004
2005	94,310
2006	97,606
2007	101,710
2008	110,001
2009	118,373
2010	127,977
2011	128,833
2012	128,882
2013	124,550
2014	112,660
2015	115,441
2016	107,382
2017	94,977
2018	86,823
2019	79,878
2020	88,631

### Net Loss Severity Model Specification

As described above, there are several components of the total loss amount, and each component is influenced by a number of factors. Foregone interest depends on the interest rate on the mortgage and on the length of the default-to-claim lag. Foreclosure expenses can vary depending on whether a judicial foreclosure process is used that can lengthen the time period of the foreclosure process. Repair expenses may be a function of the financial condition of the borrowers, which we proxy by credit scores. Sale prices are influenced by the house price appreciation since origination and by the prevailing local housing market conditions during the default and property disposition periods. Several components of the net loss amount involve expenses that are fixed across foreclosed properties. Hence, mortgages with lower values are more likely to realize higher net losses as a percentage of the sales amount, as the amount of the recovery will be smaller relative to higher value homes.

As shown in Table 61, the distribution between REO/TPS (foreclosure) and PFS was relatively stable through Fiscal Year 2009. Beginning in Fiscal Year 2010, there were widespread house price declines and a higher volume of defaults. As a result, the foreclosure claim process had been lengthened and foreclosure claims were delayed,

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

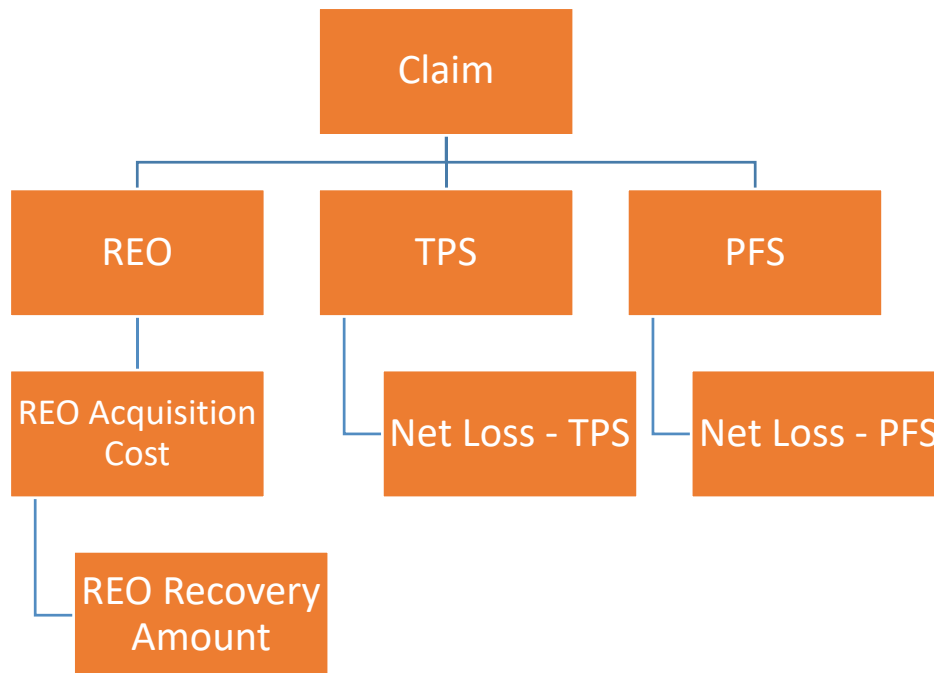
Page 246

while the PFS process has remained relatively stable. From Fiscal Year 2009 to 2012, the PFS share increased significantly. Since Fiscal Year 2012, the PFS share has declined. Moreover, the proceeds recovered from REO and PFS sales differ significantly. To achieve more accurate estimates of net loss severities, we adopted a three-stage model:

1. Model to predict the development of an REO, TPS or PFS claims
2. Model of REO acquisition cost and TPS and PFS net loss
3. Model of recovery amount conditional on claim being a foreclosure REO claim

The net loss severity model follows the flowchart in Figure 47.

Figure 47: Net Loss Severity Model Structure



First, we estimate the probability that a claim is settled by the REO, TPS, or PFS process. To model the first-stage choice event, we used a multinomial logistic model approach to estimate the probability of the claim settlement type.

Second, we estimate the REO Acquisition Amount, TPS net loss and PFS net loss as a function of all the same explanatory factors used in the multinomial model. The gross loss severity distribution is smooth and continuous with a long right tail. Thus, we use a GLM approach with a Gamma error structure and a log link function to develop the gross loss severity models. The Gamma structure is used for each loss severity model (REO, TPS, PFS). For REO claims, a recovery model estimating sales proceeds net of the Capital Income Expenses is built using a similar framework.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 247

In addition to the loss severity models described above, we also developed a set of models to project loss mitigation costs. Implemented in 1996, the loss mitigation program was designed as a way to help financially stressed borrowers stay in their homes. Loss mitigation costs can be incurred from modifying the terms of the mortgage, allowing a borrower to refinance into a new mortgage and writing off a portion of the unpaid principal (partial claim), or a forbearance, which is a written agreement with the borrower which includes a plan to reinstate the mortgage. The loss mitigation cost is modeled using a GLM with a Gamma error structure.

Thus, the estimated net loss to the MMI is the expected value of net loss of the different claim types:

$$\text{Net Loss} = \text{Probability of REO} * (\text{GrossLoss}_{\text{REO}} - \text{Recovery}) + \text{Probability of TPS} * \text{NetLoss}_{\text{TPS}} \\ + \text{Probability of PFS} * \text{NetLoss}_{\text{PFS}} + \text{Probability of Loss Mitigation} * \text{Net Loss Mitigation Cost}$$

### Estimation Sample

The sample used to estimate the loss severity model consists of mortgage level data from the FHA single-family data warehouse. The available data covers the period from the first quarter of Fiscal Year 1975 to the third quarter of Fiscal Year 2020. In total, there are over 2.9 million claims in the FHA database.

The models were built using a traditional train/validate approach. A random sample of the data is used to train the models, and the remaining data is used to validate and refine the model parameters and to determine inclusion and exclusion of explanatory variables.

### Explanatory Variables

Multiple categories of explanatory variables were used.

- Fixed initial mortgage characteristics: ARM adjustment period, mortgage product, interest rate, initial mortgage size, spread at origination
- Fixed initial borrower characteristics: down payment assistance, first time home buyer, credit score
- Property characteristics: the number of living units, initial home values
- Dynamic variables based on mortgage information: prior default indicator, prior mortgage modification, LTV ratio, interest rate spread, TEI, age of mortgage
- Dynamic variables derived by combining mortgage information and external economic data: spread, spread at origination
- Dynamic macroeconomic variables: 10-year average unemployment rate, change in the unemployment rate, prior year unemployment rate, HPI, state unemployment rate relative to countrywide unemployment rate, CMT rates, state unemployment rate
- Geographic variables: judicial state, collateral state

Most of the explanatory variables used in the loss severity model are the same as those used in the mortgage status transition models. The additional variables used in the loss severity models are defined below.

- **Product**: loan product type. This variable is incorporated as a categorical variable.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 248

- **Balance:** outstanding mortgage balance. This variable is incorporated as a variate.
- **Deltatm3:** change in three-month CMT rate from policy inception to current. This variable is incorporated as a grouped categorical variable.
- **Arm\_ind:** ARM product type indicator. This variable is incorporated as a grouped categorical variable.

### Model Parameters

#### Loss Mitigation Binomial Model

The model parameters for the binomial model to estimate whether a claim is a loss mitigation (HAMP) claim are below.

Table 63: Loss Mitigation Binomial Model Parameters

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				0.0675	0.6113	0.9121
SVSBOI_pw1		Small Business Optimism Index	median(0,SBOI-80,95-80)	-0.0053	0.0121	0.6628
SVSBOI_pw2		Small Business Optimism Index	median(0,SBOI-95,110-95)	-0.0352	0.0015	0.0000
SMproduct	ARM	Categorical of product type	adjustable rate mortgage	0.2769	0.0411	0.0000
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance	0.1271	0.0658	0.0534
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage	-1.1966	0.0496	0.0000
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance	-1.1723	0.0961	0.0000
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance	-0.1576	0.0292	0.0000
SMproduct	z_FRM30	Categorical of product type	30 year fixed rate mortgage			
SVloansize_raw_grp		Variate version of loansize_raw	min(loansize/1000,600)	0.0023	0.0001	0.0000
SMpriordef	L01	Categorical of prior defaults	prior_default_count = 1	-0.1139	0.0148	0.0000
SMpriordef	L02	Categorical of prior defaults	prior_default_count = 2	-0.2435	0.0165	0.0000
SMpriordef	L03	Categorical of prior defaults	prior_default_count >= 3	-0.3930	0.0161	0.0000
SMpriordef	Z00	Categorical of prior defaults	prior_default_count = 0			
SMpriormod	L01	Categorical of Prior Loan Modifications	prior_mod_cnt = 1	0.1361	0.0127	0.0000
SMpriormod	L02	Categorical of Prior Loan Modifications	prior_mod_cnt = 2	0.2197	0.0189	0.0000
SMpriormod	L03	Categorical of Prior Loan Modifications	prior_mod_cnt >= 3	0.3384	0.0256	0.0000
SMpriormod	Z00	Categorical of Prior Loan Modifications	prior_mod_cnt = 0			



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 249

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
SVpriordef_pw1		Variate piecewise version of prior defaults	$\min(\text{prior\_default\_cnt}, 15) - 3$	-0.1434	0.0383	0.0002
SVpriormod_pw1		Variate piecewise version of prior_mod_cnt	$\text{median}(0, \text{prior\_mod\_cnt} - 3, 15 - 3)$	-0.0778	0.0189	0.0000
SMseason	L01	Categorical of season	season = "winter"	-0.1075	0.0137	0.0000
SMseason	L02	Categorical of season	season = "spring"	-0.0870	0.0130	0.0000
SMseason	L03	Categorical of season	season = "summer"	-0.1529	0.0128	0.0000
SMseason	Z04	Categorical of season	season = "fall"			
SMperiodnbr_LML	L01_04	Categorical of period number	$1 \leq \text{period\_number} \leq 4$	-3.8880	0.2845	0.0000
SMperiodnbr_LML	L05	Categorical of period number	period_number = 5	-2.2790	0.1348	0.0000
SMperiodnbr_LML	L06	Categorical of period number	period_number = 6	-1.1753	0.0726	0.0000
SMperiodnbr_LML	L07	Categorical of period number	period_number = 7	-0.2839	0.0392	0.0000
SMperiodnbr_LML	Z00	Categorical of period number	base level: else			
SVperiodnbr_pw1		Variate piecewise version of period number	$\text{median}(0, \text{period\_number} - 8, 40 - 8)$	-0.0389	0.0007	0.0000
SVperiodnbr_pw2		Variate piecewise version of period number	$\text{median}(0, \text{period\_number} - 40, 53 - 40)$	-0.0144	0.0020	0.0000
SVperiodnbr_pw3		Variate piecewise version of period number	$\text{median}(0, \text{period\_number} - 53, 68 - 53)$	-0.0098	0.0025	0.0000
SVperiodnbr_pw4		Variate piecewise version of period number	$\text{median}(0, \text{period\_number} - 68, 108 - 68)$	-0.0116	0.0019	0.0000
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1	-0.0456	0.0097	0.0000
SMjudicial	Z00	Categorical of judicial (judicial state)	base level: else			
SMRatioTmpTei	L00	Categorical of ratio_tmp_te_i (front-end ratio)	ratio_tmp_te_i=0	1.1367	0.0491	0.0000
SMRatioTmpTei	Z01	Categorical of ratio_tmp_te_i (front-end ratio)	base level: else			
SVratiotmptei_pw1		Variate piecewise version of front end ratio	$\text{median}(0, \text{ratio\_tmp\_te}_i - 0, 24 - 0)$	0.0331	0.0020	0.0000
SVratiotmptei_pw2		Variate piecewise version of front end ratio	$\text{median}(0, \text{ratio\_tmp\_te}_i - 24, 36 - 24)$	0.0739	0.0014	0.0000
SVratiotmptei_pw3		Variate piecewise version of front end ratio	$\max(0, \text{ratio\_tmp\_te}_i - 36)$	0.0219	0.0027	0.0000

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 250

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
SVsato_pw1		Spread at origination	min(sato+0.1,0)	-0.0922	0.0234	0.0000
SVsato_pw2		Spread at origination	median(0,sato+0.1,0.7+0.1)	-0.2187	0.0191	0.0000
SVsato_pw3		Spread at origination	max(0,sato-0.7)	-0.0890	0.0341	0.0091
SVhpa2yb_pw1		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	min(hpa2y_blen ded_r,85)	-0.0004	0.0070	0.9545
SVhpa2yb_pw2		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	median(0,hpa2y_blen ded_r-85,95-85)	-0.0199	0.0110	0.0698
SVhpa2yb_pw3		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	median(0,hpa2y_blen ded_r-95,113-95)	-0.0143	0.0017	0.0000
SVhpa2yb_pw4		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	median(0,hpa2y_blen ded_r-113,120-113)	0.0262	0.0028	0.0000
SVhpa2yb_pw5		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	max(0,hpa2y_blen ded_r-120)	0.0160	0.0048	0.0008
SMdurdefepi	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	0.3897	0.0156	0.0000
SMdurdefepi	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	0.5205	0.0166	0.0000
SMdurdefepi	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	0.5380	0.0178	0.0000
SMdurdefepi	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	0.5896	0.0196	0.0000
SMdurdefepi	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	0.6549	0.0218	0.0000
SMdurdefepi	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	0.6419	0.0239	0.0000
SMdurdefepi	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	0.6556	0.0265	0.0000
SMdurdefepi	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	0.7112	0.0299	0.0000
SMdurdefepi	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	0.7537	0.0341	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 251

Variable	ClassVal0	Description	Description Detail	Estimate	StdErr	ProbChiSq
SMdurdefepi	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 11	0.7527	0.0266	0.0000
SMdurdefepi	Z01	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 1			
SVdurdefepi_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	0.0149	0.0030	0.0000
SVdurdefepi_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-30,40-30)	0.0178	0.0140	0.2044
SMDeltaTm3	L01	Categorical of DeltaTm3Init_r <sup>2</sup> (change in 3-month Treasury rate from policy inception to current)	DeltaTm3Init_r > 600	-0.1244	0.0133	0.0000
SMDeltaTm3	Z00	Categorical of DeltaTm3Init_r <sup>2</sup> (change in 3-month Treasury rate from policy inception to current)	base level: else			
SMcredit	L01	Credit Score	credit_score = 0	0.0288	0.0352	0.4135
SMcredit	L02	Credit Score	credit_score < 500	-0.1631	0.0772	0.0347
SMcredit	Z00	Credit Score	base level: else			
SVcredit_pw1		Variate piecewise of Credit Score	median(0,credit_score-500,625-500)	-0.0024	0.0003	0.0000
SVcredit_pw2		Variate piecewise of Credit Score	median(0,credit_score-625,680-625)	0.0017	0.0003	0.0000
SVcredit_pw3		Variate piecewise of Credit Score	max(0,credit_score - 680)	0.0009	0.00	0.0196

### Loss Mitigation HAMP Severity Model

The model parameters for the HAMP claim severity model are shown below.

Table 64: Loss Mitigation HAMP Severity Model Parameters

Variable	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				5.7784	0.0609	0.0000
SVbalance_i_log		Variate version of log transformed	log(balance_i/1000)	0.9589	0.0037	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 252

Variable	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		outstanding balance at start of quarter				
SVCCI_pw1		Consumer Confidence Index	median(0,CCI-30,91)	-0.0065	0.0009	0.0000
SVCCI_pw2		Consumer Confidence Index	median(0,CCI-91,142-91)	0.0080	0.0007	0.0000
SMproduct	ARM	Categorical of product type	adjustable rate mortgage	0.0690	0.0142	0.0000
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance	-0.0136	0.0254	0.5908
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage	0.1802	0.0273	0.0000
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance	0.5436	0.0532	0.0000
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance	-0.0602	0.0120	0.0000
SMproduct	z_FRM30	Categorical of product type	30 year fixed rate mortgage	0.0000	0.0000	.
SMpriormod	L01	Categorical of Prior Loan Modifications	prior_mod_cnt = 1	-0.0916	0.0051	0.0000
SMpriormod	L02	Categorical of Prior Loan Modifications	prior_mod_cnt = 2	-0.0775	0.0081	0.0000
SMpriormod	L03	Categorical of Prior Loan Modifications	prior_mod_cnt >= 3	-0.0742	0.0116	0.0000
SMpriormod	Z00	Categorical of Prior Loan Modifications	prior_mod_cnt = 0	0.0000	0.0000	.
SVpriormod_pw1		Variate piecewise version of prior_mod_cnt	median(0,prior_mod_cnt-3,15-3)	-0.0159	0.0100	0.11
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1	0.0547	0.0040	0.0000
SMjudicial	Z00	Categorical of judicial (judicial state)	base level: else	0.0000	0.0000	.
SMRatioTmpTei	L00	Categorical of ratio_tmp_tei (front-end ratio)	ratio_tmp_tei=0	0.2719	0.0235	0.0000
SMRatioTmpTei	Z01	Categorical of ratio_tmp_tei (front-end ratio)	base level: else	0.0000	0.0000	.
SVratiotmptei_pw1		Variate piecewise version of front end ratio	median(0,ratio_tmp_tei-0,24-0)	0.0023	0.0010	0.0178
SVratiotmptei_pw2		Variate piecewise version of front end ratio	median(0,ratio_tmp_tei-24,36-24)	0.0134	0.0006	0.0000
SVratiotmptei_pw3		Variate piecewise version of front end ratio	median(0,ratio_tmp_tei-36,50-36)	0.0104	0.0010	0.0000
SMrfncind	LY	Categorical of rfnc_ind	rfnc_ind <> "N"	-0.0545	0.0059	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 253

Variable	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(refinanced loan indicator)				
SMrfncind	ZN	Categorical of rfnc_ind (refinanced loan indicator)	base level: else	0.0000	0.0000	.

### Third Party Sale Claims Logistic Model

The model parameters for the binomial model to predict the TPS claim type are shown below.

Table 65: TPS Claim Binomial Model Parameters

Variable	ClassVal0	Description	Description Detail	Response	Estimate	StdErr	ProbChiSq
Intercept				TPS	-6.8185	0.0959	0.0000
SVbalance_i		Outstanding balance at start of quarter		TPS	-0.0099	0.0007	0.0000
SVCCI_pw1		Consumer Confidence Index	median(0,CCI-30,91)	TPS	0.0516	0.0011	0.0000
SVCCI_pw2		Consumer Confidence Index	median(0,CCI-91,142-91)	TPS	0.0166	0.0014	0.0000
SVSBOI_pw1		Small Business Optimism Index	median(0,SBOI-80,95-80)	TPS	-0.0193	0.0072	0.0073
SVSBOI_pw2		Small Business Optimism Index	median(0,SBOI-95,110-95)	TPS	-0.0645	0.0034	0.0000
SMproduct	ARM	Categorical of product type	adjustable rate mortgage	TPS	0.2139	0.0389	0.0000
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance	TPS	0.3034	0.0540	0.0000
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage	TPS	-0.2924	0.0507	0.0000
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance	TPS	-0.1368	0.1016	0.1783
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance	TPS	0.1474	0.0198	0.0000
SVloansize_raw_grp		Variate version of loansize_raw	min(loansize/1000,600)	TPS	0.0106	0.0006	0.0000
SMseason	L01	Categorical of season	season = "winter"	TPS	-0.0296	0.0139	0.0339
SMseason	L02	Categorical of season	season = "spring"	TPS	0.1641	0.0136	0.0000
SMseason	L03	Categorical of season	season = "summer"	TPS	0.0194	0.0132	0.1425
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1	TPS	-0.0539	0.0100	0.0000
SMdpa_govt	LGovt	Categorical of down payment assistance, government level indicator	dpa = "govt"	TPS	-0.0485	0.0326	0.1364

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 254

Variable	ClassVal0	Description	Description Detail	Response	Estimate	StdErr	ProbChiSq
SMdpa_nprof	LNPro	Categorical of down payment assistance, non-profit level indicator	dpa = "nonprof"	TPS	0.1832	0.0161	0.0000
SMdpa_rel	LRela	Categorical of down payment assistance, non-profit level indicator	dpa = "relative"	TPS	0.0604	0.0153	0.0000
SVsato_pw1		Spread at origination	min(sato+0.1,0)	TPS	0.1752	0.0235	0.0000
SVsato_pw2		Spread at origination	median(0,sato+0.1,0.7+0.1)	TPS	-0.0356	0.0195	0.0678
SVsato_pw3		Spread at origination	max(0,sato-0.7)	TPS	-0.2303	0.0351	0.0000
SVhpa2yb_pw2		Variate piecewise of hpa2y_blen ded_r <sup>1</sup>	median(0,hpa2y_blen ded_r-85,95-85)	TPS	0.1059	0.0082	0.0000
SVhpa2yb_pw3		Variate piecewise of hpa2y_blen ded_r <sup>1</sup>	median(0,hpa2y_blen ded_r-95,113-95)	TPS	0.0978	0.0017	0.0000
SVhpa2yb_pw4		Variate piecewise of hpa2y_blen ded_r <sup>1</sup>	median(0,hpa2y_blen ded_r-113,120-113)	TPS	0.0014	0.0027	0.6055
SVhpa2yb_pw5		Variate piecewise of hpa2y_blen ded_r <sup>1</sup>	max(0,hpa2y_blen ded_r-120)	TPS	0.0228	0.0018	0.0000
SMycslope	L01	Categorical of yield curve slope	1<=ycslope<=2	TPS	0.2368	0.0212	0.0000
SMrfncind	LY	Categorical of rfnc_ind (refinanced loan indicator)	frst_tm_by = "Y"	TPS	-0.1167	0.0137	0.0000
SMDeltaTY10	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	TPS	-0.0179	0.0126	0.1552
SMDeltaTY10	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r > 130	TPS	0.1381	0.0259	0.0000
SMDeltaTm3	L01	Categorical of DeltaTm3Init_r <sup>3</sup> (change in 3-month Treasury rate from policy inception to current)	DeltaTm3Init_r > 600	TPS	0.0660	0.0166	0.0000
SMicredit_grp1	L450	Categorical of credit	0<credit_score<=450	TPS	-0.3757	0.1676	0.0250
SMicredit_grp2	L500	Categorical of credit	450<credit_score<=500	TPS	-0.1690	0.0685	0.0136

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 255

Variable	ClassVal0	Description	Description Detail	Response	Estimate	StdErr	ProbChiSq
SMicredit_grp3	L600	Categorical of credit	500<credit_score<=600	TPS	-0.1917	0.0182	0.0000
SMicredit_grp4	L630	Categorical of credit	600<credit_score<=630	TPS	-0.1279	0.0182	0.0000
SMicredit_grp5	L680	Categorical of credit	630<credit_score<=680	TPS	-0.0476	0.0166	0.0040
SMicredit_grp6	L720	Categorical of credit	680<credit_score<=720	TPS	-0.0407	0.0209	0.0521
SMicredit_grp7	L745	Categorical of credit	720<credit_score<=745	TPS	-0.0270	0.0314	0.3887
SMicredit_grp8	L800	Categorical of credit	745<credit_score<=800	TPS	-0.0019	0.0304	0.9505
SMicredit_grp9	L850	Categorical of credit	800<credit_score	TPS	0.0133	0.0897	0.8824

### Pre-Foreclosure Sale Claims Logistic Model

The model parameters for the binomial model to predict the PFS claim type are shown below.

Table 66: PFS Claim Binomial Model Parameters

Variable	ClassVal0	Description	Description Detail	Response	Estimate	StdErr	ProbChiSq
Intercept					-4.4278	0.1419	0.0000
SVbalance_i		Outstanding balance at start of quarter			-0.0084	0.0009	0.0000
SVCCI_pw1		Consumer Confidence Index	median(0,CCI-30,91)		-0.0282	0.0008	0.0000
SVCCI_pw2		Consumer Confidence Index	median(0,CCI-91,142-91)		0.0327	0.0019	0.0000
SVSBOI_pw1		Small Business Optimism Index	median(0,SBOI-80,95-80)		0.1194	0.0038	0.0000
SVSBOI_pw2		Small Business Optimism Index	median(0,SBOI-95,110-95)		0.0019	0.0055	0.7282
SMproduct	ARM	Categorical of product type	adjustable rate mortgage		-0.0777	0.0305	0.0109
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance		0.3088	0.0412	0.0000
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage		-0.6364	0.0632	0.0000
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance		-0.2604	0.1156	0.0243
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance		0.3341	0.0185	0.0000
SVloansize_raw_grp		Variate version of loansize_raw	min(loansize/1000,600)		0.0150	0.0008	0.0000
SMpriormod	L01	Categorical of Prior Loan Modifications	prior_mod_cnt = 1		0.0978	0.0138	0.0000
SMpriormod	L02	Categorical of Prior Loan Modifications	prior_mod_cnt = 2		0.3371	0.0253	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 256

Variable	ClassVal0	Description	Description Detail	Response	Estimate	StdErr	ProbChiSq
SMpriormod	L03	Categorical of Prior Loan Modifications	prior_mod_cnt >= 3		0.5424	0.0434	0.0000
SVpriormod_pw1		Variate piecewise version of prior_mod_cnt	median(0,prior_mod_cnt-3,15-3)		0.2745	0.0470	0.0000
SMseason	L01	Categorical of season	season = "winter"		-0.0819	0.0128	0.0000
SMseason	L02	Categorical of season	season = "spring"		0.0541	0.0125	0.0000
SMseason	L03	Categorical of season	season = "summer"		-0.0020	0.0124	0.8708
SMperiodnbr_clm	L01_04	Categorical of period number	1 <= period_number <= 4		1.3364	0.0699	0.0000
SMperiodnbr_clm	L05	Categorical of period number	period_number = 5		0.7151	0.0475	0.0000
SMperiodnbr_clm	L06	Categorical of period number	period_number = 6		0.3864	0.0364	0.0000
SMperiodnbr_clm	L07	Categorical of period number	period_number = 7		0.2402	0.0308	0.0000
SVperiodnbr_pw1		Variate piecewise version of period number	median(0,period_number-8,40-8)		-0.0456	0.0009	0.0000
SVperiodnbr_pw2		Variate piecewise version of period number	median(0,period_number-40,53-40)		0.0041	0.0030	0.1749
SVperiodnbr_pw3		Variate piecewise version of period number	median(0,period_number-53,68-53)		-0.0267	0.0053	0.0000
SVperiodnbr_pw4		Variate piecewise version of period number	median(0,period_number-68,108-68)		-0.0276	0.0058	0.0000
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1		0.1447	0.0097	0.0000
SVhpa2yb_pw1		Variate piecewise of hpa2y_blended_r <sup>1</sup>	min(hpa2y_blended_r,85)		0.0201	0.0017	0.0000
SVhpa2yb_pw2		Variate piecewise of hpa2y_blended_r <sup>1</sup>	median(0,hpa2y_blended_r-85,95-85)		-0.0079	0.0021	0.0001
SVhpa2yb_pw3		Variate piecewise of hpa2y_blended_r <sup>1</sup>	median(0,hpa2y_blended_r-95,113-95)		0.0155	0.0014	0.0000
SVhpa2yb_pw4		Variate piecewise of hpa2y_blended_r <sup>1</sup>	median(0,hpa2y_blended_r-113,120-113)		0.0617	0.0031	0.0000
SVhpa2yb_pw5		Variate piecewise of hpa2y_blended_r <sup>1</sup>	max(0,hpa2y_blended_r-120)		0.0197	0.0018	0.0000
SMycslope	L01	Categorical of yield curve slope	1<=ycslope<=2		0.3401	0.0376	0.0000
SMrfncind	LY	Categorical of rfnc_ind (refinanced loan indicator)	frst_tm_by = "Y"		-0.0278	0.0113	0.0138
SMDeltaTY10	L01	Categorical of DeltaTy10Init_r <sup>2</sup>	DeltaTy10Init_r < 53		0.2191	0.0117	0.0000



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 257

Variable	ClassVal0	Description	Description Detail	Response	Estimate	StdErr	ProbChiSq
		(change in 10-year Treasury rate from policy inception to current)					
SMDeltaTY10	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r > 130		-0.0109	0.0335	0.7442
SMDeltaTm3	L01	Categorical of DeltaTm3Init_r <sup>3</sup> (change in 3-month Treasury rate from policy inception to current)	DeltaTm3Init_r > 600		-0.1246	0.0286	0.0000
SMicredit_grp1	L450	Categorical of credit	0<credit_score<=450		-0.4361	0.1468	0.0030
SMicredit_grp2	L500	Categorical of credit	450<credit_score<=500		-0.5500	0.0641	0.0000
SMicredit_grp3	L600	Categorical of credit	500<credit_score<=600		-0.3486	0.0187	0.0000
SMicredit_grp4	L630	Categorical of credit	600<credit_score<=630		-0.1699	0.0190	0.0000
SMicredit_grp5	L680	Categorical of credit	630<credit_score<=680		0.0651	0.0174	0.0002
SMicredit_grp6	L720	Categorical of credit	680<credit_score<=720		0.3212	0.0203	0.0000
SMicredit_grp7	L745	Categorical of credit	720<credit_score<=745		0.5534	0.0271	0.0000
SMicredit_grp8	L800	Categorical of credit	745<credit_score<=800		0.7565	0.0257	0.0000
SMicredit_grp9	L850	Categorical of credit	800<credit_score		0.6637	0.0793	0.0000

### Conveyance Severity Model

The model parameters for the Conveyance severity model are shown below.

Table 67: Conveyance Severity Model Parameters

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				9.2051	0.0537	0.0000
SVbalance_i_log		Variate version of log transformed outstanding balance at start of quarter	log(balance_i/1000)	0.3201	0.0013	0.0000
SVCCI_pw1		Consumer Confidence Index	median(0,CCI-30,91)	0.0006	0.0000	0.0000
SVCCI_pw2		Consumer Confidence Index	median(0,CCI-91,142-91)	-0.0005	0.0000	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 258

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SVSBOI_pw1		Small Business Optimism Index	median(0,SBOI-80,95-80)	-0.0022	0.0001	0.0000
SVSBOI_pw2		Small Business Optimism Index	median(0,SBOI-95,110-95)	0.0011	0.0000	0.0000
SVcredit_subsidy_cohort		Credit Subsidy Cohort	SVcredit_subsidy_cohort = credit_subsidy_cohort	-0.0004	0.0000	0.0000
SMproduct	ARM	Categorical of product type	adjustable rate mortgage	0.0100	0.0005	0.0000
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance	0.0082	0.0012	0.0000
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage	-0.0270	0.0010	0.0000
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance	-0.0266	0.0020	0.0000
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance	-0.0061	0.0006	0.0000
SMproduct	z_FRM30	Categorical of product type	30 year fixed rate mortgage	0.0000	0.0000	.
SVloansize_raw_grp		Variate version of loansize_raw	min(loansize/1000,600)	0.0291	0.0001	0.0000
SMpriormod	L01	Categorical of Prior Loan Modifications	prior_mod_cnt = 0	0.0504	0.0005	0.0000
SMpriormod	L02	Categorical of Prior Loan Modifications	prior_mod_cnt = 1	0.1078	0.0009	0.0000
SMpriormod	L03	Categorical of Prior Loan Modifications	prior_mod_cnt = 2	0.1655	0.0015	0.0000
SMpriormod	Z00	Categorical of Prior Loan Modifications	prior_mod_cnt >= 3	0.0000	0.0000	.
SVpriormod_pw1		Variate piecewise version of prior_mod_cnt	median(0,prior_mod_cnt-3,15-3)	0.0430	0.0019	0.0000
SMcredit	L01	Credit Score	SMcredit = "L01"	0.0117	0.0009	0.0000
SMcredit	L02	Credit Score	SMcredit = "L02"	0.0067	0.0020	0.0009
SMcredit	Z00	Credit Score	SMcredit = "Z00"	0.0000	0.0000	.
SVcredit_pw1		Variate piecewise of Credit Score	median(0,credit_score-500,625-500)	0.0000	0.0000	0.0001
SVcredit_pw2		Variate piecewise of Credit Score	median(0,credit_score-625,680-625)	0.0000	0.0000	0.0000
SMseason	L01	Categorical of season	season = "winter"	0.0001	0.0003	0.6628
SMseason	L02	Categorical of season	season = "spring"	-0.0019	0.0003	0.0000
SMseason	L03	Categorical of season	season = "summer"	-0.0020	0.0003	0.0000
SMseason	Z04	Categorical of season	season = "fall"	0.0000	0.0000	.
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1	0.0461	0.0002	0.0000
SMjudicial	Z00	Categorical of judicial (judicial state)	base level: else	0.0000	0.0000	.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 259

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SMRatioTmpTei	L00	Categorical of ratio_tmp_teI (front-end ratio)	ratio_tmp_teI=0	0.0092	0.0008	0.0000
SMRatioTmpTei	Z01	Categorical of ratio_tmp_teI (front-end ratio)	base level: else	0.0000	0.0000	.
SVratiotmpteI_pw1		Variate piecewise version of front end ratio	median(0,ratio_tmp_teI-0,24-0)	0.0004	0.0000	0.0000
SVratiotmpteI_pw2		Variate piecewise version of front end ratio	median(0,ratio_tmp_teI-24,36-24)	0.0005	0.0000	0.0000
SVratiotmpteI_pw3		Variate piecewise version of front end ratio	median(0,ratio_tmp_teI-36,50-36)	-0.0004	0.0001	0.0000
SVsato_pw1		Variate piecewise of sato (spread at origination)	min(sato+0.1,0)	-0.0008	0.0002	0.0000
SVsato_pw2		Variate piecewise of sato (spread at origination)	median(0,sato+0.1,0.7+0.1)	0.0265	0.0004	0.0000
SVsato_pw3		Variate piecewise of sato (spread at origination)	max(0,sato-0.7)	-0.0044	0.0001	0.0000
SVhpa2yb_pw1		Variate piecewise of hpa2y_bIended_r <sup>-1</sup>	min(hpa2y_bIended_r,85)	-0.0002	0.0000	0.0000
SVhpa2yb_pw2		Variate piecewise of hpa2y_bIended_r <sup>-1</sup>	median(0,hpa2y_bIended_r-85,95-85)	-0.0006	0.0001	0.0000
SVhpa2yb_pw3		Variate piecewise of hpa2y_bIended_r <sup>-1</sup>	median(0,hpa2y_bIended_r-95,113-95)	-0.0015	0.0000	0.0000
SVhpa2yb_pw4		Variate piecewise of hpa2y_bIended_r <sup>-1</sup>	median(0,hpa2y_bIended_r-113,120-113)	0.0032	0.0001	0.0000
SVhpa2yb_pw5		Variate piecewise of hpa2y_bIended_r <sup>-1</sup>	max(0,hpa2y_bIended_r-120)	0.0006	0.0001	0.0000
SMycslope	L01	Categorical of yield curve slope	Categorical of yield curve slope	0.0071	0.0003	0.0000
SMycslope	Z00	Categorical of yield curve slope	Categorical of yield curve slope	0.0000	0.0000	.
SMrfncind	LY	Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind <> "N"	-0.0042	0.0004	0.0000
SMrfncind	ZN	Categorical of rfnc_ind (refinanced loan indicator)	base level: else	0.0000	0.0000	.
SMdurdefepi	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.0280	0.0004	0.0000
SMdurdefepi	L03	Categorical of dur_def_episode	dur_def_episode = 3	-0.0122	0.0004	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 260

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
SMdurdefepi	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	0.0039	0.0004	0.0000
SMdurdefepi	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	0.0200	0.0005	0.0000
SMdurdefepi	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	0.0338	0.0005	0.0000
SMdurdefepi	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	0.0458	0.0005	0.0000
SMdurdefepi	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	0.0565	0.0006	0.0000
SMdurdefepi	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	0.0660	0.0006	0.0000
SMdurdefepi	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	0.0760	0.0007	0.0000
SMdurdefepi	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 11	0.0812	0.0005	0.0000
SMdurdefepi	Z01	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 1	0.0000	0.0000	.
SVdurdefepi_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	0.0064	0.0001	0.0000
SVdurdefepi_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-30,40-30)	0.0033	0.0002	0.0000
SMDeltaTY10	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	0.0008	0.0004	0.0324
SMDeltaTY10	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from	DeltaTy10Init_r > 130	0.0027	0.0008	0.001

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 261

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		policy inception to current)				
SMDeltaTY10	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else	0.0000	0.0000	.
Smloansize	L01	Categorical loansize_raw	loansize_raw<32000	-0.0276	0.0007	0.0000
SMloansize	Z01	Categorical loansize_raw	loansize_raw>=32000	0.0000	0.0000	.
SVloanraw_pw1		Variate piecewise of loansize_raw	median(0,loansize_raw-32000,70000-32000)	0.0000	0.0000	0.0000
SVloanraw_pw2		Variate piecewise of loansize_raw	median(0,loansize_raw-70000,98000-70000)	0.0000	0.0000	0.0000
SVloanraw_pw3		Variate piecewise of loansize_raw	median(0,loansize_raw-98000,180000-98000)	0.0000	0.0000	0.0000
SVloanraw_pw4		Variate piecewise of loansize_raw	median(0,loansize_raw-180000,500000-180000)	0.0000	0.0000	0.0000

## Conveyance Recovery Severity Model

The model parameters for the Conveyance Recovery severity model are shown below.

Table 68: Conveyance Recovery Severity Model Parameters

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				8.0104	0.0269	0.0000
SVbalance_i_log		Variate version of log transformed outstanding balance at start of quarter	log(balance_i/1000)	0.3012	0.0070	0.0000
SVCCI_pw1		Consumer Confidence Index	median(0,CCI-30,91)	-0.0010	0.0001	0.0000
SVCCI_pw2		Consumer Confidence Index	median(0,CCI-91,142-91)	0.0007	0.0001	0.0000
SVSBOI_pw1		Small Business Optimism Index	median(0,SBOI-80,95-80)	0.0111	0.0005	0.0000
SVSBOI_pw2		Small Business Optimism Index	median(0,SBOI-95,110-95)	0.0201	0.0003	0.0000
SMproduct	ARM	Categorical of product type	adjustable rate mortgage	-0.0909	0.0028	0.0000
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance	-0.0207	0.0064	0.0012
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage	0.0296	0.0061	0.0000
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance	0.2104	0.0107	0.0000
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance	0.0371	0.0029	0.0000
SMproduct	z_FRM30	Categorical of product type	30 year fixed rate mortgage	0.0000	0.0000	.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 262

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SVloansize_raw_grp		Variate version of loansize_raw	min(loansize/1000,600)	0.0158	0.0006	0.0000
SMpriormod	L01	Categorical of Prior Loan Modifications	prior_mod_cnt = 1	-0.0379	0.0025	0.0000
SMpriormod	L02	Categorical of Prior Loan Modifications	prior_mod_cnt = 2	-0.0358	0.0047	0.0000
SMpriormod	L03	Categorical of Prior Loan Modifications	prior_mod_cnt >= 3	-0.0177	0.0083	0.0323
SMpriormod	Z00	Categorical of Prior Loan Modifications	prior_mod_cnt = 0	0.0000	0.0000	.
SVpriormod_pw1		Variate piecewise version of prior_mod_cnt	median(0,prior_mod_cnt-3,15-3)	0.0344	0.0099	0.0005
SMseason	L01	Categorical of season	season = "winter"	0.0242	0.0016	0.0000
SMseason	L02	Categorical of season	season = "spring"	0.0142	0.0017	0.0000
SMseason	L03	Categorical of season	season = "summer"	-0.0055	0.0016	0.0009
SMseason	Z04	Categorical of season	season = "fall"	0.0000	0.0000	.
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1	-0.0729	0.0013	0.0000
SMjudicial	Z00	Categorical of judicial (judicial state)	base level: else	0.0000	0.0000	.
SMdpa_govt	LGovt	Categorical of down payment assistance, government level indicator	dpa = "govt"	-0.0999	0.0044	0.0000
SMdpa_govt	ZOthr	Categorical of down payment assistance, government level indicator	base level: else	0.0000	0.0000	.
SMdpa_nprof	LNPro	Categorical of down payment assistance, non-profit level indicator	dpa = "nonprof"	-0.1566	0.0021	0.0000
SMdpa_nprof	ZOthr	Categorical of down payment assistance, non-profit level indicator	base level: else	0.0000	0.0000	.
SVsato_pw1		Spread at origination	min(sato+0.1,0)	-0.0296	0.0014	0.0000
SVsato_pw2		Spread at origination	median(0,sato+0.1,0.7+0.1)	-0.1229	0.0024	0.0000
SVsato_pw3		Spread at origination	max(0,sato-0.7)	-0.0066	0.0039	0.0858

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 263

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SVhpa2yb_pw1		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	min(hpa2y_blen ded_r,85)	-0.0054	0.0000	0.0000
SVhpa2yb_pw2		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	median(0,hpa2y_blen ded_r-85,95-85)	0.0274	0.0003	0.0000
SVhpa2yb_pw3		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	median(0,hpa2y_blen ded_r-95,113-95)	0.0149	0.0002	0.0000
SVhpa2yb_pw4		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	median(0,hpa2y_blen ded_r-113,120-113)	0.0093	0.0004	0.0000
SVhpa2yb_pw5		Variate piecewise of hpa2y_blen ded_r <sup>-1</sup>	max(0,hpa2y_blen ded_r-120)	0.0101	0.0003	0.0000
SMrfncind	LY	Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind <> "N"	-0.2015	0.0023	0.0000
SMrfncind	ZN	Categorical of rfnc_ind (refinanced loan indicator)	base level: else	0.0000	0.0000	.
SMdurdefepi	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	0.0103	0.0033	0.0016
SMdurdefepi	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	0.0061	0.0031	0.0477
SMdurdefepi	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-0.0104	0.0031	0.0009
SMdurdefepi	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	-0.0182	0.0032	0.0000
SMdurdefepi	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	-0.0279	0.0033	0.0000
SMdurdefepi	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	-0.0339	0.0035	0.0000
SMdurdefepi	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	-0.0357	0.0037	0.0000
SMdurdefepi	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	-0.0331	0.0039	0.0000
SMdurdefepi	L10	Categorical of dur_def_episode	dur_def_episode = 10	-0.0353	0.0041	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 264

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
SMdurdefepi	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 11	-0.0403	0.0035	0.0000
SMdurdefepi	Z01	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 1	0.0000	0.0000	.
SVdurdefepi_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	0.0023	0.0003	0.0000
SVdurdefepi_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	0.0134	0.0012	0.0000
SMDeltaTY10	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	-0.1235	0.0020	0.0000
SMDeltaTY10	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r > 130	-0.0124	0.0069	0.072
SMDeltaTY10	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else	0.0000	0.0000	.
SMDeltaTm3	L01	Categorical of DeltaTm3Init_r <sup>3</sup> (change in 3-month Treasury rate from policy inception to current)	DeltaTm3Init_r > 600	-0.0534	0.0046	0.0000
SMDeltaTm3	Z00	Categorical of DeltaTm3Init_r <sup>3</sup> (change in 3-month Treasury rate from policy inception to current)	base level: else	0.0000	0.0000	.
SMcredit	L01	Credit Score	credit_score = 0	0.1878	0.0047	0.0000
SMcredit	L02	Credit Score	credit_score < 500	0.0095	0.0108	0.3794
SMcredit	Z00	Credit Score	credit_score >= 500	0.0000	0.0000	.
SVcredit_pw1		Variate piecewise of Credit Score	median(0,credit_score-500,625-500)	0.0000	0.0000	0.4151



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 265

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SVcredit_pw2		Variate piecewise of Credit Score	median(0,credit_score-625,680-625)	0.0005	0.0001	0.0000
SMloansize	L01	Categorical loansize_raw	loansize_raw<32000	-0.2417	0.0050	0.0000
SMloansize	Z01	Categorical loansize_raw	loansize_raw>=32000	0.0000	0.0000	.
SVloanraw_pw1		Loan amount	median(0,loansize_raw-32000,70000-32000)	0.0000	0.0000	0.0000
SVloanraw_pw2		Loan amount	median(0,loansize_raw-70000,98000-70000)	0.0000	0.0000	0.0000
SVloanraw_pw3		Loan amount	median(0,loansize_raw-98000,180000-98000)	0.0000	0.0000	0.0000
SVloanraw_pw4		Loan amount	median(0,loansize_raw-180000,500000-180000)	0.0000	0.0000	0.0000

### Third Party Sales Severity Model

The model parameters for the Third Party Sales severity model are shown below.

Table 69: Third Party Sales Severity Model Parameters

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				8.0119	0.0502	0.0000
SVbalance_i_log		Variate version of log transformed outstanding balance at start of quarter	log(balance_i/1000)	0.6494	0.0041	0.0000
SVSBOI_pw1		Small Business Optimism Index	median(0,SBOI-80,95-80)	-0.0242	0.0027	0.0000
SVSBOI_pw2		Small Business Optimism Index	median(0,SBOI-95,110-95)	-0.0097	0.0006	0.0000
SMproduct	ARM	Categorical of product type	adjustable rate mortgage	0.0667	0.0177	0.0002
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance	0.0820	0.0253	0.0012
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage	-0.0359	0.0223	0.1076
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance	0.0214	0.0471	0.6487
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance	0.0217	0.0111	0.0504
SMproduct	z_FRM30	Categorical of product type	30 year fixed rate mortgage	0.0000	0.0000	.
SMpriormod	L01	Categorical of Prior Loan Modifications	prior_mod_cnt = 1	0.0908	0.0057	0.0000
SMpriormod	L02	Categorical of Prior Loan Modifications	prior_mod_cnt = 2	0.1797	0.0091	0.0000
SMpriormod	L03	Categorical of Prior Loan Modifications	prior_mod_cnt >= 3	0.3107	0.0120	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 266

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SMpriormod	Z00	Categorical of Prior Loan Modifications	prior_mod_cnt = 0	0.0000	0.0000	.
SMseason	L01	Categorical of season	season = "winter"	0.0101	0.0062	0.1005
SMseason	L02	Categorical of season	season = "spring"	-0.0112	0.0060	0.0606
SMseason	L03	Categorical of season	season = "summer"	-0.0042	0.0059	0.4756
SMseason	Z04	Categorical of season	season = "fall"	0.0000	0.0000	.
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1	0.2184	0.0048	0.0000
SMjudicial	Z00	Categorical of judicial (judicial state)	base level: else	0.0000	0.0000	.
SMRatioTmpTei	L00	Categorical of ratio_tmp_te_i (front-end ratio)	ratio_tmp_te_i=0	-0.0563	0.0184	0.0023
SMRatioTmpTei	Z01	Categorical of ratio_tmp_te_i (front-end ratio)	base level: else	0.0000	0.0000	.
SVratiotmpte_i_pw1		Variate piecewise version of front end ratio	median(0,ratio_tmp_te_i-0,24-0)	-0.0027	0.0008	0.0004
SVratiotmpte_i_pw2		Variate piecewise version of front end ratio	median(0,ratio_tmp_te_i-24,36-24)	-0.0015	0.0007	0.036
SVratiotmpte_i_pw3		Variate piecewise version of front end ratio	median(0,ratio_tmp_te_i-36,50-36)	-0.0047	0.0013	0.0003
SVsato_pw1		Variate piecewise of sato (spread at origination)	min(sato+0.1,0)	0.0294	0.0100	0.0034
SVsato_pw2		Variate piecewise of sato (spread at origination)	median(0,sato+0.1,0.7+0.1)	0.0841	0.0087	0.0000
SVsato_pw3		Variate piecewise of sato (spread at origination)	max(0,sato-0.7)	0.1076	0.0163	0.0000
SVhpa2yb_pw1		Variate piecewise of hpa2y_blen_ded_r <sup>-1</sup>	min(hpa2y_blen_ded_r,85)	0.0058	0.0006	0.0000
SVhpa2yb_pw2		Variate piecewise of hpa2y_blen_ded_r <sup>-1</sup>	median(0,hpa2y_blen_ded_r-85,95-85)	-0.0099	0.0047	0.0364
SVhpa2yb_pw3		Variate piecewise of hpa2y_blen_ded_r <sup>-1</sup>	median(0,hpa2y_blen_ded_r-95,113-95)	-0.0258	0.0008	0.0000
SVhpa2yb_pw4		Variate piecewise of hpa2y_blen_ded_r <sup>-1</sup>	median(0,hpa2y_blen_ded_r-113,120-113)	-0.0216	0.0012	0.0000
SVhpa2yb_pw5		Variate piecewise of hpa2y_blen_ded_r <sup>-1</sup>	max(0,hpa2y_blen_ded_r-120)	0.0040	0.0010	0.0000
SMrfncind	LY	Categorical of rfnc_ind	rfnc_ind <> "N"	0.1694	0.0059	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 267

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(refinanced loan indicator)				
SMrfncind	ZN	Categorical of rfn_ind (refinanced loan indicator)	base level: else	0.0000	0.0000	.
SMdurdefepi	L02	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 2	-0.1530	0.0128	0.0000
SMdurdefepi	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	-0.0984	0.0125	0.0000
SMdurdefepi	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	-0.0385	0.0123	0.0017
SMdurdefepi	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	0.0063	0.0124	0.6103
SMdurdefepi	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	0.0772	0.0128	0.0000
SMdurdefepi	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	0.0900	0.0132	0.0000
SMdurdefepi	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	0.1387	0.0138	0.0000
SMdurdefepi	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	0.1731	0.0142	0.0000
SMdurdefepi	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	0.2125	0.0149	0.0000
SMdurdefepi	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 11	0.2199	0.0124	0.0000
SMdurdefepi	Z01	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 1	0.0000	0.0000	.
SVdurdefepi_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	0.0243	0.0007	0.0000
SVdurdefepi_pw2		Variate piecewise of dur_def_episode	median(0,dur_def_episode-30,40-30)	0.0067	0.0027	0.0137

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 268

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
SMDeltaTm3	L01	Categorical of DeltaTm3Init_r <sup>2</sup> (change in 3-month Treasury rate from policy inception to current)	DeltaTm3Init_r > 600	-0.1704	0.0060	0.0000
SMDeltaTm3	Z00	Categorical of DeltaTm3Init_r <sup>2</sup> (change in 3-month Treasury rate from policy inception to current)	base level: else	0.0000	0.0000	.

### Pre-Foreclosure Sale Severity Model

The model parameters for the Pre-Foreclosure Sale severity model are shown below.

Table 70: Pre-Foreclosure Sale Severity Model

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
Intercept				7.0319	0.0535	0.0000
SVbalance_i_log		Variate version of log transformed outstanding balance at start of quarter	log(balance_i/1000)	0.8103	0.0040	0.0000
SMproduct	ARM	Categorical of product type	adjustable rate mortgage	-0.0243	0.0084	0.004
SMproduct	ARMSR	Categorical of product type	adjustable rate mortgage - streamline refinance	0.1222	0.0134	0.0000
SMproduct	FRM15	Categorical of product type	15 year fixed rate mortgage	-0.0838	0.0253	0.0009
SMproduct	FRM15SR	Categorical of product type	15 year fixed rate mortgage - streamline refinance	0.0852	0.0428	0.0465
SMproduct	FRM30SR	Categorical of product type	30 year fixed rate mortgage - streamline refinance	0.1701	0.0066	0.0000
SMproduct	z_FRM30	Categorical of product type	30 year fixed rate mortgage	0.0000	0.0000	.
SMseason	L01	Categorical of season	season = "winter"	0.0106	0.0050	0.0343
SMseason	L02	Categorical of season	season = "spring"	-0.0206	0.0047	0.0000
SMseason	L03	Categorical of season	season = "summer"	-0.0100	0.0048	0.037
SMseason	Z04	Categorical of season	season = "fall"	0.0000	0.0000	.
SMjudicial	L01	Categorical of judicial (judicial state)	judicial = 1	0.0340	0.0037	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 269

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SMjudicial	Z00	Categorical of judicial (judicial state)	base level: else	0.0000	0.0000	.
SMdpa_govt	LGovt	Categorical of down payment assistance, government level indicator	dpa = "govt"	0.0606	0.0142	0.0000
SMdpa_govt	ZOthr	Categorical of down payment assistance, government level indicator	base level: else	0.0000	0.0000	.
SMdpa_nprof	LNPro	Categorical of down payment assistance, non-profit level indicator	dpa = "nonprof"	0.1383	0.0056	0.0000
SMdpa_nprof	ZOthr	Categorical of down payment assistance, non-profit level indicator	base level: else	0.0000	0.0000	.
SVhpa2yb_pw1		Variate piecewise of hpa2y_bledned_r <sup>-1</sup>	min(hpa2y_bledned_r,85)	-0.0004	0.0006	0.5094
SVhpa2yb_pw2		Variate piecewise of hpa2y_bledned_r <sup>-1</sup>	median(0,hpa2y_bledned_r-85,95-85)	-0.0272	0.0008	0.0000
SVhpa2yb_pw3		Variate piecewise of hpa2y_bledned_r <sup>-1</sup>	median(0,hpa2y_bledned_r-95,113-95)	-0.0151	0.0004	0.0000
SVhpa2yb_pw4		Variate piecewise of hpa2y_bledned_r <sup>-1</sup>	median(0,hpa2y_bledned_r-113,120-113)	0.0100	0.0011	0.0000
SVhpa2yb_pw5		Variate piecewise of hpa2y_bledned_r <sup>-1</sup>	max(0,hpa2y_bledned_r-120)	0.0012	0.0006	0.0594
SMycslope	L01	Categorical of yield curve slope	Categorical of yield curve slope	-0.2004	0.0050	0.0000
SMycslope	Z00	Categorical of yield curve slope	Categorical of yield curve slope	0.0000	0.0000	.
SMfrst_tm_by	1	Categorical of frst_tm_by (first-time buyer)	frst_tm_by = "Y"	0.0669	0.0052	0.0000
SMfrst_tm_by	2	Categorical of frst_tm_by (first-time buyer)	base level: else	0.0000	0.0000	.
SMrfncind	LY	Categorical of rfnc_ind (refinanced loan indicator)	rfnc_ind <> "N"	0.2295	0.0064	0.0000
SMrfncind	ZN	Categorical of rfnc_ind (refinanced loan indicator)	base level: else	0.0000	0.0000	.
SMdurdefepi	L02	Categorical of dur_def_episode	dur_def_episode = 2	0.1065	0.0054	0.0000

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 270

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
		(duration of default episode)				
SMdurdefepi	L03	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 3	0.1929	0.0057	0.0000
SMdurdefepi	L04	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 4	0.2572	0.0063	0.0000
SMdurdefepi	L05	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 5	0.3344	0.0073	0.0000
SMdurdefepi	L06	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 6	0.3951	0.0081	0.0000
SMdurdefepi	L07	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 7	0.4495	0.0092	0.0000
SMdurdefepi	L08	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 8	0.4780	0.0103	0.0000
SMdurdefepi	L09	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 9	0.5271	0.0116	0.0000
SMdurdefepi	L10	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 10	0.5792	0.0129	0.0000
SMdurdefepi	L11	Categorical of dur_def_episode (duration of default episode)	dur_def_episode >= 11	0.6112	0.0104	0.0000
SMdurdefepi	Z01	Categorical of dur_def_episode (duration of default episode)	dur_def_episode = 1	0.0000	0.0000	.
SVdurdefepi_pw1		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-10,30-10)	0.0258	0.0015	0.0000
SVdurdefepi_pw2		Variate piecewise of dur_def_episode (duration of default episode)	median(0,dur_def_episode-30,40-30)	-0.0186	0.0085	0.0294
SMDeltaTY10	L01	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r < 53	0.2684	0.0047	0.0000

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 271

Parameter	Level1	Description	Description Detail	Estimate	StdErr	ProbChiSq
SMDeltaTY10	L02	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	DeltaTy10Init_r > 130	-0.0451	0.0122	0.0002
SMDeltaTY10	Z00	Categorical of DeltaTy10Init_r <sup>2</sup> (change in 10-year Treasury rate from policy inception to current)	base level: else	0.0000	0.0000	.
SMcredit	L01	Credit Score	credit_score = 0	-0.2430	0.0128	0.0000
SMcredit	L02	Credit Score	credit_score < 500	-0.0099	0.0302	0.7417
SMcredit	Z00	Credit Score	credit_score ≥ 500	0.0000	0.0000	.
SVcredit_pw1		Variate piecewise of Credit Score	median(0, credit_score - 500, 625 - 500)	-0.0007	0.0001	0.0000
SVcredit_pw2		Variate piecewise of Credit Score	median(0, credit_score - 625, 680 - 625)	-0.0008	0.0001	0.0000

## Model Validation

Model validation was accomplished by applying the models developed using the training set to the validation dataset. The application of the models to the validation data produces the probability of each type of claim settlement type and a predicted net loss. The actual target variable is then compared to the predicted target variable to ensure the model fits the claim settlement process and net loss process without over-fitting the actual data.

Specifically, for the loss settlement models, for the final loss settlement type we calculate the predicted probability of the settlement type. The actual settlement type is 1 for the final type of claim and 0 for all other claim types. The probability of each claim type for each record in the validation dataset is derived from the model parameters. The sum of all predicted claim type probabilities is 1 for each record.

For the net loss severity models, we calculate a predicted net loss. We also summarize the actual net loss for each claim. The predicted loss severity for each record in the validation dataset is derived from the model parameters.

Decile charts are then created for each final claim type selection and each net loss. All records are sorted, or ranked, in ascending order by the predicted value. Ten equal-sized decile groups are created with 10% of the records in each group. The sum of the actual probability and the sum of the predicted probability for each claim type within each decile is calculated for the claim type models. The sum of the actual net loss and the sum of the predicted net loss within each decile is calculated for the loss severity models. The actual and predicted numbers are then compared for consistency. The objective of a model is to have a significant spread in predicted values while maintaining a close relationship between the resulting actual and predicted values.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 272

## Loss Mitigation Model

The validation charts for the loss mitigation models are shown below.

Figure 48: Loss Mitigation Binomial Model Validation

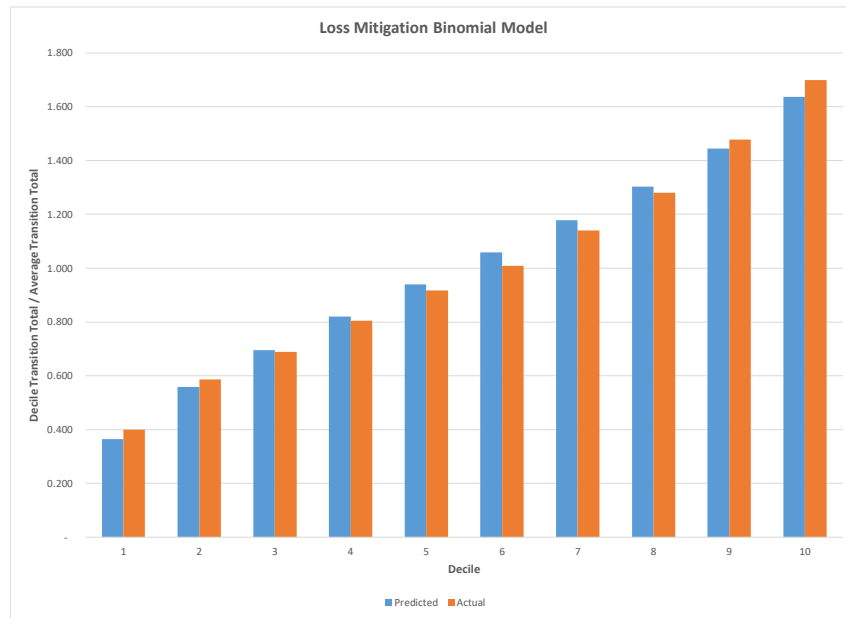
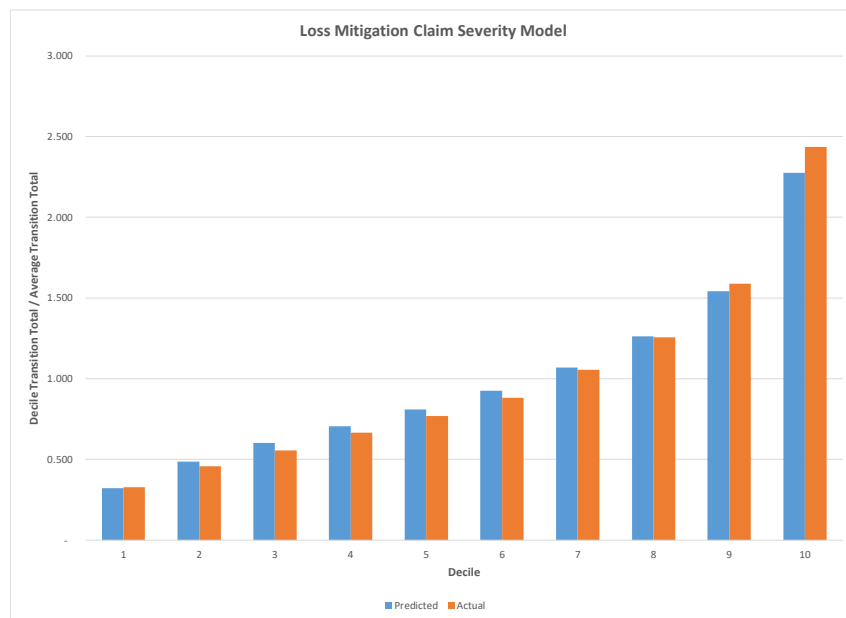


Figure 49: Loss Mitigation Claim Severity Model Validation



## Claim Type Model

The validation charts for the Claim Type model are shown below.



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 273

Figure 50: Conveyance Claim Type Model Validation Chart

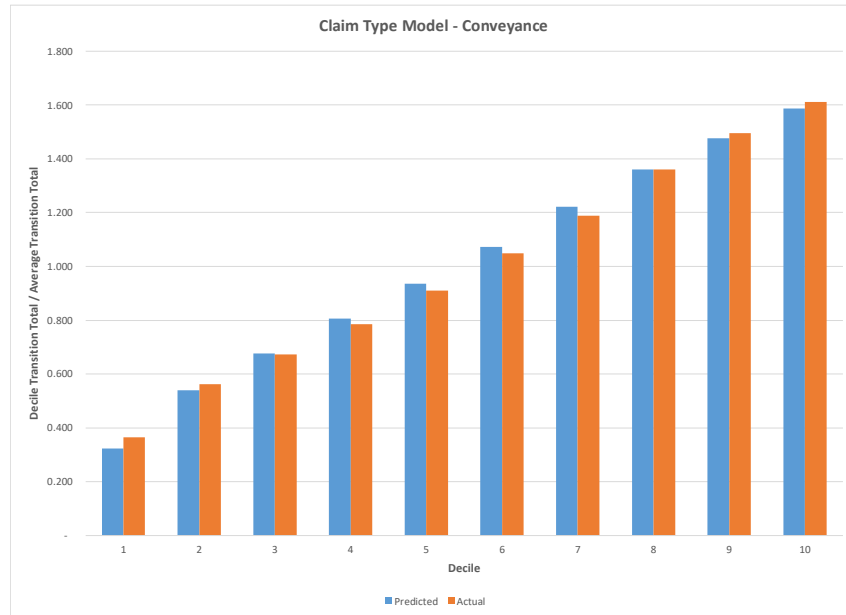
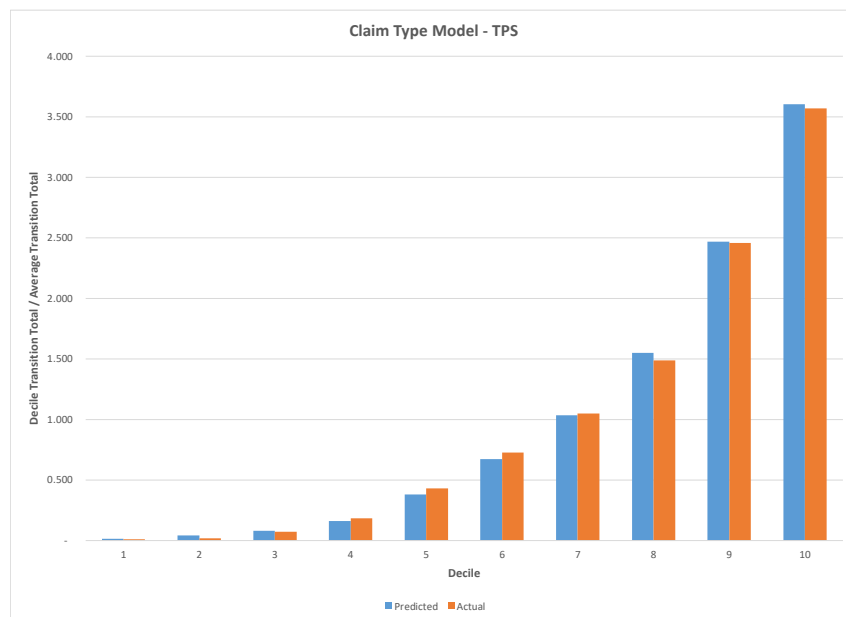


Figure 51: TPS Claim Type Model Validation Chart

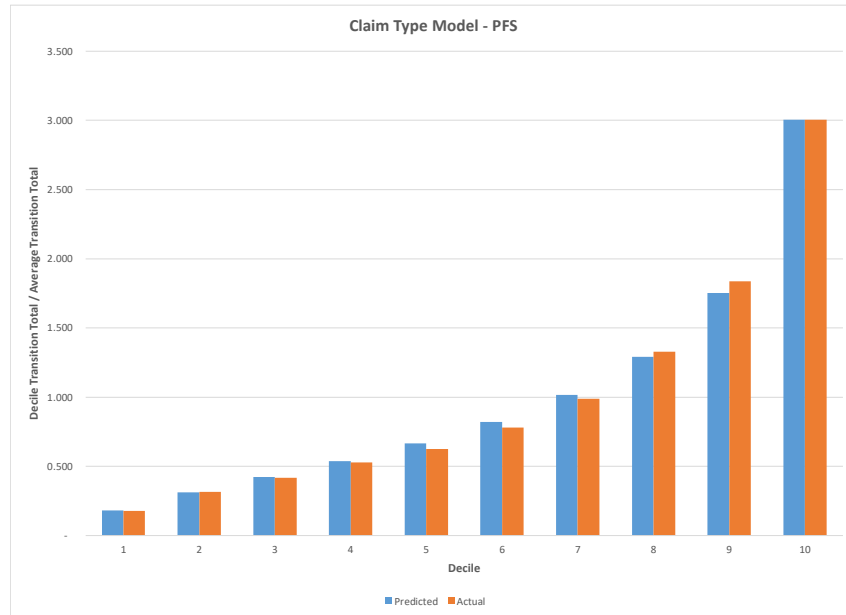


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 274

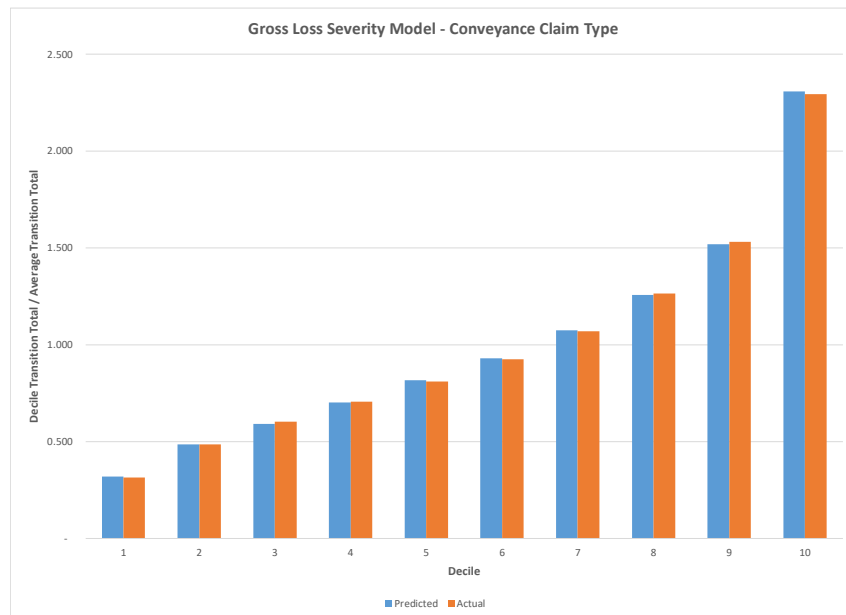
Figure 52: PFS Claim Type Model Validation Chart



## Claim Type Severity Models

The validation charts for the Claim Type Severity Models are shown below.

Figure 53: Conveyance Loss Severity Model Validation



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 275

Figure 54: Conveyance Recovery Loss Severity Model Validation

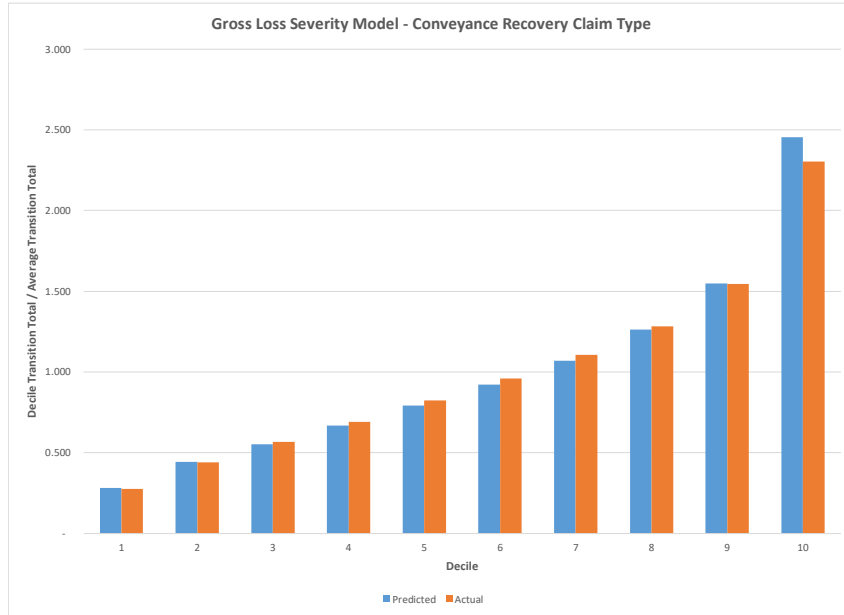
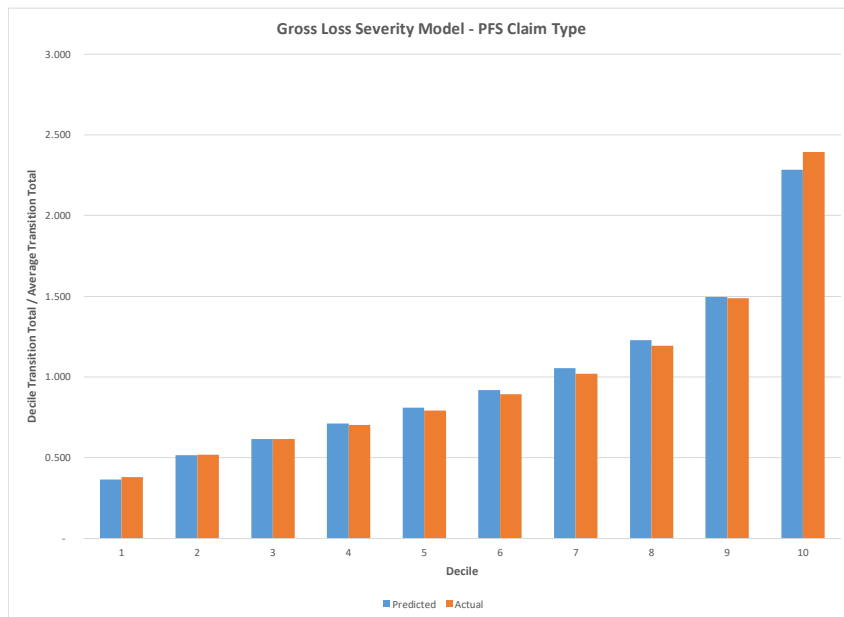


Figure 55: PFS Loss Severity Model Validation

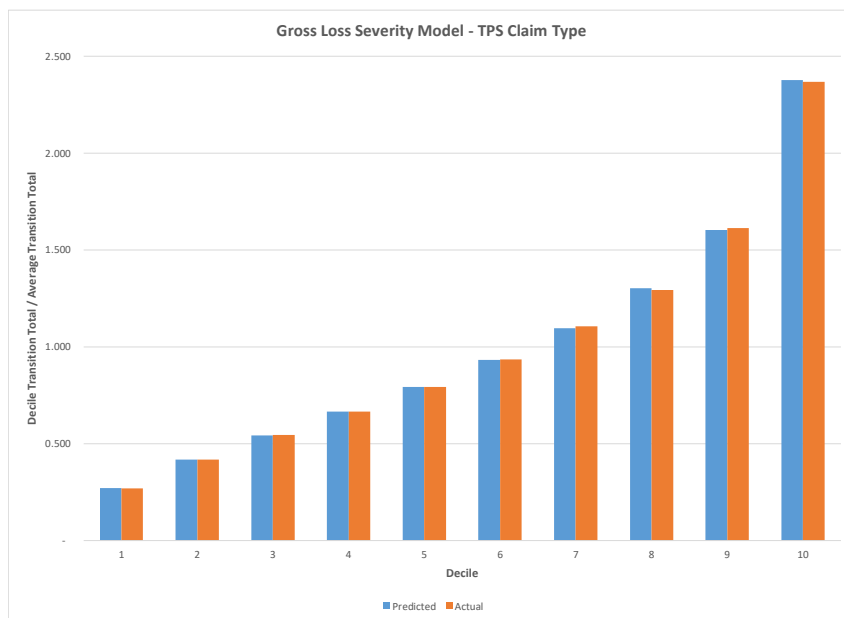


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 276

Figure 56: TPS Loss Severity Model Validation



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 277

### Appendix D: Economic Scenarios

---

To measure the possible variation in MMI's Cash Flow NPV on the existing portfolio, we developed a baseline projection using OMB Economic Assumptions and also projections for ten additional deterministic economic scenarios from Moody's. For this analysis, we used the Moody's October 2020 forecast of the U.S. economy. For purposes of our analysis, the components of Moody's forecast include:

- HPI at the MSA, state, regional and national levels
- One-year CMT rate
- Three-year CMT rate
- Five-year CMT rate
- 10-year CMT rate
- 30-year CMT rate
- Commitment rate on 30-year fixed-rate mortgages
- Unemployment rates at the MSA, state, regional and national levels
- GDP

#### Alternative Scenarios

To assess the effect of alternative economic scenarios on the Cash Flow NPV, ten alternative scenarios from Moody's were used. The ten Moody's scenarios are:

- Baseline
- Alternative 0 – Upside (4<sup>th</sup> Percentile)
- Alternative 1 – Upside (10<sup>th</sup> Percentile)
- Alternative 2 – Downside (75<sup>th</sup> Percentile)
- Alternative 3 – Downside (90<sup>th</sup> Percentile)
- Alternative 4 – Downside (96<sup>th</sup> Percentile)
- Slower Trend Growth
- Stagflation
- Next-Cycle Recession
- Low Oil Price

The Moody's projections provide a range of better than expected economic assumptions and worse than expected economic assumptions. This range of assumptions produces a range of Cash Flow NPV projections.

#### Graphical Depiction of the Scenarios

Figure 57 shows the future movements of the HPI under the baseline and the alternative economic scenarios. In the Baseline scenario, the HPI is flat through the third quarter of 2021, and then increases over the remainder of the projection period. The rate of increase is just under 5% per year through 2029, and then decreases to about 3% per year for the remainder of the projection period

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 278

Figure 57: Paths of the Future National House Price Index in Different Scenarios

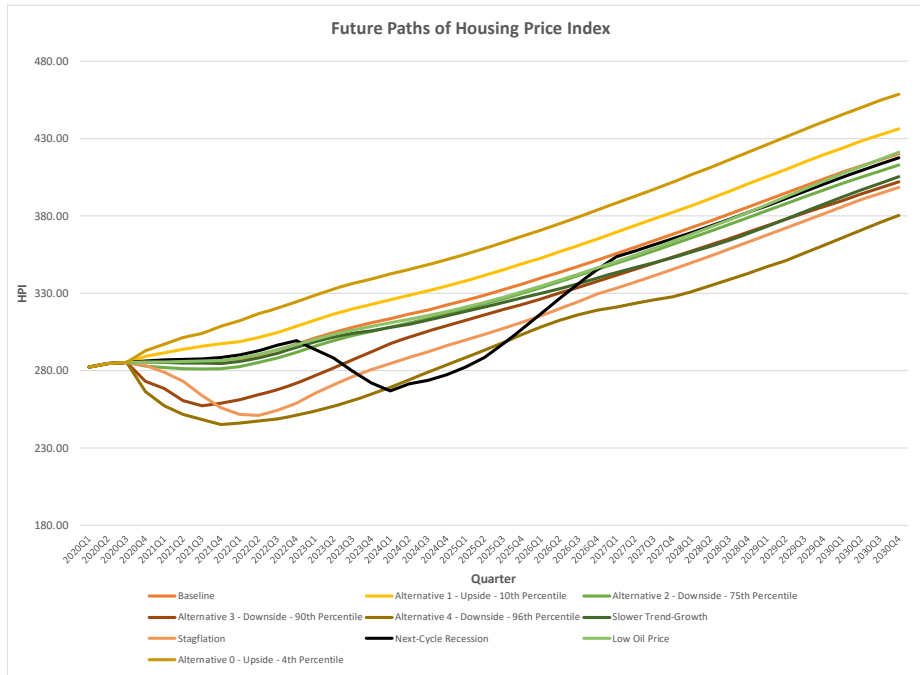


Figure 58 shows the forecasted mortgage rate of 30-year fixed-rate mortgages for the ten Moody’s scenarios. For the Moody’s Baseline Scenario, the mortgage interest rate decreases to about 3% through the second quarter of 2021 and then increases through 2028. The mortgage rate levels off at approximately 5.5% by 2029.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 279

Figure 58: Paths of the Future Mortgage Rate

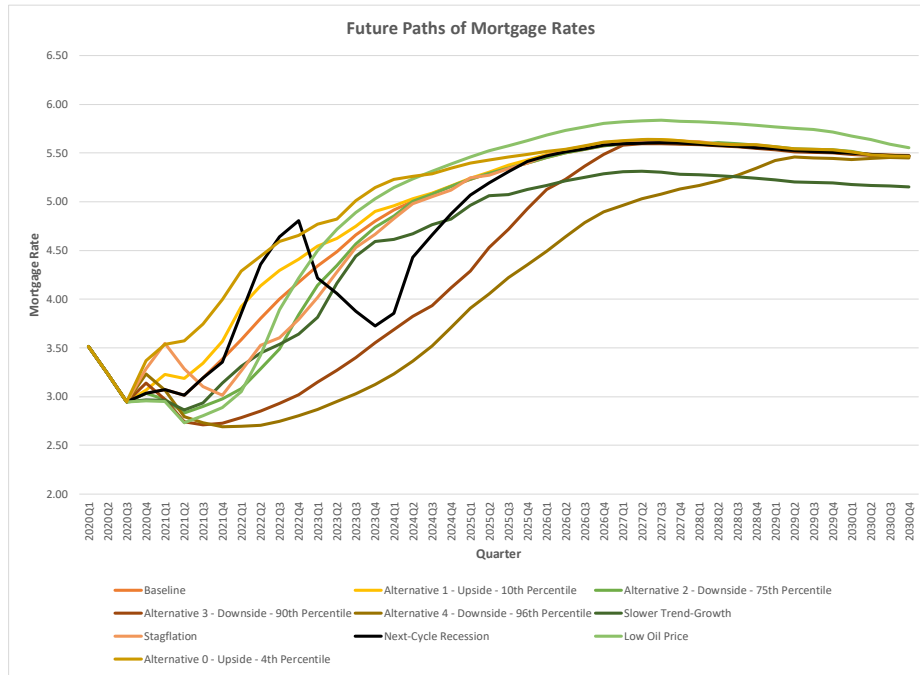


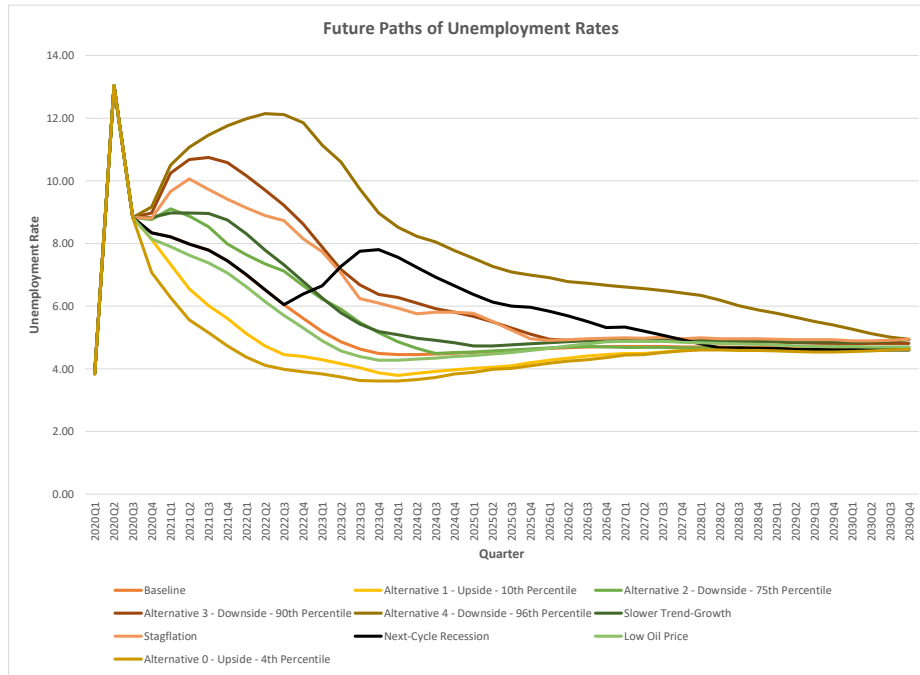
Figure 59 shows the forecasted unemployment rate under alternative economic scenarios. Under the Moody’s Baseline forecast, the unemployment rate is projected to decrease through 2023 to approximately 4.5%, and then remains steady at that level for the remainder of the projection period. Under this scenario, it is projected that it will take approximately three years for unemployment to fully return to more stable levels, and it is projected to stabilize at a level higher than pre-COVID-19 unemployment levels.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 280

Figure 59: Paths of Future National Unemployment Rate



## Stochastic Simulation

This section describes the stochastic models fitted to generate the economic variables simulations used in the projection of Cash Flow NPV.

The economic variables modeled herein as stochastic for computing expected present values include:

- Six-month CMT rates
- 10-year CMT rates
- One-year CMT Rates
- 30-year CMT rates
- 30-year FRM rates
- FHFA national purchase only house price index (HPI-PO)
- Unemployment rates
- Gross domestic product (GDP)
- Small business normalized optimism index (NOI)
- Consumer confidence index (CCI)

## Historical Data

### A. Interest Rates

Figure 60 shows historical interest rates since 1971.



# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 281

This graph illustrates the variability of interest rates over time and the consistent spread between rates. Shown are the one year CMT rate (tr1y), 10-year CMT rate (tr10y) and the 30-year FRM rate (mr).

High inflation rates caused by the global oil crisis in the late 1970's were the major factor for the historically high level in early 1980's. The Federal Reserve shifted its monetary policy from managing interest rates to managing the money supply as a way to influence interest rates after this period of time. The tr1y was around 5% in Calendar Year 1971 and increased steadily to its peak of 16.31% in Calendar Year 1981 Quarter 3. After that, it followed a decreasing trend and reached an all-time low of 0.10% in Calendar Year 2014 Quarter 2. Since then rates had started a slow upward trend until recently, where there is a sharp downward trend as a result of the COVID-19 pandemic.

Figure 60: Historical Interest Rates (%)



Figure 61 shows historical interest rate spreads, including the spread between 10-year and one-year CMT rates

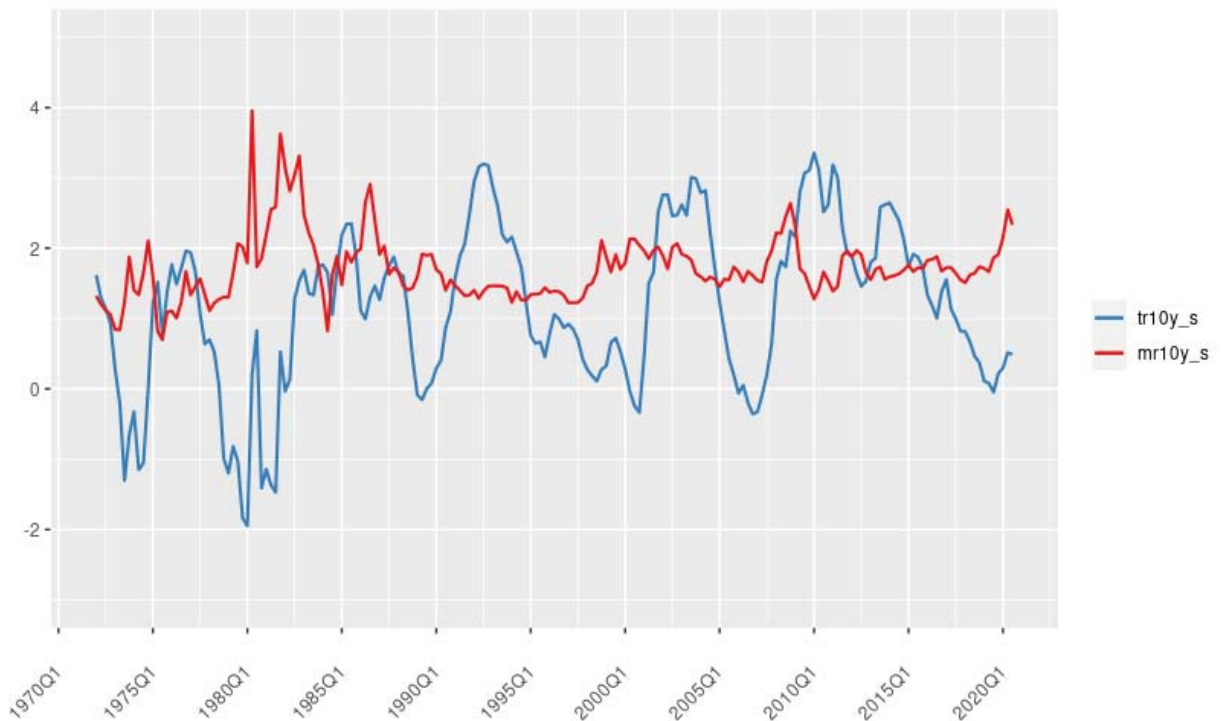
# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 282

(tr10y\_s) and the spread between the 30-year mortgage rate and the 10-year Treasury rate (mr10y\_s). Both spreads are primarily positive with long cycles. Lower and negative spreads typically correspond with economic downturns, as was seen during the late 1970's through early 1980's. Also note, the spread of the mortgage rate over the 10-year CMT rate is always positive, reflecting the premium for credit risk.

Figure 61: Historical Interest Rate Spreads (%)



## B. House Price Appreciation Rates

The national HPA rate is derived from the FHFA repeat sales house price indexes (HPIs) of purchase-only (PO) transactions. The PO HPI provides a reliable measure of housing market conditions, since it is based on repeat sales at market prices and does not use any appraised values.

The HPA series being modeled is defined as:

$$HPA_t = \ln\left(\frac{HPI_t}{HPI_{t-1}}\right) \quad (1)$$

Figure 62 shows the national quarterly HPA from Calendar Year 1991 Quarter 1 to Calendar Year 2020 Quarter 2. The long-term average quarterly HPA is around 0.87% (3.30% annual rate).

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 283

Figure 62: Historical National Quarterly HPA



The HPA increased steadily before 2004, and the quarterly appreciation rate was around 1.14%. Then house prices rose sharply starting in 2004. The average quarterly house price appreciation rate was 1.88% during the subprime mortgage expansion period from 2004 to 2006, and reached its peak of 2.59% in Calendar Year 2005 Quarter 2. After 2006, the average growth rate of house prices became negative until 2011 when appreciation returns to a positive value. Following an almost eight quarter period of a nearly flat appreciation rate, the last two quarters showed an sharp decrease to nearly 0% appreciation, again, resulting from the economic shock COVID-19 has created.

Table 71 shows the quarterly HPA by selected historical time-periods.

Table 71: Average Quarterly HPA by Time Span

Period	Average Quarterly HPA
1991 – 2003	1.13%
2004 – 2006	1.87%
2007 – 2010	-1.23%
2011 – 2020-Q3	1.12%

**C. Confidence Indices**

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 284

The Small Business Normalized Optimism Index (NOI) and Consumer Confidence Index (CCI) are confidence indices based on surveys conducted throughout the year by The Conference Board. These indexes are designed to provide a relative measure of how optimistic or pessimistic consumers and small business are regarding their expected financial situation. Both indices are based around 100 points where indicators above 100 signal relative optimism for the future of the economy, values below 100, relative pessimism. Figure 63 and Figure 64 graph CCI and NOI, with noted sharp drops in confidence associated to the 2008 mortgage crisis and the recent COVID-19 pandemic.

Figure 63: Consumer Confidence Index

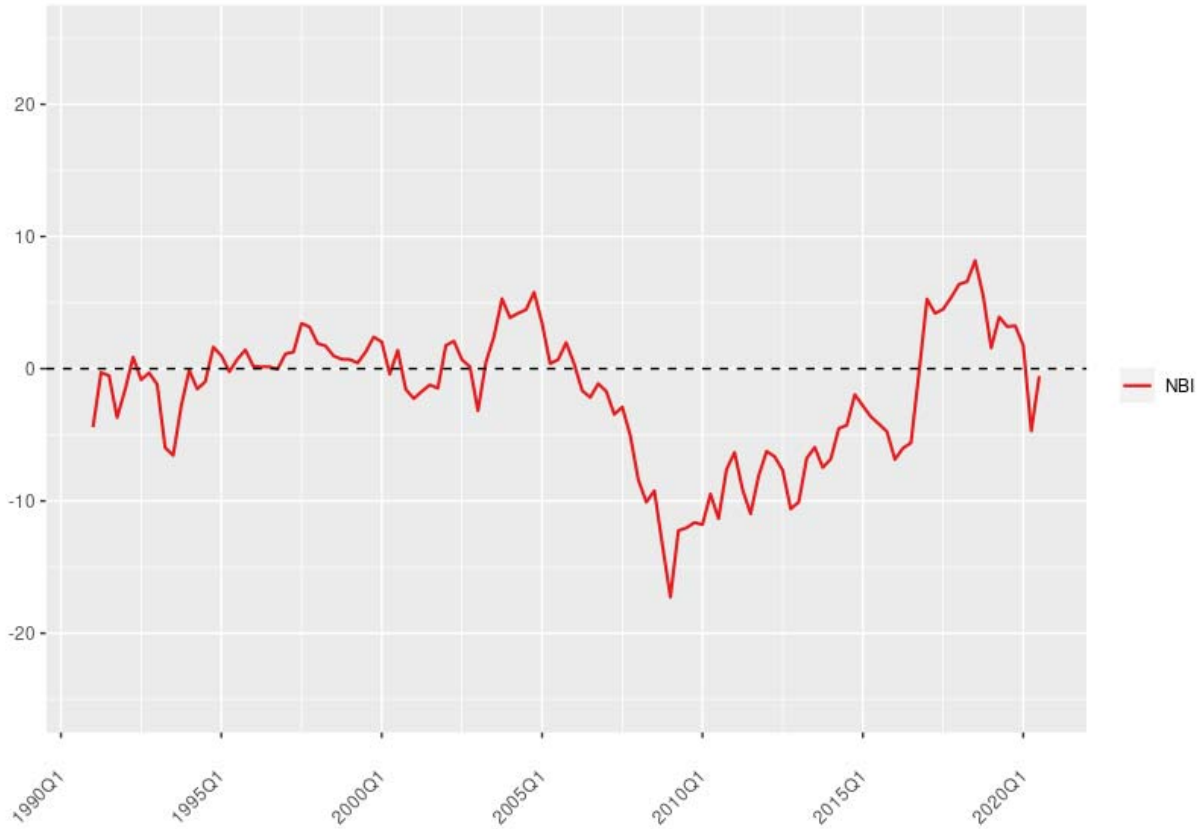


# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 285

Figure 64: Small Business Normalized Optimism Index



## Modeling Method

In financial econometrics, predicting the dependence in the co-movements of these series is important when simulating a set of economic factors. This is illustrated in Figure 60, where interest rates track closely.

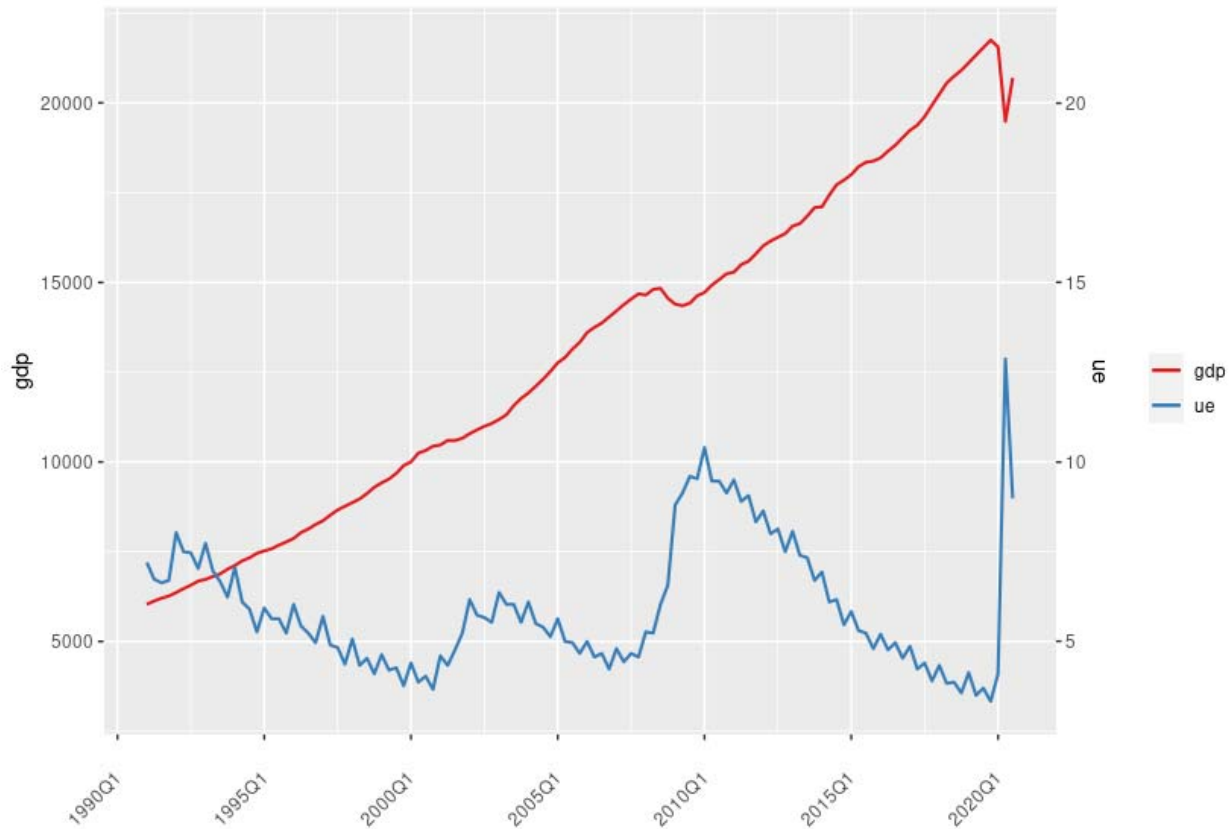
Long periods of high unemployment will lead to lower GDP. In Figure 65, we can see two obvious examples of this following the mortgage crisis in 2008 and again with the recent COVID-19 pandemic.

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 286

Figure 65: Unemployment vs. GDP



Volatilities will also move together across these series. High levels of economic instability and uncertainty will lead to volatility in these measures, affecting all economic indicators. A modeling method that accounts for these factors will lead to models that are more predictive.

Recognizing and accounting for these features through a multivariate model should lead to more accurate empirical models than working with separate univariate models.

For these reasons a multivariate General Auto Regressive Conditional Heteroscedasticity (GARCH) modeling approach was chosen.

Univariate GARCH models are typically specified as  $GARCH(p,q)$  where  $p$  is the auto regressive (AR) component of  $\sigma_t^2$ , and  $q$  is the auto regressive component of the error term. Multivariate GARCH models are defined similarly to a standard GARCH model, where the univariate term is replaced with a vector of terms. Mezrich (1995) and Shephard (1996) provide a more detailed explanation of these models.

There are a number of implementations of multivariate GARCH models. One such implementation, Dynamic Conditional Correlation (DCC) estimators, have the flexibility of univariate GARCH but avoid the complexity of conventional multivariate GARCH algorithms. Engle and Sheppard (2000) detail descriptions and examples of

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 287

using a DCC models for time series analysis.

The ‘rmgarch’ package implemented with the Cran-R project was specifically used for this modeling effort, developed by Ghalanos (2019), and based off the methods described by Engle (2000).

## Data Transformation

The algorithms required to calculate maximum likelihood estimates in these families of models are prone to non-convergence. Variable scale, stationarity of the variables, and covariance within the variable vector set are often the underlying issue when dealing with non-convergence in these complex matrix calculations. Data transformation was performed on these variables to provide a more robust and consistent estimate.

Dickey-Fuller stationarity tests were performed on all variables. GDP and HPA test as non-stationary. As a result, first difference transformations were applied to all variables to provide stationarity. Further scaling was required for index variables (*Ind*) using a log transformation:

$$Ind_{trans} = \ln(Ind + \sqrt{Ind^2 + 1}) \quad (1)$$

Table 72 below provides a description of each variable transformation.

## Model Specifications

Each variable is provided a univariate type specification, in a standard (p,q) format where p,q for the ARMA (mean) specification describes the number of autoregressive and moving average lags to include in the model, and (p,q) for the GARCH specification correspond to the autoregressive components and heteroskedastic components (auto regressive component of error term) respectively. See Table 72 for each variable specification.

Table 72: Model Variable Transformations and specifications

VARIABLE	VARIABLE TRANSFORMATION	ARMA(P,Q)	GARCH(P,Q)	DISTRIBUTION
6-MONTH	First difference	(0,1)	(1,1)	Normal
1-YEAR	First difference	(1,0)	(1,1)	Normal
10-YEAR	First difference	(1,0)	(1,1)	Normal
30-YEAR	First difference	(1,0)	(1,1)	Normal
30-YEAR FRM	First difference	(1,0)	(1,1)	Normal
UNEMPLOYMENT	First difference	(0,0)	(1,1)	Normal

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 288

VARIABLE	VARIABLE TRANSFORMATION	ARMA(P,Q)	GARCH(P,Q)	DISTRIBUTION
<b>GDP</b>	First difference, log function transformation	(1,1)	(1,1)	Skewed generalized error
<b>HPI</b>	First difference, log function transformation	(1,1)	(1,0)	Skewed student-t
<b>NOI</b>	First difference, log function transformation	(0,0)	(0,1)	Normal
<b>CCI</b>	First difference, log function transformation	(0,0)	(0,1)	Normal

When fitting a DCC model, the dynamic correlation is fitted with an autoregressive parameter that is applied across all variables. This was set with a (p,q) value of (1,1), describing the correlation across all variables as one autoregressive and one moving average period. These parameters are then used in calculating the correlation matrix.

Table 73 provides all parameter estimates, where “mu” is the mean, “ar” represent the auto regressive and “ma” represent the moving average of the mean model.

Parameters “omega”, “alpha” and “beta” are the mean, autoregressive, and heteroskedastic parameters of the variance model.

Parameters “skew” and “shape” are estimates to account for specified skewed distributions (GDP and HPI).

*Table 73: Parameter Estimates*

VARIABLE	ESTIMATE
<b>TR1YR.MU</b>	0.017689
<b>TR1YR.MA1</b>	0.728266
<b>TR1YR.OMEGA</b>	0.000356
<b>TR1YR.ALPHA1</b>	0.34166



**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 289

<b>VARIABLE</b>	<b>ESTIMATE</b>
TR1YR.BETA1	0.65734
TR6M.MU	-0.24204
TR6M.AR1	0.844206
TR6M.OMEGA	0.000333
TR6M.ALPHA1	0.249041
TR6M.BETA1	0.749959
TR10YR.MU	1.788644
TR10YR.AR1	0.978005
TR10YR.OMEGA	0.037319
TR10YR.ALPHA1	0.177057
TR10YR.BETA1	0.456361
TR30YR.MU	2.013788
TR30YR.AR1	0.983967
TR30YR.OMEGA	0.068666
TR30YR.ALPHA1	0.282963
TR30YR.BETA1	0.20449
MR.MU	3.154242
MR.AR1	0.974412
MR.OMEGA	0.045142
MR.ALPHA1	0.359321
MR.BETA1	0.231788
UE.OMEGA	0.006415
UE.ALPHA1	1.23E-07

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 290

VARIABLE	ESTIMATE
UE.BETA1	0.999
GDP.MU	5.646064
GDP.AR1	-0.39614
GDP.MA1	0.553704
GDP.OMEGA	0.007758
GDP.ALPHA1	0.073694
GDP.BETA1	0.897449
GDP.SKEW	0.84059
GDP.SHAPE	0.44123
HPI.MU	1.010044
HPI.OMEGA	0.968759
HPI.ALPHA1	0.327666
HPI.SKEW	0.673737
NOI.MU	0.04032
NOI.AR1	0.052933
NOI.OMEGA	0.627161
NOI.ALPHA1	0.117652
NOI.BETA1	0.748712
CCI.MU	0.220487
CCI.AR1	0.066981
CCI.OMEGA	0.099934
CCI.ALPHA1	6.82E-11
CCI.BETA1	0.998999

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 291

## COVID-19 Pandemic Considerations

The impact from the COVID-19 pandemic is noticeable and dramatic when analyzing these economic indicators. Dramatic, historic, and rapid changes to these economic measures provided additional challenges when fitting these models, and produced simulated results that were skewed and assumed to misrepresent historical data.

Because of the historic nature of this event, and its impact on the economy, it is unknown what the long-term impacts of this pandemic will have on the economy. Numerous research articles have been produced to estimate or predict these long-term impacts (Chudik, 2020; Malliet, 2020).

Based on this research, the current state of COVID-19 cases, and an analysis of historical data, a randomized impact of the pandemic was applied.

As a result, two models were estimated, one basing estimates on pre-pandemic data, and the second including the pandemic data. A continued impact of COVID-19 on the economy of eighteen months to five years (six to 20 quarters) was applied randomly as a diminishing linear weight. The two model simulations were then combined using this weighting factor. Initially, the COVID-19 simulation is given the largest weight, and the weight slowly decreases over the randomized period of time until the COVID-19 simulations were given no weight, thus giving the the pre-COVID-19 simulations 100% of the weight.

## Simulation Generation

Model fit was performed through an iterative process, varying parameter specifications for both ARMA and GARCH model components. Distributions were determined using standard distribution fitting techniques, including QQ-plots and Kolmogorov-Smirnov tests. Further parameter selection and distribution adjustments were made based on comparative analysis of simulations to historical series, providing the most reasonable estimates and simulations possible. One hundred simulations were generated for each of the economic variables. These variables were fully transformed back to the common form and scale as the original pre-transformed versions.

## Interest Rate Simulations

Table 74 shows the summary statistics of the historical one-year CMT rates for two different periods as well as the simulated series. We can see that in the last 50 or more years, interest rates have had a much broader range as compared to the last 25 years.

Table 74: Statistics for the One-Year Treasury Rates

STATISTICS	SINCE 1953	SINCE 1991	SIMULATIONS
95-PERCENTILE	10.29%	6.14%	10.29%
90-PERCENTILE	8.94%	5.70%	8.28%
50-PERCENTILE	4.60%	2.41%	3.79%
25-PERCENTILE	2.28%	0.57%	2.01%
10-PERCENTILE	0.51%	0.18%	0.90%

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

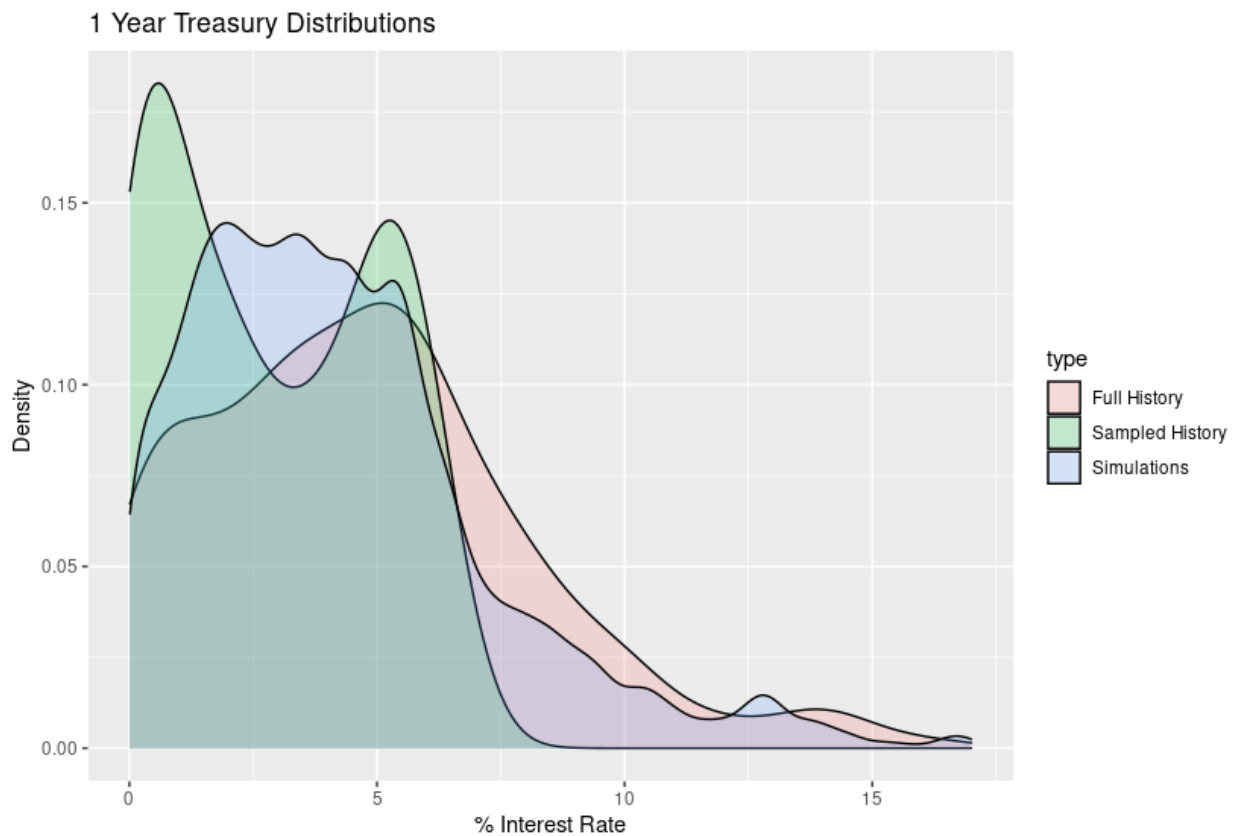
November 12, 2020

Page 292

STATISTICS	SINCE 1953	SINCE 1991	SIMULATIONS
5-PERCENTILE	0.19%	0.13%	0.39%
MEAN	4.78%	2.84%	4.27%
MAX	16.31%	6.71%	17.00%
MIN	0.10%	0.10%	0.01%
VARIANCE	10.78%	4.71%	2.06%

Figure 66 shows density distributions, comparing the distribution of the historical treasury rates, historic sample used for simulations, and the distributions of all the simulations.

Figure 66: One-Year CMT Rate Densities, Historical and Simulations



To avoid negative interest rates, a lower bound of 0.01% was applied to all the simulated future interest rates.

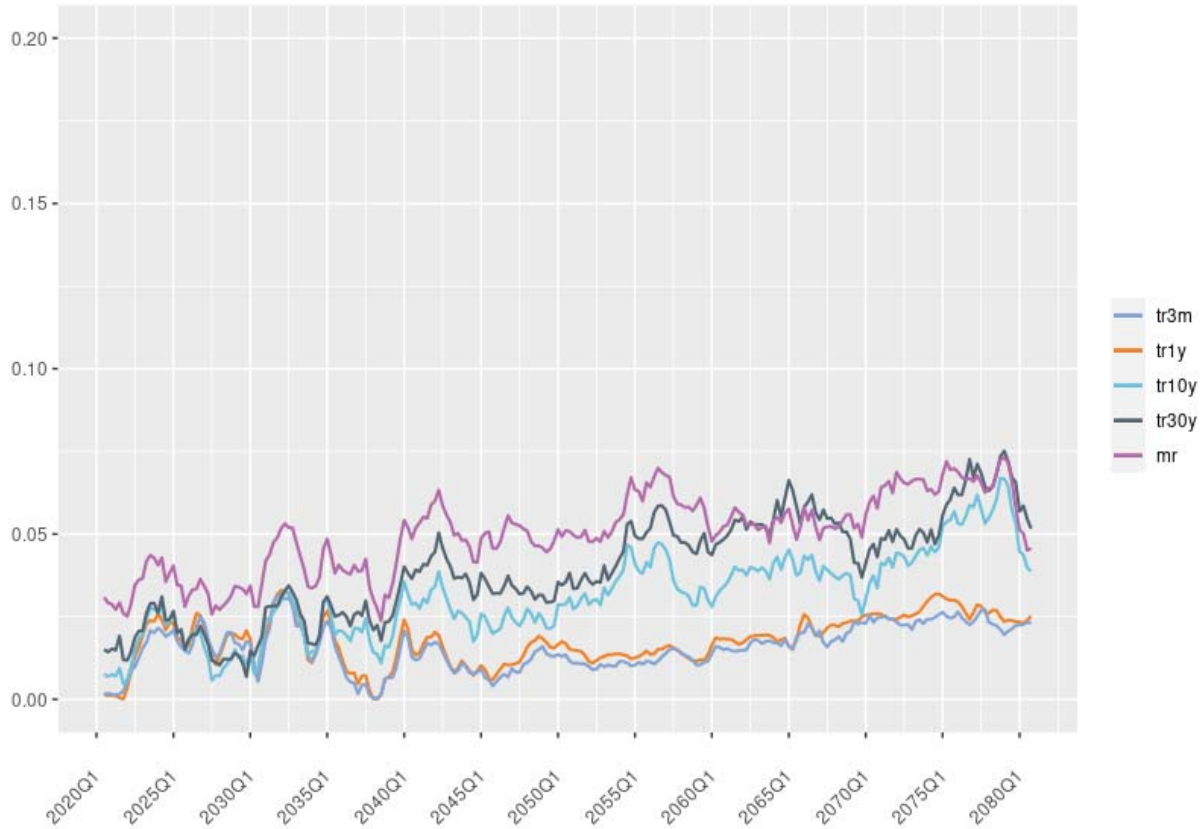
Figure 67 graphs one of the one-hundred simulations, illustrating the co-movements and correlations between these variables and how the multivariate modeling method accounts for these interdependencies.

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 293

Figure 67: Interest Rate Sample Simulation



House Price Appreciation Rate

**A. National HPA**

The national HPA is calculated by first estimating and simulating HPI. From the HPI simulation, these simulations are then transformed using formula (1) to simulate HPA.

Table 75 provides comparison of simulated HPI average trends and the historical sample trends. The analysis show a significant spread between the series when comparing the largest and smallest trends, but when simulated trends are averaged across all series they are very close to the historical trend used in model fitting.

Table 75: HPI Simulation Statistics

	SIMULATED SERIES			HISTORICAL
	Max trend	Min trend	Mean trend	Trend
<b>HPI</b>	1.9411	1.2510	1.6392	1.8777

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 294

## B. Geographic Dispersion

The MSA-level HPA forecasts were based on Moody’s forecast of local and the national HPA forecasts. Specifically, at each time  $t$ , there is a dispersion ratio of HPAs between the  $i^{\text{th}}$  MSA or State level and the national forecast:

$$Disp_{i,t}^{Base} = HPA_{i,t}^{Base} / HPA_{national,t}^{Base} \quad (6)$$

This dispersion forecast under Moody’s base case was preserved for all local house price forecasts under individual future economic paths. That is, for economic path  $j$ , the HPA of the  $i^{\text{th}}$  MSA at time  $t$  was computed as:

$$HPA_{i,t}^j = HPA_{national,t}^j * Disp_{i,t}^{Base} \quad (7)$$

This approach retains the relative current housing market cycle among different geographic locations and it allows us to capture the geographical concentration of FHA’s current endorsement portfolio. This approach is also consistent with Moody’s logic in creating local market HPA forecasts relative to the national HPA forecast under alternative economic scenario forecasts.<sup>62</sup>

We understand this approach is equivalent to assuming perfect correlation of dispersions among different locations across simulated national HPA paths, which creates systematic house price decreases during economic downturns and vice versa during booms. Due to Jensen’s Inequality, this tends to generate a more conservative estimate of claim losses of the Fund.

## Unemployment Rate

### A. National Unemployment Rate

Table 76 provides statistics comparing series samples of unemployment rates to the simulated series

Table 76: Unemployment Historical and Simulation Statistics

STATISTICS	SINCE 1953	SINCE 1991	SIMULATIONS
95-PERCENTILE	9.13%	9.47%	10.77%
90-PERCENTILE	8.08%	8.68%	9.76%
50-PERCENTILE	5.53%	5.45%	6.37%
25-PERCENTILE	4.53%	4.61%	5.04%
10-PERCENTILE	3.69%	4.10%	4.30%
5-PERCENTILE	3.38%	3.82%	4.00%
MEAN	5.76%	5.89%	6.71%
MAX	12.42%	12.42%	15.79%
MIN	2.47%	3.33%	1.53%

<sup>62</sup> The dispersion of each MSA remains constant among all alternative Moody’s forecast scenarios.

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

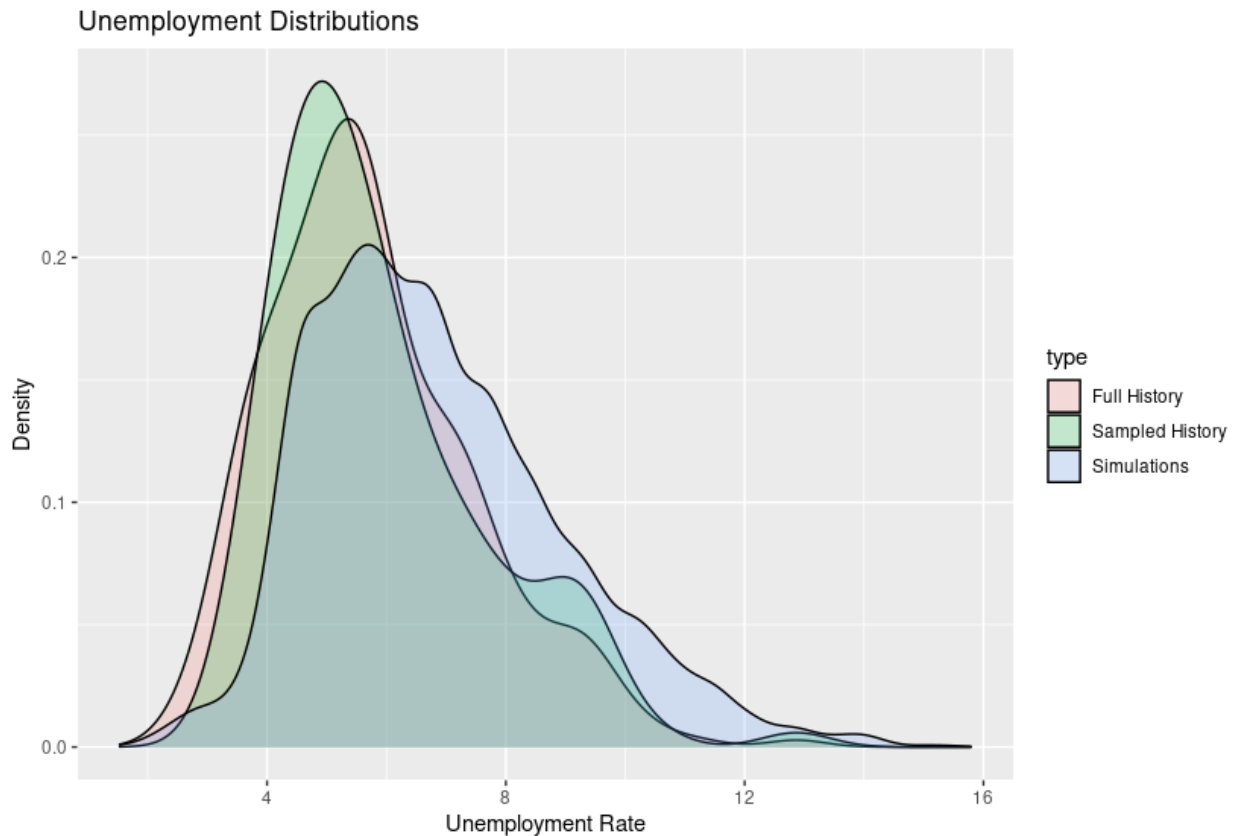
Page 295

STATISTICS	SINCE 1953	SINCE 1991	SIMULATIONS
VARIANCE	2.96%	3.06%	2.04%

Based on historical statistics, the national unemployment rate limits were set at a 20% maximum and a 2% minimum.

Figure 68 is a density plot comparison of the historical series and simulated sets.

*Figure 68: Unemployment Rate Densities Historical and Simulations*



**B. Geographic Dispersion**

Following the same logic that we applied to the MSA-level HPA forecasts, we first obtained the dispersion of unemployment rates between the  $i^{th}$  MSA or State level and the national level from Moody’s July base-case forecast at each time  $t$ :

$$Disp_{i,t}^{Base} = ue_{i,t}^{Base} / ue_{national,t}^{Base} \tag{9}$$

This dispersion forecast was preserved for all local unemployment rate forecasts under each individual future

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 296

economic path. That is, for economic path  $j$ , the unemployment rate of the  $i^{\text{th}}$  MSA at time  $t$  was computed as:

$$ue_{i,t}^j = ue_{national,t}^j * Disp_{i,t}^{Base} \tag{10}$$

For the simulation, we capped the unemployment rate at the local level at 30% with a floor at 1%.

## Gross Domestic Product

Table 77 provides statistics comparing the historical GDP series trend to simulated trends. The analysis show a fairly small spread between the series when comparing the largest and smallest trends, and when simulated trends are averaged across all series they are very close to the historical GDP trend used in model fitting.

Table 77: GDP Simulation Statistics

	SIMULATED SERIES			HISTORICAL
	Max trend	Min trend	Mean trend	Trend
<b>GDP</b>	2.921	1.742	2.215	2.430

## Small Business Normalized Optimism Index/ Consumer Confidence Index

The small business and consumer confidence indices are based on a 100 point scale, where values under 100 represent less confidence in the economy, values over 100 indicate an increase in confidence.

Table 78: Confidence Indices Statistics

	HISTORICAL	SIMULATED	HISTORICAL	SIMULATED
	NOI	NOI	CCI	CCI
<b>MAX</b>	142.11	177.35	108.18	122.21
<b>MIN</b>	29.86	24.61	82.73	65.89
<b>MEAN</b>	94.38	96.22	98.13	94.18

Table 78 provides comparisons of the range and means for both indices and the corresponding simulated data showing that the simulations provide reasonable ranges compared to historical data.

## REFERENCES:

Shephard, N. 1996. Statistical aspects of ARCH and stochastic volatility. In Time Series Models in Econometrics, Finance and Other Fields, Hinkley DV, Cox DR, Barndorff-Nielsen OE (eds). Chapman & Hall: London.

Engle, Robert F., Dynamic Conditional Correlation - a Simple Class of Multivariate GARCH Models (May 2000). UCSD Economics Discussion Paper No. 2000-09, Available at SSRN: <https://ssrn.com/abstract=236998> or



**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 297

<http://dx.doi.org/10.2139/ssrn.236998>

Ghalanos, Alexios (2019) Multivariate GARCH Models – rmgarch(1.3-7) [Cran-R]. <https://cran.r-project.org/web/packages/rmgarch/rmgarch.pdf>

Malliet, P., Reynès, F., Landa, G. *et al.* Assessing Short-Term and Long-Term Economic and Environmental Effects of the COVID-19 Crisis in France. *Environ Resource Econ* 76, 867–883 (2020). <https://doi.org/10.1007/s10640-020-00488-z>

Chudik, A, Mohaddes, K, et al. Economic consequences of Covid-19: A counterfactual multi-country analysis (Oct 2020) <https://voxeu.org/article/economic-consequences-covid-19-multi-country-analysis>

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 298

## Appendix E: Cash Flow Analysis

### Introduction

The calculation of the Cash Flow NPV of the MMI involves the estimation of the present value of future cash flows generated by the existing portfolio. The analysis requires the projection of future prepayment and claim incidences, and severity and cash flow items associated with each type of outcome. The Cash Flow NPV represents future revenue and expenses associated with the existing book of mortgage guarantees. This appendix describes the components of these cash flow calculations.

To develop the estimated Cash Flow NPV, our model incorporates projections of mortgage performance and information about the existing portfolio composition to project the MMI's various cash flow sources. The cash flow projection model uses projections from predictive models as discussed in Appendix B (Transition Models), Appendix C (Loss Severity Models), and the economic scenarios described in Appendix D. We developed predictive models for conditional transition probabilities for individual mortgages depending on a number of mortgage and economic characteristics. From these models and using detailed mortgage-level characteristics, we estimated the various transition probabilities and then generated respective cash flows for individual mortgages.

Based on the mortgage termination rates projected by the predictive models, individual components of cash flows are projected into the future. These cash flows are discounted to present value based on the single discount rate provided by the OMB. Based on the specific characteristics of the mortgage, the probability of each transition is calculated. Then, a random number between 0 and 1 is generated, and based on this random draw a mortgage transition is determined. The projection process continues for each mortgage until the mortgage ends by prepayment, claim or reaches maturity.

The cash flow components are shown in the following table:

*Table 79: Cash Flow Components*

Cash Inflows	Cash Out Flows
Upfront MIP	Net Claim Payments
Annual MIP	Loss Mitigation Expenses
Interest Income	Refunded Upfront Premiums

These cash flows were projected quarterly for individual mortgages and then aggregated by product type and origination year. Below, we discuss the development of each of these cash flows.

### Cash Flow Components

The components of cash flow are discussed below.

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 299

### MIP

The primary source of revenue to the MMI is insurance premiums. If the MMI's mortgage insurance is priced to meet the expected liabilities, the MIP collected and interest earned on the MIP will cover all costs associated with mortgages insured by the MMI under a normal or expected economic environment. The MIP structure and the premium rates have changed over the period under evaluation. Details of MIP changes are as follows:

- For mortgages originated prior to September 1, 1983, the MIP was collected on a monthly basis at an annualized rate of 0.50% of the outstanding principal balance for the period. To align this change with fiscal quarters, we assumed that this annual MIP policy was in effect through September 30, 1983.
- Between September 1, 1983 and June 30, 1991, the MIP was charged only upon mortgage origination and was based on a percentage of the original mortgage amount at the time of origination. This amount was 3.80% for 30-year mortgages and 2.40% for 15-year mortgages.
- Effective July 1, 1991, NAHA implemented a new MIP structure. An upfront MIP of 3.80% was charged for all product types except for 15-year non-SR mortgages, for which the upfront MIP was set at 2.00%. An annual MIP of 0.50% per year on the outstanding balance was also implemented. The annual MIP would cease at different years of maturity depending on the initial LTV of the mortgage.
- On October 1, 1992, the upfront MIP for 30-year mortgages was reduced from 3.80% to 3.00%. The annual MIP for 30-year mortgages was extended for a longer time period, while for 15-year mortgages it was lowered to 0.25% for a shorter time period or completely waived if the initial LTV ratio was less than 90%.
- As of April 17, 1994, FHA lowered the upfront MIP rate on 30-year mortgages from 3.00% to 2.25%. To align this change with fiscal quarters, we applied this policy change on April 1, 1994.
- Starting from October 1, 1996, FHA lowered the upfront MIP rate on 30-year mortgages for first-time homebuyers who received homeowner counseling from 2.25% to 2.00%. This rate was further reduced to 1.75% for mortgages originated on or after September 22, 1997. This favorable treatment for borrowers with homeownership counseling was terminated shortly thereafter.
- Effective January 1, 2001, FHA lowered the upfront MIP rate for all mortgages to 1.50%. The annual MIP would be discontinued as soon as the current LTV ratio of the mortgage was below 78% according to the home price as of the mortgage origination date. The annual MIP was required to be paid for a minimum of five years for 30-year mortgages.
- Effective October 1, 2008, FHA charged an upfront premium rate of 1.75% for home purchase and full-credit qualifying refinances; and 1.50% for all types of streamline refinance mortgages. A varying annual

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 300

MIP, collected on a monthly basis, was charged based on the initial LTV ratio and maturity of the mortgage.

- Effective April 1, 2010, FHA changed the upfront MIP to 2.25% for all mortgages executed after April 1, 2010.
- Effective October 4, 2010, FHA lowered the upfront MIP of all mortgages to 1.0%. The annual MIP for mortgages with 30-year terms was increased to 0.85% for LTV ratios up to 95 percent and to 0.90% for LTV ratios greater than 95%. For mortgages with 15-year terms, an annual MIP of 0.25% was set for LTV ratios greater than 90%. To align this change with fiscal quarters, we started applying this policy change on October 1, 2010.
- Effective April 18, 2011, the annual MIP for mortgages with 30-year terms was increased to 1.10% for LTV ratios up to 95% and to 1.15% for LTV ratios greater than 95%. For mortgages with 15-year terms, the annual MIP was increased to 0.25% for LTV ratios up to 90% and to 0.50% for LTV ratios greater than 90%. To align this change with fiscal quarters, we started applying this policy change on April 1, 2011.
- Effective April 9, 2012, FHA increased the upfront MIP of all mortgages to 1.75%. The annual MIP for mortgages with 30-years terms was increased to 1.20% for LTV ratios up to 95%, and to 1.25% for LTV ratios greater than 95%. For mortgages with 15-year terms, the annual MIP was increased to 0.35% for LTV ratios up to 90%, and to 0.60% for LTV ratios greater than 90%. To align this change with fiscal quarters, we started applying this policy change on April 1, 2012.
- Effective June 11, 2012, the annual MIP for mortgages with 30-year terms and base mortgage amounts above \$625,500 was increased to 1.45% for LTV ratios up to 95%, and to 1.50% for LTV ratios greater than 95%. For mortgages with 15-year terms, and base mortgage amount above \$625,500, the annual MIP was increased to 0.60% for LTV ratios up to 90%, and to 0.85% for LTV ratios greater than 90%. Also effective June 11, 2012, for all single family forward SR mortgages which are refinancing existing FHA mortgages that were endorsed on or before May 31, 2009, the upfront MIP decreased to 0.01% of the base mortgage amount, and the annual MIP was set at 0.55%, regardless of the base mortgage amount. To align this change with fiscal quarters, we started applying this policy change on July 1, 2012.
- Effective April 1, 2013, the annual MIP for mortgages with 30-year terms and base mortgage amounts below \$625,500 was increased to 1.30% for LTV ratios up to 95%, and to 1.35% for LTV ratios greater than 95%. The annual MIP for mortgages with 30-year terms and base mortgage amounts above \$625,500 was increased to 1.50% for LTV ratios up to 95%, and to 1.55% for LTV ratios greater than 95%. For mortgages with 15-year terms and base mortgage amounts below \$625,500, the annual MIP was increased to 0.45% for LTV ratios up to 90%, and to 0.70% percent for LTV ratios greater than 90%. For mortgages with 15-year terms and base mortgage amounts above \$625,500, the annual MIP was

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 301

increased to 0.70% for LTV ratios up to 90%, and to 0.95% for LTV ratios greater than 90%. This increase was effective for all forward mortgages except single family forward SR transactions that refinance existing FHA mortgages that were endorsed on or before May 31, 2009.

- Effective June 3, 2013, the annual MIP rates for mortgages with an LTV of less than or equal to 78% and with terms of up to 15 years was 0.45%. The new payment period for annual MIP for mortgages with case numbers assigned on or after June 3, 2013 and with an LTV up to 90% was 11 years, and the annual MIP applied for the life of the mortgage for LTVs greater than 90%. To align this change with fiscal quarters, we started applying these policy changes on July 1, 2013.
- Effective January 26, 2015, the annual MIP rates for mortgages with a term greater than 15-years have been reduced by 50 basis points. To align this change with fiscal quarters, we applied these policy changes on January 1, 2015.

### Upfront MIP

The upfront MIP is assumed to be fully paid at the mortgage origination date and the amount is calculated as follows:

$$\text{Upfront MIP} = \text{Origination Mortgage Amount} * \text{Upfront MIP Rate}$$

In practice, FHA allows qualified homeowners to finance the upfront MIP so that the upfront MIP does not add to the borrower's equity burden at the beginning of the contract. Instead, the borrower can add the upfront MIP to the original mortgage balance, in essence paying the upfront MIP on the same schedule as their principal balance. The annual MIP is charged based on the unpaid principal balance excluding the financed upfront MIP. Almost all borrowers finance their upfront MIP in this fashion. However, the LTV including refinanced upfront MIP cannot exceed 96.5%.

### Annual Premium

The annual MIP is calculated as follows:

$$\text{Monthly MIP} = \text{UPB (excluding any upfront MIP)} * \text{Annual MIP Rate} / 12$$

The MIP is actually collected on a monthly basis. For purposes of the simulation, the monthly MIP is aggregated by quarter, and this quarterly premium is used to discount MIP for the simulation.

### Refunded MIP

FHA first introduced the upfront MIP refund program in 1983. It specified that FHA would refund a portion of the upfront MIP when a household prepaid its mortgage. The upfront MIP was considered to be "earned" over the life of the mortgage. Upon prepayment, an approximation of the unearned upfront MIP is returned to the borrower. Therefore, the amount of the refund depends on the time from origination to when the mortgage is prepaid. For modeling purposes, the refund payments are calculated as follows:

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 302

$$\text{Refund Payments} = \text{Original UPB} * \text{Upfront MIP Rate} * \text{Refund Rate}$$

Refund payments at each quarter are calculated based on the number of mortgages prepaid in that quarter and the origination date of the mortgage. In the past, borrowers always received the upfront MIP refund when they prepaid their mortgages before the maturity of the mortgage contract. In 2000, FHA changed its policy so that borrowers would obtain refunds only if they prepaid within the first five years of their mortgage contracts. The most recent policy change at the end of 2004 eliminated refunds for early prepayments of any mortgages endorsed after that date, except for those borrowers who refinanced into a new FHA mortgage within three years following the original endorsement date.

### Losses Associated with Claims

The MMI's largest expense component comes in the form of payments arising from claims. FHA pays the claim to the lender after a lender files a claim. Traditionally, in most cases, FHA takes possession of the foreclosed property and sells the property to partially recover the loss. This particular type of claim is called a conveyance (REO).

Based on this practice, claim cash flows can be decomposed into two components:

1. Cash outflow of the claim payment at the claim date including expenses incurred, and
2. Cash inflow of any net proceeds received in selling the conveyed property at the property disposition date.

We have estimated the net loss as discussed in Appendix C separately for PFS, TPS and REO. Based on the specific characteristics of the mortgage, the net loss for each claim is calculated. Then, a random number between 0 and 1 is generated, and based on this random draw the predicted net loss is determined.

### Loss Mitigation Expenses

FHA initiated a loss mitigation program in 1996 in an effort to provide opportunities for borrowers in financial difficulties to retain homeownership. Loss mitigation also reduces foreclosure costs. In the standard process, the mortgagees provide default counseling for borrowers who are behind in their payments, and offer appropriate loss mitigation options to prevent borrowers from losing their homes. In 2009, FHA started the HAMP program as a new loss mitigation option, and the program represented increasing percentages of loss mitigation assistance through the years. In 2016, Mortgage Modification as a standalone option was eliminated and combined into HAMP.

The loss mitigation program includes Forbearance and HAMP, which has Loan Modification and Partial Claim options. A Special Forbearance is a written repayment agreement between the mortgagee, acting on behalf of FHA, and the borrower that contains a plan to reinstate a mortgage. A Loan Modification modifies the contractual terms of the mortgage permanently, such as lowering the interest rate, or increasing the mortgage term. Under the partial claim option, a mortgagee will advance funds on behalf of a mortgagor in an amount necessary to reinstate a delinquent mortgage. The borrowers are required to sign a promissory note and a

# Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

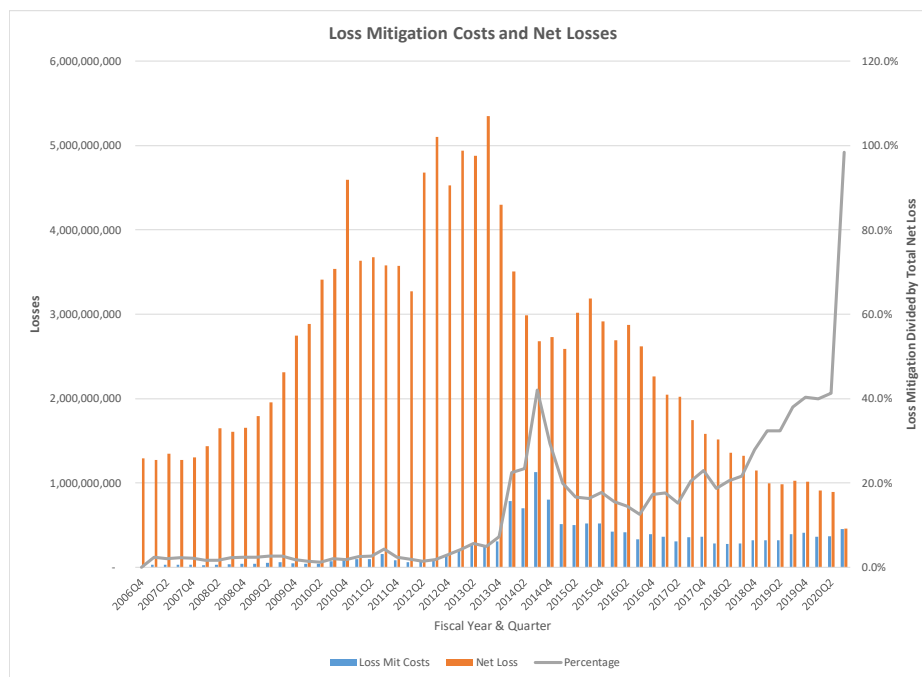
November 12, 2020

Page 303

subordinated mortgage payable to FHA of the amount advanced.

Figure 69 shows the ratio of loss mitigation costs to overall net losses. Loan mitigation cases increased significantly from Fiscal Year 2007 to Fiscal Year 2014. There were just under 80,000 loss mitigation claims in Fiscal Year 2007 which grew to over 180,000 cases in Fiscal Year 2014. The amount FHA paid in these cases and curtailments was \$116 million in Fiscal Year 2007, which increased to \$3.41 billion in Fiscal Year 2014. From 2014 to 2018, loss mitigation payments decreased to \$1.16 billion, but then increased in 2019, and are projected to increase again in 2020. For the second quarter of 2020, loss mitigation payments account for 98% of all claim payments. This is due to the COVID forbearance rules that were implemented on March 1, 2020. All foreclosure proceedings have been halted, and no new foreclosure proceedings can begin until 2021. Therefore, the non-loss mitigation claims will be delayed until normal foreclosure and claim processes can resume. Loss mitigation payments made by FHA include administrative fees and costs of title searches, recording fees and subordinated mortgage note amounts.

Figure 69: Loss Mitigation Expense



As discussed in Appendix C, we have developed models to project loss mitigation expenses.

## Net Present Value

Once all the above future cash flow components are estimated, their present value is computed by discounting them at an appropriate rate. The discount factors applied were provided by FHA and reflect the OMB discount factors and the expected timing of future cash flows. The rates are constant and vary by mortgage cohort year. The discount factors reflect the most recent Treasury yield curve, which captures the federal government's cost

**Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 304

of capital in raising funds. These factors reflect the capital market's expectation of the consolidated interest risk of U.S. Treasury securities. Our simulations aggregated each future year's cash flows by quarter, and treat the cash flows as being received at the end of the quarter.



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 305

### Appendix F: Review of HUD Analysis of Economic Net Worth, Comparison of HUD and Pinnacle Models, and Assessment of Vulnerabilities

---

Appendix F presents a high-level review of HUD models developed to project Economic Net Worth, compares the models developed by HUD with the models developed by Pinnacle, and assesses the vulnerabilities of the models developed. We have also identified potential areas of future research based on this assessment.

Deliverable 4 of the Actuarial Report states:

***To promote transparency of the Studies' assessments, the Studies should identify methodological vulnerabilities that may occur in its actuarial models or in HUD's analyses of Economic Net Worth. This discussion should evaluate the scope and scale of such vulnerabilities in creating possible forecast risk and suggest possible lines of research in these areas. The Studies shall assess and comment upon HUD's own models that estimate Economic Net Worth for methodological vulnerabilities and compare HUD's methodologies with those in the Studies.***

There are several different aspects of forecast risk that can arise in the projection of Economic Net Worth, including:

- Process risk— actual results vary from projected results due to variability in the mortgage insurance process
- Parameter risk— the uncertainty related to the parameters selected for a given model
- Specification risk— the uncertainty related to the type of model that is selected for a forecast

The following discussion comments on these various types of forecast risk.

#### Forward Budget Model Commentary

Summit-Milliman (S-M) has developed a series of models consisting of the Single Family (Forward) Budget Model Schema that are used to forecast cash flows for the Forward mortgages in the FHA portfolio. The following discusses strengths and potential vulnerability of these models, as well as identifies potential areas for further research.

#### Model Schema

The Loan Performance Models consist of a Stage 1 model for loans that have never been seriously delinquent and a Stage 2 model for loans that have experienced a 90-day delinquency. Both models are used to predict the likelihood of a given loan becoming seriously delinquent or prepaying. This is reasonable as the two sub-populations exhibit different future transition behaviors.

The Stage 1 model uses a series of binomial logistic cell regressions to estimate the probabilities for non-claim termination and serious delinquency, incorporating the assumption of Independent Irrelevant Alternatives (IIA). The IIA assumption states that adding or removing termination events does not impact the odds of the original

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 306

termination event. This is a potential vulnerability of the models if this assumption is violated. However, to the extent this assumption holds, then the S-M approach is mathematically equivalent to a multinomial logistic model, which would be a reasonable approach given the number and type of outcomes being predicted.

S-M built two Stage 1 models, one for purchase loans and one for refinance loans, as they exhibit different prepayment rates. This also appears to be a reasonable assumption based on our independent analysis of purchase and refinance loans.

The Stage 1 models were built using cell regression, which aggregates the loans into unique groups using combinations of values of 20 different variables. The purpose of this method is to maximize the amount of data used to build the model while minimizing the required computing capacity. This is different than Pinnacle's approach where the models were built on an individual loan level. S-M noted that there were only minimal changes to the current models as compared to the prior FY2021.1 versions. Specifically, S-M updated the spline knots for the Stage 1 Purchase Prepay Loan size relativity variable. This is reasonable, and also similar to Pinnacle's approach of making updates to placement of knots based on updated data.

There are some potential vulnerabilities in the S-M modeling approach, which are acknowledged by S-M as well:

- The models were developed using a long period of data (1990-2019). For Stage 2 loss mitigation models, delinquencies from 2009 and subsequent were used. This may cause slower reflection of shorter term trends. As Pinnacle uses data from the beginning of the Forward Mortgage Guaranty program, this is potential vulnerability in the Pinnacle models as well.
- Only the Stage 2 model is used for a loan once it is 90 days delinquent, which can fail to fully reflect short-term changes if a loan quickly self-cures, for example.
- The historical data may not be reflective of future performance or of program changes. Again, these are potential shortcomings in the Pinnacle models as well. See section below regarding S-M adjustments due to COVID-19 impacts.
- Other significant changes in economic conditions, such as in unemployment as has been seen recently due to the COVID-19 pandemic, may not be fully or adequately reflected in the model results.

For these vulnerabilities, but in particular the first one, one area of potential future research is to refit the models on more recent data and evaluate the change in the model parameters. Also, results of the model could be validated against more recent data to test how well the models reflect more recent experience. One approach that Pinnacle has incorporated to account for this vulnerability is to include credit subsidy cohort and loan period as variables in the models. An additional research step would be to test the interaction of these time related elements with other independent variables in the models.

The Stage 2 Loan Performance Model was developed on a loan level basis. Due to different claim rates, S-M built

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 307

two Stage 2 models depending on whether the loan received loss mitigation in the past or not. Once a loan enters a Stage 2 model it cannot revert back to Stage 1. The models used multinomial logistic regression given the number and type of different potential outcomes. S-M evaluated the structure and appropriateness of the Stage 2 models but did not make any updates from the prior FY2021.1 models.

S-M used a few approaches to validate their Stage 1 and Stage 2 Loss Performance Models, including out-of-sample actual vs. expected results, Receiver Operating Characteristic (ROC) curves, and comparison of claim rates for loans that did or did not receive loss mitigation. S-M also reviewed the variable significance levels for the models. All of these are reasonable approaches. An additional approach to consider would be to use out of time data to validate the models, however if more recent data was left out of the initial model development, it would potentially increase the likelihood of shorter-term trends being missed.

The Loss Mitigation Models developed by S-M have two parts for Stage 2, one for loans with loss mitigation applied and one for loans without loss mitigation. This is done since the probabilities of claim vs. non-claim termination vary greatly depending on if a loan receives loss mitigation or not, and is consistent with the S-M approach for Stage 2 Loan Performance Models. However, due to changes in government programs and frequency of mitigation usage over the years, S-M notes there may not be enough data to develop a reliable model to predict which delinquent loans will receive loss mitigation. Therefore, actuarial methods were used to project these rates. S-M selected a 38% loss mitigation rate for the current models based on updated data which was a slight decrease from the 40% rate selected for the prior FY2021.0 models. While it is reasonable to use actuarial methods in this case, this does introduce an additional potential source of uncertainty in the results. Also, it is not clear what testing that S-M did to conclude there was not enough data to develop a loss mitigation prediction model. Future research could involve attempting to build models on the data that does exist and comparing the model results to recent actual results to determine if the accuracy is sufficient.

The Loss Severity Models developed by S-M predict the disposition and severity of a loan loss from Stage 2 in two parts. The disposition estimation model predicts the probability of a loan entering a specific disposition path (PFS, Single Family Loans Sales [SFLS], CWCOT, or REO). The loss severity model predicts the amount of loss given a default. The disposition model uses a waterfall approach.

The model first uses binomial logistic regression to estimate the probability of a PFS vs. other type of disposition. Data from 1995 and forward was used. Due to lower data volume, historical data from January 1, 2018 to January 1, 2020 is then used to determine if a non-PFS is estimated to be either a SFLS or CWCOT. Finally, the conditional probability for REO is simply the remaining proportion of claims since it is the end of the process waterfall. Potential future research could be to test the two-year period for historical data to determine whether two years of data is sufficient, or to demonstrate how sensitive the results are to different lengths of time. Similarly, CWCOT severity, SFLS severity, and SFLS sales price are determined using this same two-year period. Future analysis should be considered to validate this length of time and its impact on results. Pinnacle uses the entire data history to build models determining the likelihood of an REO or TPS claim.

With the current models, S-M made methodological changes to PFS and REO loss severity estimation by

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 308

eliminating the econometric estimation of acquisition cost components and instead used a historical distribution method. Also, they updated the variable specification for PFS disposition regression, the PFS Sale Ratio regression, and the REO Sale Ratio regression with the current models. These changes were made to improve the fit and performance of the models. S-M validated their models using comparisons of out-of-sample actual-to-expected results by termination quarter, claim rates for all loans, and of the log of loss for REO and PFS claims. Also, they found that estimates produced by the models are consistent with historical experience. All of these methods are reasonable approaches to validation.

These three models (Loan Performance, Loss Mitigation, and Loss Severity) combine to produce cash flows to then calculate Liability of Loan Guarantee (LLG) and Return on Assets.

S-M then estimates acquisition costs separately from Net Loss using Ordinary Least-Squares (OLS) regression. They also estimate sale ratio using linear regression, whereas previously the ratio was calculated from sales price. While these can be improvements in sophistication of the modeling and results, this can also now add additional uncertainty from the additional model parameters.

With the prior (FY 2021.1) model version, S-M introduced a 2.0% Quarterly Prepayment Rate Floor. While this could introduce some future variability in the results particularly considering the current economic conditions, S-M tested the selection using historical data to determine a reasonable floor, and also tested results with different (including no) floors. This was also the result of S-M's discussion with FHA on a reasonable prepayment rate floor to use. Note that as described below that due to COVID-19 impacts, S-M has increased the rate to 3.5% to reflect the recent increase in pre-payment activity.

S-M's process for selecting variables is reasonable. This process included performing exploratory data analyses and univariate analyses to better understand the data. Specifically, S-M reviewed how well a variable was populated, how the variable changes over time, and how well the variable relates to the target. S-M also considered collinearity between variables. Univariate regression analysis and backward selection stepwise regression were used, with a p-value threshold of 10% to determine which variable to include in the stepwise procedure. S-M also ran models across time to assess model stability. Splines were added to various models to improve performance, with the c-statistic measured to determine impact. Finally, when considering whether to include a variable in a model, S-M considered the intuitive relationship of the model variables and the predictive nature of the variable.

S-M notes that several variables such as credit score, borrower income, debt-to-income ratio, and loan-to-value ratio have an influence on mortgage performance yet are censored or have missing data in the datasets for various reasons. S-M made an explicit adjustment on the credit data to back-populate it, as is described in more detail below. An area for further research would be determining if there are additional sources to better populate other types of variables for which a significant portion of the data is missing.

There are several additional potential areas for future research/testing of assumptions.

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 309

- The S-M report notes that the majority of FHA's endorsement volume is from post-2007 credit subsidy cohorts, and as a result, the data for the cohorts is not fully developed. The implicit assumption is that these younger cohorts will perform similarly to older cohorts. As more data is obtained over time, this assumption should be tested, and appropriate adjustments made if any differences in performance are seen.
- The report noted that the FHA to FHA refinance rate changed from 25% to 20% from the prior (FY2021.0) to the current (FY2022.0) model version due to the declining trend observed since 2015. It should also be noted that the refinance rate was decreased from 35% used for the models prior to FY2021.0 versions. The sensitivity of the results to this change should be further explored since the change in the refinance rate is significant.
- The payment reduction factor used from the prior to the current version of the model changed from 22.5% to 15% due to the mean and median observed percentages that varied from 12.7% to 26.7% observed from 2013 through 2019 and the declining rate trend. The report also noted that the factor has varied substantially over the past several years. The sensitivity of the results to this change should be further explored given the variation that has been seen in this parameter over time.
- The results use a two-year lookback period for the Return on Properties calculation. While not necessarily unreasonable, further exploration of different lookback periods and support for the two-year selection would be a reasonable approach to validate the selection.

Following are some additional sources of potential vulnerabilities in the methodology.

- Declining vs. Increasing Interest Rate Environment—while noted in the report, the historical data used in model development was collected in a generally declining interest rate environment. However, the forecast is for interest rates to increase. This introduces a potential source for uncertainty in the results since the historical data is not necessarily reflective of loan performance in the future expected interest rate environment.
- Sensitivity tests performed on HPA and interest rate factors assume independence of factors and so may impact the results that would actually be seen with multiple varying parameters.
- S-M selected 2012-2019 cohorts due to volume and availability of actual historical cashflows for performing back-testing of their model results. This is a different approach than taken with last year's study where 1992, 1999, and 2006 were the only years selected. While this is not unreasonable, this could be a potential source of variability in results if different cohort years were selected.
- During the discussion of their modeling methodology, S-M notes that they built the Loan Performance

## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 310

and Loss Severity models on 80% of the data and validated them on the remaining 20% as an out-of-sample holdout. This is a reasonable approach. However, S-M did note that after they validated the performance of the model, they re-estimated it on 100% of the data. One potential vulnerability in this approach would be a significant change in the estimated model parameters between the 80% fit and the 100% fit. S-M did do such a validation comparison for the Loss Severity Models, with overall results looking reasonably similar.

- There are multiple models being used in combination, so there is the risk of error propagation across the multiple models.

### COVID-19 Impact Adjustments:

S-M made several adjustments to models due to expected impacts from COVID-19. These adjustments appear to be reasonable based on available data.

- Increase Roll Rates to Reflect COVID—30 and 60-day delinquency roll rates were developed to estimate the population of 90+ day delinquencies using data from the 2008-2011 financial crisis as guidance. This was only a temporary adjustment until September 2020 data was available.
- Increase Loss Mitigation rates to Reflect COVID—rates were increased for loans that have utilized forbearance based on data that shows delinquent loans during COVID that have used forbearance are more likely to also use loss mitigation.
- Implement Revised Loss Mitigation Waterfall—the waterfall pattern was updated based on mortgagee letter 2020-22 that was issued in July 2020.
- COVID PC Payments and Timing—S-M selected a multiplier of 6 for each loan's monthly PITI based on assumed number of missed payments for a 6-month forbearance period per mortgagee letter 2020-22. Also, S-M included an assumption that COVID PC payments will occur in Q1 of FY2021 with recoveries occurring with Stage 2 NCT events. Loans ineligible for the COVID PC will follow standard loss mitigation timing and be dependent on the HAMP loss mitigation module.
- Higher near-term Prepayment rates to Reflect Low-Interest Rate Outlook—S-M has adjusted the three month prepayment floor from 2.0% to 3.5% to be in place through the end of FY2021 based on observed rates over the past 12 months.

Through their analysis of the data, S-M recognized that the credit score is a very important component of prediction, and also that a significant amount of credit scores were missing for loans prior to 2004 due to how the FHA program was administered. Therefore, S-M attempted to supplement the credit score data from additional sources. One source was a study completed by Fannie Mae, but upon review of the data that approach still resulted in a significant number of missing scores. Next, loan level data was then appended from a CoreLogic source. S-M compared aspects of this data to the existing scores for a time period that overlapped between the CoreLogic and FHA data (2005-2013) and determined that it was reasonable to use based on the average credit scores by year for each of the datasets. Based on Pinnacle's review of the summary statistics of

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 311

the data, while this is not an unreasonable approach to take to supplement missing credit scores, some degree of caution should be exercised since there is a significant difference in the average credit scores between the two sources, with the CoreLogic source showing higher scores. To help account for this, S-M included an indicator for score source in the models, which is reasonable.

### **Pinnacle Forward Budget Model Commentary**

The following illustrates some of the similarities and differences in methodologies for the Forward budget models between the Pinnacle analysis and that done by S-M for HUD.

The Pinnacle models analyzed the forward book of loans based on separate products: 30-year FRM, 15-year FRM, refinances, and ARM. The S-M approach did not build models separately by product beyond the purchase loans vs. refinance loans for their Stage 1 model. Also, the Pinnacle models were built on an individual loan level. S-M used individual loans for their Stage 2 models but grouped the data (cell regression) for their Stage 1 models.

### **Model Schema**

The schema of the models is different between the S-M process and that of Pinnacle. Both reflect models for Performing (Stage 1 or Current) vs. Non-Performing (Stage 2 or Default) loans. Pinnacle further develops separate models based on product (FRM30, FRM15, ARM). The HUD models predict the likelihood of prepayment or delinquency from each of the Stage 1 or Stage 2 starting points. Pinnacle's models reflect potential transition to multiple states.

- Transitions from Current mortgage: remain current, default/claim, prepay by SR, other prepayments, cure with mortgage modification, self-cure
- Transitions from Default mortgage: prepay, transition into a claim, self-cure, cure with mortgage modification, remain in default

Transition models for Pinnacle are used to project how a loan will move to a different status. Loss Severity Models are used to project the amount of loss given a claim.

Regarding the modeling process, for this year's analysis Pinnacle has continued to use multiple binomial models for the Forward transition models. Pinnacle researched reverting to a multinomial model but found no significant differences in the resulting parameter estimates, and thus decided to continue the same process.

The main vulnerability in the models is the general vulnerability of developing predictive models: the extent to which historical patterns between target and projected results are indeed predictive. We have attempted to mitigate this potential vulnerability through a training and validation construct. For the Transition Models, we use 60% of the data to train the models and 40% of the data to validate the models. This is different than the split percentages used by S-M. For the Loss Severity Models, a train/validate approach also was used. Pinnacle did not do any out of time sample validation.

## **Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force**

November 12, 2020

Page 312

Pinnacle models were validated in general by comparing actual to predicted results in decile charts. This was done for both the transition models and loss severity models.

Pinnacle applied random sampling for a few of the Current transition model types to improve efficiency of the modeling process. This could be a potential source of variability if not truly random, and a future area of refinement could be to test to see if using different sampling percentages result in a difference in the model results. Pinnacle did use the full data sample on many more of the transition model types with this analysis than in past reports.

For Loss Severity models, Pinnacle built a multinomial logistic model to predict claim disposition—PFS, REO, or CWCOT. S-M also included the Single Family Loan Sales (SFLS) as a type. Pinnacle also built models to predict loss severity (using Generalized Linear Models with a Gamma error structure and a log link function) for each of PFS, REO, and CWCOT, as well as a model for recovery amounts if the claim is a foreclosure REO. S-M does not separately specify a recovery amount model. Finally, Pinnacle also modeled loss mitigation costs.

S-M utilized data from Moody's in their loan projections. Pinnacle uses 10 economic scenarios from Moody's, and 100 random stochastic simulations of key economic variables to develop a range of Cash Flow NPV. Both S-M and Pinnacle utilized Moody's data on a state and MSA level when possible to provide for a greater reflection of differences in home prices, etc. across the country.

### **Simulation**

Pinnacle ultimately utilized 100 random stochastic simulations to determine the range of Cash Flow NPV estimates. This compares to the S-M process which used 10,000 Monte Carlo simulations. Pinnacle developed simulations of key economic variables as inputs into the Cash Flow NPV simulations, while the S-M process used 10,000 simulations of target variables (default rate, prepayment rate).



## Fiscal Year 2020 Independent Actuarial Review of the Mutual Mortgage Insurance Fund: Economic Value of Forward Mortgage Insurance-In-Force

November 12, 2020

Page 313

### Appendix G: Summary of Historical and Projected Claim Rates, Non-Claim Termination Rates and Loss Severities

---

The following incremental annual summaries are shown by cohort for Fixed Rate 30, Fixed Rate 15, ARM products separately, and for all products combined.

1. **Conditional Claim Rate:** percentage of active Loans at the beginning of the evaluation year that end in claim during the evaluation year
2. **Cumulative Claim Rate:** cumulative claims as of evaluation year divided by active loans as of evaluation year 1
3. **Conditional Non-Claim Termination Rate:** percentage of active loans at the beginning of the evaluation year that end in termination by other than claim during the evaluation year
4. **Cumulative Non-Claim Termination Rate:** cumulative non-claim terminations as of evaluation year divided by active loans as of evaluation year 1
5. **Conditional Loss Rate:** claim cost net of recovery in each evaluation year divided by gross claim cost in each evaluation year
6. **Cumulative Loss Rate:** total losses net of recovery for each Fiscal Year as of the end of the evaluation year divided by total gross losses for each Fiscal Year as of the end of the evaluation year









Mutual Mortgage Insurance Fund
Forward Mortgage Summaries
Cumulative Non-Claim Termination Rate
All Products Combined

Table 8: Cumulative Number of Non-Claim Terminations as of Each Evaluation Year
Total Number of Non-Claim Terminations for each Fiscal Year as of the End of the Evaluation Year

Table with 31 columns (Fiscal Year 1990-2020) and 31 rows (Evaluation Year 1-31). Data represents cumulative non-claim terminations for each year.

Table 9: Cumulative Non-Claim Termination Rate - Table 8 / Table 1 (Evaluation Year 1)
Cumulative Non-Claim Terminations as of Evaluation Year Divided by Active Loans as of Evaluation Year 1

Table with 31 columns (Fiscal Year 1990-2020) and 31 rows (Evaluation Year 1-31). Data represents the cumulative non-claim termination rate as a percentage of active loans.





Mutual Mortgage Insurance Fund  
Forward Market Summaries  
Cumulative Loss Rate  
All Products Combined

Table 13: Cumulative Gross Claim Cost  
Total Losses for Each Fiscal Year as of the End of the Evolution Year

Table with 24 columns (Year 1-24) and 25 rows of data. The first row represents Year 1 with values from 9,071.714 to 4,293,971.941. Subsequent rows show cumulative values for Years 2 through 24, with values generally increasing and then stabilizing or slightly decreasing towards the end of the period.

Table 14: Cumulative Net Claim Cost Net of Recovery  
Total Losses for Each Fiscal Year as of the End of the Evolution Year

Table with 24 columns (Year 1-24) and 25 rows of data. The first row represents Year 1 with values from 2,480.479 to 2,145,972.949. Subsequent rows show cumulative values for Years 2 through 24, with values generally increasing and then stabilizing or slightly decreasing towards the end of the period.

Table 15: Cumulative Loss Severity - Table 14/Table 13  
Loss Severity for Each Evolution Year

Table with 24 columns (Year 1-24) and 25 rows of data. The first row represents Year 1 with values from 80.71% to 49.98%. Subsequent rows show cumulative values for Years 2 through 24, with values generally increasing and then stabilizing or slightly decreasing towards the end of the period.











Mutual Mortgage Insurance Fund  
Forward Mortgage Summaries  
Cumulative Non-Claim Termination Rate  
ARM

Table 8: Cumulative Number of Non-Claim Terminations as of Each Evaluation Year  
Total Number of Non-Claim Terminations for each Fiscal Year as of the End of the Evaluation Year

Table with columns: Fiscal Year (1990-2020), Evaluation Year (1-31), and Cumulative Number of Non-Claim Terminations. The table shows a steady increase in terminations over time, reaching over 300 by the end of 2020.

Table 9: Cumulative Non-Claims Termination Rate - Table 8 / Table 1 (Evaluation Year 1)

Cumulative Non-Claim Termination Rate as of Evaluation Year Divided by Active Loans as of Evaluation Year 1

Table with columns: Fiscal Year (1990-2020), Evaluation Year (1-31), and Cumulative Non-Claim Termination Rate. The rates fluctuate significantly, with some years showing high termination rates (up to 9.55%) and others showing lower rates (down to 0.11%).

Mutual Mortgage Insurance Fund  
 Forward Mortgage Summaries  
 Conditional Loss Rate  
 ARM

Table 10: Gross Claim Cost in Each Evolution Year

Fiscal Year	Evolution Year																																				
	1	2	3	4	5	6	7	8	9	10																											
1990	0	11,001.023	3,385.144	5,879.194	7,310.930	5,519.000	6,331.310	6,781.556	5,516.830	2,760.940	2,638.433	1,080.862	429.714	377.824	267.980	70.442	85.247	111.878	0	0	0	11,141.428	0	0	0	20,396.0	0	14.616	0	0	0	0	0	0	0	0	0

Table 11: Claim Cost Net of Recovery in Each Evolution Year

Fiscal Year	Evolution Year																																					
	1	2	3	4	5	6	7	8	9	10																												
1990	0	506.957	1,768.005	3,281.109	4,109.946	3,174.889	3,447.764	3,174.890	2,671.900	1,140.930	1,018.741	272.242	111.472	161.359	24.622	60.935	30.884	8.764	0	0	0	71.866	14.084	0	0	9,104	149.525	54.567	0	0	0	0	0	0	0	0	9.468	0

Table 12: Conditional Loss Severity = Table 11/10

Fiscal Year	Evolution Year																																				
	1	2	3	4	5	6	7	8	9	10																											
1990	0.0%	45.71%	52.23%	55.81%	56.15%	57.52%	54.46%	51.83%	48.43%	41.33%	38.04%	25.19%	25.94%	42.76%	9.19%	86.50%	36.24%	7.83%	0.00%	0.00%	64.50%	32.84%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	0.00%	65.41%	0.00%	0.00%	0.00%



Mutual Mortgage Insurance Fund  
Forward Mortgage Summary  
Cumulative Loss Rate  
ARM

Table 13: Cumulative Gross Claim Ratio  
Total Gross Losses for Each Fiscal Year as of the End of the Evaluation Year

Table with columns for Fiscal Year, Loss Rate, and 30 sequential data points. The table shows a general downward trend in loss rates over time, starting around 1.1% in 1990 and ending near 0.7% in 2020.

Table 14: Cumulative Claim Cost Net of Recovery  
Total Losses Net of Recovery for Each Fiscal Year as of the End of the Evaluation Year

Table with columns for Fiscal Year, Net Loss Rate, and 30 sequential data points. The net loss rates are consistently lower than the gross loss rates, starting around 0.5% in 1990 and ending near 0.2% in 2020.

Table 15: Cumulative Loss Severity - Table 14/Table 13  
Loss Severity for Each Evaluation Year

Table with columns for Fiscal Year, Loss Severity, and 30 sequential data points. The loss severity values fluctuate between 40% and 60% over the period.

**Mutual Mortgage Insurance Fund**  
**Forward Mortgage Summaries**  
**Active Loans**  
**FRM15**

Table 1: Number of Loans Active at the End of Each Evaluation Year

Fiscal Year	Evaluation Year															
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1990	26,921	26,161	23,761	18,337	13,748	12,318	10,593	9,342	7,935	6,663	5,830	5,051	4,214	3,360	2,470	318
1991	29,468	28,170	23,138	17,556	15,772	13,607	11,926	9,947	8,096	7,064	6,072	4,958	3,892	3,146	2,316	257
1992	41,059	38,180	32,616	29,998	26,419	23,453	19,657	16,031	14,102	11,991	9,513	7,229	5,629	4,420	3,138	224
1993	116,811	109,498	103,092	93,669	84,805	73,504	61,526	54,630	47,053	38,340	28,532	22,627	18,213	14,233	10,341	660
1994	143,241	137,352	127,070	116,698	103,100	88,597	79,374	69,271	57,672	44,603	35,714	29,385	23,698	19,050	11,594	331
1995	18,057	16,906	15,599	13,560	11,491	10,337	8,956	7,434	5,894	4,890	4,151	3,576	3,059	2,587	1,727	112
1996	31,745	30,401	27,432	23,583	21,213	18,400	15,074	11,259	8,916	7,390	6,120	5,238	4,439	3,624	2,523	92
1997	20,055	18,671	16,239	14,829	13,029	10,586	7,960	6,354	5,267	4,497	3,810	3,353	2,916	2,494	1,800	124
1998	36,525	34,390	32,100	28,745	24,017	17,320	13,607	11,254	9,501	8,243	7,178	6,317	5,477	4,554	3,368	289
1999	43,371	41,691	37,905	32,262	23,856	18,871	15,705	13,478	11,879	10,604	9,409	8,461	7,298	6,084	4,302	116
2000	10,197	8,822	6,784	4,607	3,487	2,819	2,353	2,024	1,808	1,637	1,458	1,336	1,215	1,015	730	44
2001	25,106	22,445	15,067	11,148	8,817	7,489	6,563	5,824	5,297	4,795	4,293	3,836	3,345	2,784	2,055	233
2002	46,782	37,669	30,216	24,759	21,335	18,920	17,161	15,720	14,391	13,092	11,641	10,202	8,824	7,193	5,081	450
2003	59,594	53,429	45,995	40,300	36,135	32,986	30,311	27,922	25,597	23,185	20,210	17,829	15,219	12,239	8,239	11
2004	52,263	46,736	41,364	37,396	34,522	32,183	29,889	27,737	25,480	22,702	19,997	17,709	15,008	11,831	5,796	20
2005	19,801	18,011	16,287	14,982	13,976	13,017	12,107	11,196	10,160	9,118	7,853	6,941	5,948	4,731	2,960	91
2006	10,420	9,413	8,425	7,536	6,870	6,344	5,796	5,172	4,708	4,214	3,677	3,244	2,772	2,297	1,433	10
2007	7,224	6,428	5,428	4,823	4,400	3,929	3,426	3,038	2,739	2,437	2,129	1,861	1,645	1,377	897	3
2008	24,117	20,750	18,233	16,262	14,159	11,814	10,360	9,212	8,147	7,260	6,406	5,731	4,981	4,123	3,014	26
2009	59,685	55,673	49,780	42,259	34,228	30,006	26,152	22,974	20,236	17,905	15,807	13,780	11,455	9,261	6,172	50
2010	84,857	79,565	69,364	57,592	51,083	44,657	39,034	34,251	30,378	27,096	23,581	19,861	16,275	12,781	7,892	32
2011	87,603	76,621	64,000	56,816	49,177	42,543	36,868	32,600	28,942	25,068	21,279	17,995	14,574	11,577	7,302	44
2012	99,358	90,189	81,746	72,618	63,927	56,466	50,690	45,796	40,122	34,153	28,927	24,165	19,650	15,352	9,434	22
2013	65,580	62,329	56,934	51,372	46,115	41,630	37,757	33,292	28,712	24,890	21,098	17,873	14,671	11,422	6,913	106
2014	29,419	25,929	22,418	19,264	16,886	14,925	12,948	11,489	10,135	8,967	7,756	6,705	5,634	4,531	2,812	60
2015	29,689	26,595	22,932	19,799	17,328	14,898	12,984	11,469	10,053	8,874	7,722	6,621	5,463	4,299	2,692	73
2016	31,079	28,193	24,733	21,847	18,620	16,183	14,339	12,611	11,088	9,737	8,380	7,155	5,860	4,553	2,889	59
2017	32,209	29,157	25,663	21,712	18,839	16,540	14,509	12,781	11,311	9,899	8,453	7,085	5,732	4,471	2,727	53
2018	20,381	18,157	14,519	12,511	10,842	9,372	8,214	7,226	6,310	5,516	4,719	4,010	3,285	2,605	1,548	45
2019	15,541	12,278	10,505	9,028	7,753	6,726	5,892	5,121	4,432	3,848	3,177	2,685	2,174	1,679	985	20
2020	11,837	10,666	9,315	8,050	7,026	6,122	5,312	4,584	3,942	3,364	2,858	2,380	1,931	1,485	846	11



Mutual Mortgage Insurance Fund  
Forward Mortgage Summaries  
Conditional Claim Rate  
FRM15

Table 2: Number of Claims in Each Evaluation Year

Fiscal Year	Evaluation Year															
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1990	0	41	147	209	204	201	134	88	59	41	36	12	5	7	4	1
1991	1	32	121	156	188	158	106	75	55	28	14	7	4	4	6	2
1992	0	21	92	99	116	79	84	50	30	22	9	5	6	3	2	0
1993	0	47	160	193	193	172	122	101	54	38	24	18	9	6	4	1
1994	5	98	270	336	345	263	206	107	89	53	35	18	17	9	4	1
1995	3	19	54	80	69	58	34	27	26	18	5	10	3	2	1	0
1996	0	19	70	100	105	86	64	45	33	25	17	11	1	3	3	2
1997	0	12	53	71	69	43	25	21	25	17	7	1	4	2	4	0
1998	0	11	71	66	96	67	46	36	15	17	6	12	12	1	6	1
1999	0	15	66	85	110	83	48	22	19	16	17	14	10	11	12	2
2000	0	6	42	72	61	31	29	13	11	14	11	5	4	3	5	2
2001	0	21	77	98	78	54	28	16	26	27	24	10	13	10	12	3
2002	1	37	112	104	87	50	39	33	41	50	33	43	18	24	30	6
2003	0	39	85	90	64	78	80	95	86	83	89	70	45	54	25	7
2004	8	47	103	103	98	109	148	116	125	110	86	73	70	34	18	2
2005	1	64	135	119	127	123	89	70	87	68	67	56	37	15	9	2
2006	3	103	138	158	128	91	93	101	69	63	47	49	23	10	9	0
2007	2	63	149	137	87	119	139	85	66	65	42	27	18	9	4	1
2008	3	91	268	256	328	489	312	216	181	127	69	58	24	6	6	8
2009	7	120	187	323	534	408	401	262	172	111	73	38	23	15	14	3
2010	1	45	161	307	283	276	238	177	111	72	46	27	16	23	15	2
2011	1	40	131	159	169	153	112	91	56	26	19	22	18	12	7	1
2012	1	34	82	103	119	103	64	44	27	27	17	21	13	15	15	1
2013	0	9	46	65	89	57	46	33	25	28	24	12	12	15	9	2
2014	0	13	22	53	53	32	18	17	24	20	11	12	10	8	5	2
2015	0	10	29	42	35	31	21	26	29	18	18	11	6	7	4	1
2016	1	6	36	44	31	25	36	36	28	26	18	10	10	4	5	2
2017	0	8	31	22	16	31	26	28	28	22	20	15	12	8	5	1
2018	0	10	15	20	29	41	39	21	17	9	16	10	11	1	1	1
2019	0	4	17	26	34	35	31	20	22	14	11	4	2	2	2	2
2020	0	6	20	23	20	28	14	13	13	8	6	6	5	3	0	2



















Mutual Mortgage Insurance Fund  
Forward Mortgage Summaries  
Conditional Loss Rate  
FRM15

Table 11: Claim Cost Net of Recovery in Each Evaluation Year

Fiscal Year	Evaluation Year															
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1990	0	1,355,718	5,166,962	9,577,641	10,314,347	13,060,906	8,419,627	3,662,183	2,615,340	1,570,490	1,360,768	349,569	122,362	163,991	96,222	19,182
1991	46,891	951,855	4,529,024	6,937,453	12,153,941	10,379,713	4,835,228	3,340,612	2,072,140	908,518	347,106	172,034	29,895	51,919	(136,131)	(9,613)
1992	0	617,859	2,280,752	4,138,880	5,336,518	2,851,796	2,381,209	1,314,941	577,428	505,450	127,158	32,264	26,826	61,222	59,221	0
1993	0	1,338,268	5,828,008	6,590,116	5,137,706	3,441,287	3,051,653	2,197,158	953,146	600,712	187,852	244,113	7,977	92,452	100,479	(458)
1994	95,848	2,783,429	8,494,430	8,421,910	7,577,776	5,439,398	3,873,778	1,825,826	1,499,772	634,015	433,059	320,564	312,093	178,281	40,704	15,323
1995	47,920	283,239	1,003,106	1,595,129	1,232,106	942,993	480,932	412,936	242,160	192,646	76,915	204,506	43,033	47,684	(5,022)	0
1996	0	447,824	1,470,049	2,039,818	2,303,738	1,430,511	926,304	603,407	650,601	437,181	304,831	240,778	27,397	21,413	13,383	27,274
1997	0	285,939	1,194,443	1,530,560	1,626,493	751,308	544,505	461,198	329,666	261,699	98,090	23,843	62,111	43,891	22,540	0
1998	0	188,031	1,533,596	1,347,850	2,097,206	1,159,268	826,010	733,161	489,778	252,221	89,196	221,529	414,307	0	224,110	0
1999	0	303,212	1,251,676	1,725,734	2,271,989	1,638,328	1,116,574	544,829	479,316	362,372	482,095	357,850	179,834	201,570	234,087	18,769
2000	0	143,357	1,001,034	1,684,177	1,656,261	991,748	722,292	375,325	356,154	419,331	413,404	136,337	38,631	28,219	74,124	0
2001	0	436,581	2,175,999	2,882,580	2,231,060	1,656,132	1,186,981	595,663	793,356	730,399	931,814	341,166	263,224	246,394	294,445	37,029
2002	0	961,445	3,469,719	3,195,542	2,429,415	1,436,828	1,503,347	1,424,991	1,359,789	1,604,479	1,128,069	1,266,188	289,693	601,019	799,130	189,162
2003	0	1,160,691	3,166,811	2,720,599	2,026,113	2,502,080	3,122,807	3,685,666	3,069,631	3,086,812	2,536,445	1,303,315	929,107	1,444,687	394,819	284,973
2004	197,201	1,349,421	2,916,416	3,520,598	3,778,608	4,373,201	5,858,298	4,425,560	4,533,173	3,016,751	2,341,641	2,112,114	1,879,021	446,825	632,897	0
2005	0	2,288,062	4,995,732	4,878,508	5,252,999	5,676,227	4,039,481	2,902,635	3,831,690	2,162,706	2,250,048	1,466,829	1,030,214	56,769	83,241	119,708
2006	167,017	4,749,132	7,170,972	8,792,086	7,283,499	5,322,231	5,600,418	4,671,021	3,540,666	2,615,465	1,802,317	1,668,972	778,891	185,668	168,606	0
2007	98,263	3,240,730	8,541,515	8,843,001	5,725,362	8,338,847	7,857,203	4,441,641	3,013,354	3,301,674	1,817,983	1,238,686	594,884	273,598	148,674	22,122
2008	180,714	5,053,501	17,127,472	17,888,687	21,776,693	30,183,601	16,965,676	11,133,809	9,444,156	6,863,486	2,021,045	2,138,144	1,168,571	240,556	128,478	149,635
2009	310,239	7,641,425	11,955,227	20,390,209	32,659,266	20,585,641	19,041,647	13,014,982	7,280,949	4,250,248	2,400,170	1,313,275	803,579	425,187	261,636	56,611
2010	0	2,258,486	9,667,062	16,733,653	13,117,747	12,867,799	11,390,106	6,594,915	3,864,557	1,852,033	1,128,674	1,097,113	494,110	602,902	220,142	14,440
2011	0	2,539,877	6,219,472	6,413,372	7,910,189	6,903,460	4,170,414	2,720,460	758,814	620,560	783,363	828,486	627,063	260,718	135,567	45,130
2012	61,140	1,515,694	3,340,360	4,668,440	4,873,554	3,676,288	2,258,445	1,411,620	741,571	1,165,685	566,139	683,332	507,508	317,475	337,111	24,836
2013	0	99,333	1,689,860	2,372,878	3,209,164	1,866,279	1,681,534	1,506,375	1,081,389	1,126,316	812,705	316,204	441,838	398,079	146,885	37,111
2014	0	345,717	830,534	2,042,565	2,088,830	844,892	503,373	805,840	982,694	760,392	459,236	341,179	231,127	169,723	131,252	13,750
2015	0	370,298	1,170,944	1,480,450	1,097,798	969,743	955,917	993,707	1,150,798	733,283	544,949	317,432	164,339	235,680	110,215	11,056
2016	0	97,395	1,267,871	1,194,090	1,065,760	1,226,858	1,672,658	1,457,016	997,634	951,771	587,518	288,789	367,132	132,588	126,863	26,353
2017	0	216,270	942,042	716,079	763,113	1,109,452	1,066,089	1,141,844	1,074,971	796,442	756,809	513,948	353,901	210,298	143,960	25,345
2018	0	251,501	618,234	844,750	1,349,003	1,806,991	1,577,759	921,137	753,584	347,920	583,405	243,844	412,097	35,981	16,251	16,710
2019	0	18,216	911,937	1,449,447	1,528,838	1,530,638	1,400,868	1,049,459	1,255,114	488,525	546,611	193,698	53,833	77,864	37,871	51,369
2020	0	226,144	898,713	1,189,353	1,049,855	1,553,620	760,009	593,940	743,611	451,763	216,803	230,478	218,971	87,503	0	38,625

Mutual Mortgage Insurance Fund  
Forward Mortgage Summaries  
Conditional Loss Rate  
FRM15

Table 12: Conditional Loss Severity = Table 11/Table 10  
Loss Severity for Each Evaluation Year

Fiscal Year	Evaluation Year															
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1990	0.00%	62.52%	58.96%	64.50%	68.37%	77.06%	77.17%	60.48%	62.62%	53.09%	52.03%	43.65%	42.11%	39.97%	69.19%	92.53%
1991	34.42%	50.46%	55.46%	63.18%	75.03%	76.63%	62.65%	57.36%	54.68%	50.85%	38.77%	38.38%	15.32%	34.24%	-43.76%	-20.96%
1992	0.00%	46.00%	47.26%	66.81%	66.75%	57.72%	50.06%	44.88%	42.50%	46.91%	29.94%	27.67%	22.15%	95.28%	115.83%	0.00%
1993	0.00%	53.80%	62.50%	54.34%	45.48%	37.09%	44.29%	40.56%	35.23%	35.77%	25.84%	43.84%	3.33%	53.00%	83.31%	-1.44%
1994	29.41%	53.79%	55.99%	43.80%	37.65%	37.73%	37.97%	35.83%	38.56%	32.61%	38.20%	49.78%	70.58%	95.07%	51.31%	65.54%
1995	34.87%	29.15%	35.91%	37.48%	36.31%	35.01%	27.91%	36.76%	24.82%	34.10%	38.13%	61.55%	54.81%	107.32%	-15.09%	0.00%
1996	0.00%	43.01%	36.67%	35.04%	43.47%	32.81%	28.28%	31.58%	41.90%	51.64%	50.28%	63.00%	72.95%	34.07%	16.31%	104.65%
1997	0.00%	35.97%	34.31%	39.20%	42.11%	34.17%	42.28%	44.95%	25.75%	34.99%	47.94%	111.55%	58.70%	41.56%	16.26%	0.00%
1998	0.00%	37.15%	33.42%	32.69%	34.81%	34.16%	32.53%	40.34%	54.30%	46.13%	39.27%	50.54%	71.13%	0.00%	78.51%	0.00%
1999	0.00%	38.59%	29.22%	34.85%	32.69%	35.11%	41.61%	48.40%	57.90%	43.79%	56.68%	65.76%	48.20%	57.48%	45.69%	20.30%
2000	0.00%	34.36%	38.09%	32.90%	39.44%	50.29%	48.27%	45.61%	64.18%	56.48%	68.10%	73.71%	37.09%	20.59%	38.92%	0.00%
2001	0.00%	28.05%	36.54%	39.20%	39.59%	43.59%	52.81%	53.58%	47.95%	54.83%	71.17%	79.21%	43.26%	39.40%	50.36%	7.04%
2002	0.00%	42.37%	39.41%	40.21%	35.30%	42.09%	59.48%	61.30%	58.84%	57.20%	63.59%	54.79%	32.25%	36.37%	50.10%	66.38%
2003	0.00%	35.61%	42.20%	40.60%	44.90%	45.42%	55.43%	60.23%	55.68%	62.11%	43.70%	26.22%	33.78%	40.92%	31.40%	62.95%
2004	33.42%	39.04%	38.22%	46.45%	51.83%	58.02%	58.27%	60.09%	54.00%	48.02%	40.62%	52.62%	43.43%	38.56%	50.16%	0.00%
2005	0.00%	37.11%	43.18%	48.57%	49.79%	56.37%	56.83%	60.60%	54.83%	41.54%	51.79%	43.88%	53.42%	8.32%	35.80%	99.29%
2006	43.88%	46.85%	52.97%	56.52%	57.68%	65.02%	64.89%	54.75%	53.74%	52.41%	48.46%	64.24%	52.96%	34.67%	52.62%	0.00%
2007	44.15%	53.61%	60.34%	64.78%	68.44%	67.21%	56.60%	57.42%	56.08%	57.12%	47.57%	66.72%	47.45%	62.09%	54.61%	70.24%
2008	41.83%	48.12%	59.67%	64.43%	63.52%	58.63%	56.21%	56.16%	58.28%	58.73%	57.92%	56.65%	71.87%	63.08%	49.17%	49.84%
2009	50.97%	57.56%	63.33%	63.28%	53.00%	48.47%	51.38%	53.19%	56.74%	56.37%	52.53%	68.03%	55.40%	69.35%	50.27%	57.22%
2010	0.00%	54.52%	61.33%	52.81%	46.07%	47.57%	55.18%	55.06%	53.82%	51.45%	52.29%	54.61%	59.78%	63.77%	69.27%	48.21%
2011	0.00%	62.41%	50.24%	41.32%	46.58%	50.41%	50.97%	58.28%	22.42%	65.13%	53.10%	60.23%	66.45%	66.64%	50.09%	45.29%
2012	58.88%	47.02%	40.19%	43.40%	44.52%	45.57%	56.29%	48.85%	66.16%	54.48%	53.70%	69.00%	61.25%	65.06%	65.55%	41.68%
2013	0.00%	10.32%	48.03%	47.84%	56.32%	52.91%	55.05%	70.63%	47.40%	52.66%	63.33%	49.30%	63.82%	52.84%	50.26%	41.93%
2014	0.00%	39.94%	45.23%	43.90%	52.18%	49.60%	52.32%	57.72%	58.52%	51.15%	52.66%	48.31%	53.58%	51.02%	49.28%	100.00%
2015	0.00%	52.28%	57.53%	60.44%	51.25%	61.57%	48.79%	52.69%	70.62%	51.55%	65.47%	64.30%	57.36%	55.43%	38.76%	
2016	0.00%	29.88%	54.99%	52.80%	58.63%	61.88%	60.71%	61.75%	61.11%	60.27%	65.11%	63.88%	65.92%	70.14%	53.90%	100.00%
2017	0.00%	32.37%	42.66%	63.17%	47.04%	47.12%	50.04%	63.02%	67.88%	62.62%	63.76%	59.88%	58.48%	60.79%	61.69%	57.88%
2018	0.00%	41.62%	60.53%	51.08%	58.43%	60.12%	58.60%	56.68%	49.82%	52.56%	53.40%	70.31%	63.52%	57.73%	100.00%	55.61%
2019	0.00%	10.22%	51.70%	65.36%	58.18%	63.56%	64.62%	81.38%	63.72%	63.81%	68.58%	54.65%	54.86%	50.49%	64.61%	66.33%
2020	0.00%	31.91%	54.10%	70.82%	54.10%	60.18%	63.87%	62.33%	60.86%	57.82%	47.95%	59.13%	55.91%	54.56%	0.00%	63.07%





Mutual Mortgage Insurance Fund  
Forward Mortgage Summaries  
Cumulative Loss Rate  
FRM15

Table 15: Cumulative Loss Severity = Table 14/Table 13  
Loss Severity for Each Evaluation Year

Fiscal Year	Evaluation Year															
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1990	0.00%	62.52%	59.66%	62.45%	64.64%	68.28%	69.69%	68.94%	68.61%	68.05%	67.55%	67.33%	67.24%	67.11%	67.12%	67.12%
1991	34.42%	49.38%	54.25%	58.88%	65.88%	68.74%	67.94%	66.98%	66.30%	65.91%	65.56%	65.39%	65.26%	65.19%	64.72%	64.67%
1992	0.00%	46.00%	46.99%	56.92%	60.78%	60.18%	58.58%	57.36%	56.78%	56.48%	56.16%	56.07%	55.96%	56.03%	56.11%	56.11%
1993	0.00%	53.80%	60.67%	57.46%	53.62%	50.18%	49.39%	48.55%	47.94%	47.61%	47.35%	47.32%	47.15%	47.17%	47.24%	47.21%
1994	29.41%	52.35%	55.02%	49.61%	45.60%	44.08%	43.34%	42.92%	42.73%	42.53%	42.48%	42.53%	42.65%	42.75%	42.76%	42.77%
1995	34.87%	29.86%	34.19%	35.91%	36.03%	35.83%	34.98%	35.10%	34.54%	34.53%	34.57%	35.03%	35.11%	35.28%	35.19%	35.19%
1996	0.00%	43.01%	37.98%	36.41%	38.72%	37.47%	36.20%	35.86%	36.20%	36.20%	36.67%	37.30%	37.34%	37.28%	37.28%	37.34%
1997	0.00%	35.97%	34.61%	36.80%	38.50%	37.84%	38.20%	38.62%	37.70%	37.59%	37.70%	37.79%	37.90%	37.92%	37.77%	37.77%
1998	0.00%	37.15%	33.79%	33.30%	33.90%	33.94%	33.78%	34.29%	35.05%	35.30%	35.33%	35.60%	36.40%	36.38%	36.85%	36.80%
1999	0.00%	38.59%	30.67%	32.74%	32.72%	33.23%	34.16%	34.79%	35.52%	35.77%	36.40%	36.97%	37.11%	37.36%	37.50%	37.45%
2000	0.00%	34.36%	37.58%	34.65%	36.27%	38.20%	39.15%	39.47%	40.27%	40.94%	41.83%	42.14%	42.12%	41.96%	41.93%	41.68%
2001	0.00%	28.05%	34.78%	36.97%	37.69%	38.61%	39.81%	40.37%	40.80%	41.41%	42.63%	43.11%	43.11%	43.05%	43.17%	42.62%
2002	0.00%	42.31%	40.01%	40.09%	38.82%	39.20%	40.81%	42.20%	43.26%	44.25%	45.09%	45.60%	45.33%	45.01%	45.18%	45.31%
2003	0.00%	35.61%	40.20%	40.35%	41.29%	42.12%	44.38%	46.85%	47.94%	49.36%	48.76%	46.91%	46.34%	46.05%	45.78%	45.90%
2004	33.42%	38.22%	38.22%	41.46%	44.31%	47.34%	49.83%	51.30%	51.67%	51.33%	50.47%	50.58%	50.20%	50.03%	50.03%	50.03%
2005	0.00%	36.38%	40.78%	43.58%	45.29%	47.59%	48.77%	49.71%	50.24%	49.61%	49.74%	49.49%	49.59%	49.25%	49.21%	49.28%
2006	43.88%	46.74%	50.25%	52.71%	55.40%	55.42%	56.60%	56.19%	55.98%	55.68%	55.91%	55.87%	55.75%	55.74%	55.74%	55.74%
2007	44.15%	53.27%	58.17%	60.82%	62.32%	63.43%	62.05%	61.58%	61.22%	60.95%	60.39%	60.52%	60.34%	60.35%	60.33%	60.34%
2008	41.83%	47.87%	56.41%	59.72%	61.00%	60.20%	59.55%	59.22%	59.15%	59.13%	59.11%	59.07%	59.16%	59.16%	59.15%	59.14%
2009	50.97%	57.27%	60.76%	62.01%	57.62%	55.32%	54.62%	54.46%	54.58%	54.64%	54.60%	54.70%	54.70%	54.74%	54.73%	54.73%
2010	0.00%	54.32%	59.86%	55.53%	52.17%	51.01%	51.68%	51.97%	52.06%	52.05%	52.05%	52.08%	52.13%	52.20%	52.23%	52.23%
2011	0.00%	61.49%	53.06%	47.37%	47.10%	47.82%	48.18%	48.81%	47.68%	47.88%	47.98%	48.18%	48.39%	48.47%	48.48%	48.47%
2012	58.88%	47.39%	42.25%	42.80%	43.37%	43.80%	44.90%	45.14%	45.61%	45.98%	46.13%	46.56%	46.78%	46.94%	47.12%	47.11%
2013	0.00%	10.32%	39.93%	44.08%	48.69%	49.49%	50.27%	52.09%	51.68%	51.75%	52.26%	52.19%	52.45%	52.46%	52.44%	52.41%
2014	0.00%	39.94%	43.54%	43.77%	46.73%	47.11%	47.46%	48.39%	49.39%	49.53%	49.67%	49.62%	49.70%	49.73%	49.72%	49.75%
2015	0.00%	52.28%	56.18%	58.19%	56.16%	57.12%	55.62%	55.18%	55.63%	56.61%	56.30%	56.55%	56.66%	56.68%	56.67%	56.64%
2016	0.00%	22.48%	49.85%	51.18%	53.17%	55.13%	56.46%	57.36%	57.75%	57.98%	58.34%	58.48%	58.69%	58.81%	58.75%	58.80%
2017	0.00%	32.37%	40.27%	46.74%	46.83%	46.92%	47.57%	49.92%	52.02%	52.94%	53.74%	54.05%	54.21%	54.34%	54.43%	54.44%
2018	0.00%	41.62%	53.50%	52.28%	54.82%	56.67%	57.13%	57.08%	56.32%	56.15%	55.97%	56.27%	56.54%	56.55%	56.59%	56.58%
2019	0.00%	10.22%	47.90%	57.21%	57.59%	59.15%	60.19%	62.35%	62.54%	62.60%	62.89%	62.72%	62.67%	62.56%	62.57%	62.58%
2020	0.00%	31.91%	47.47%	57.15%	56.16%	57.38%	58.17%	58.54%	58.77%	58.72%	58.35%	58.37%	58.30%	58.26%	58.26%	58.28%







Mutual Mortgage Insurance Fund
Forward Mortgage Summaries
Cumulative Claim Rate
FRM30

Table 4: Cumulative Number of Claims as of Each Evaluation Year

Table with 32 columns (Fiscal Year 1990-2020) and 32 rows (Evaluation Year 1-32). Shows cumulative number of claims over time.

Table 5: Cumulative Claim Rate - Table 4 / Table 1 [Evaluation Year 1]
Cumulative Claims as of Evaluation Year Divided by Active Loans as of Evaluation Year 1

Table with 32 columns (Fiscal Year 1990-2020) and 32 rows (Evaluation Year 1-32). Shows cumulative claim rate percentages over time.

Mutual Mortgage Insurance Fund
Forward Mortgage Summaries
Conditional Non-Claim Termination Rate
FRM30

Table 6: Number of Non-Claim Terminations in Each Evaluation Year

Table with 32 columns (Fiscal Year and Evaluation Year 1-30) and 32 rows of data showing the number of non-claim terminations for each year from 1990 to 2020.

Table 7: Non-Claim Termination Rate - Table 6 / Table 1
Percentage of Active Loans at the Beginning of the Evaluation Year that end in Termination by Other Than Claim During the Evaluation Year

Table with 32 columns (Fiscal Year and Evaluation Year 1-30) and 32 rows of data showing the percentage of active loans that end in termination by other than claim for each year from 1990 to 2020.





